

Confirmation of the exotic $Z(4430)^-$ resonance at LHCb

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Edinburgh, 16th May 2014

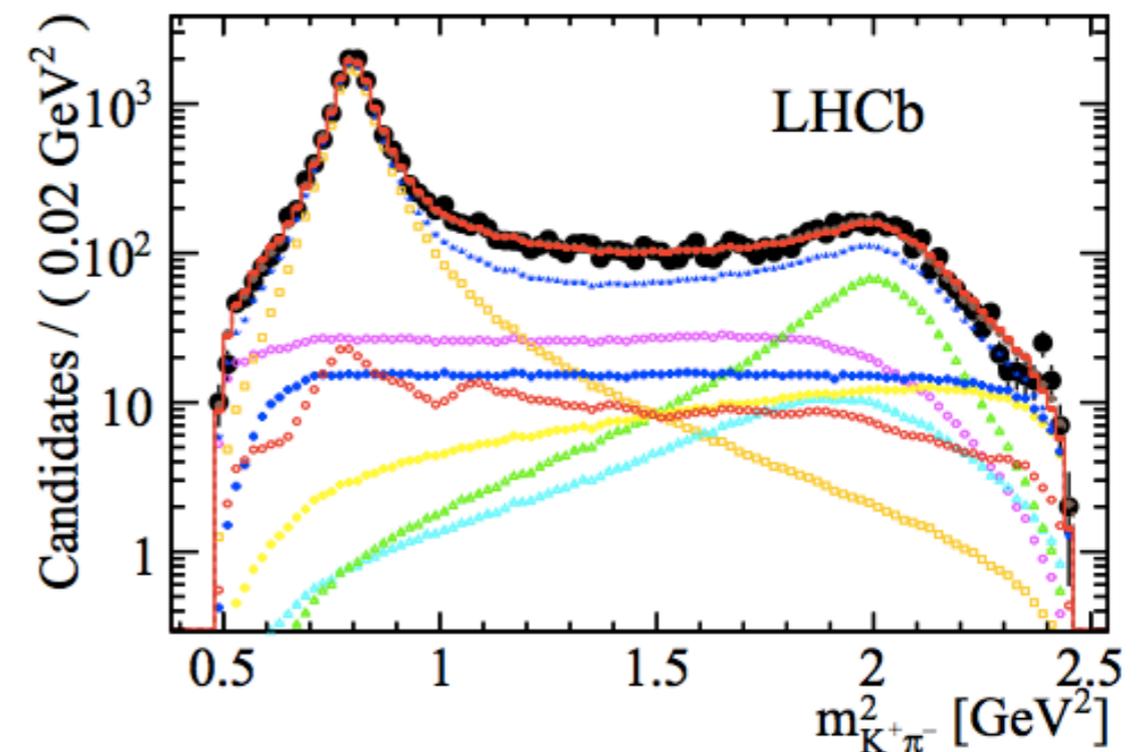


Science & Technology
Facilities Council

Overview

1. Exotic spectroscopy: motivation
2. Introduction to the LHCb experiment
3. Reminder of Dalitz plots and amplitude analyses
4. The $Z(4430)^-$
 - History
 - Searching for the $Z(4430)^-$ in $B^0 \rightarrow \psi(2S)K^+\pi^-$ decays
 - Determining the quantum numbers (J^P)
5. Other exotic spectroscopy results
 - $X(3872)$
 - The scalar mesons, $f_0(500)$ and $f_0(980)$

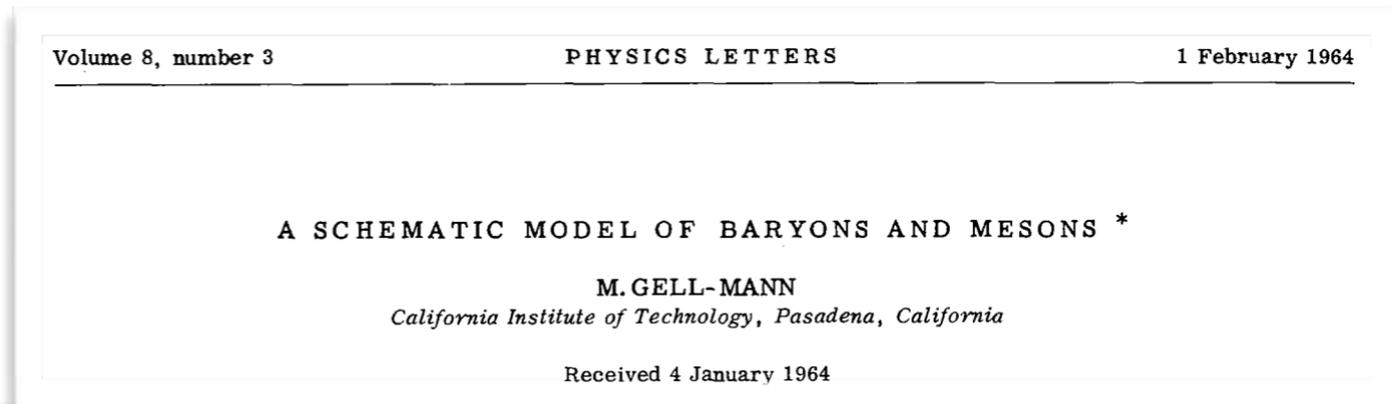
Will give some technical details to explain plots like this



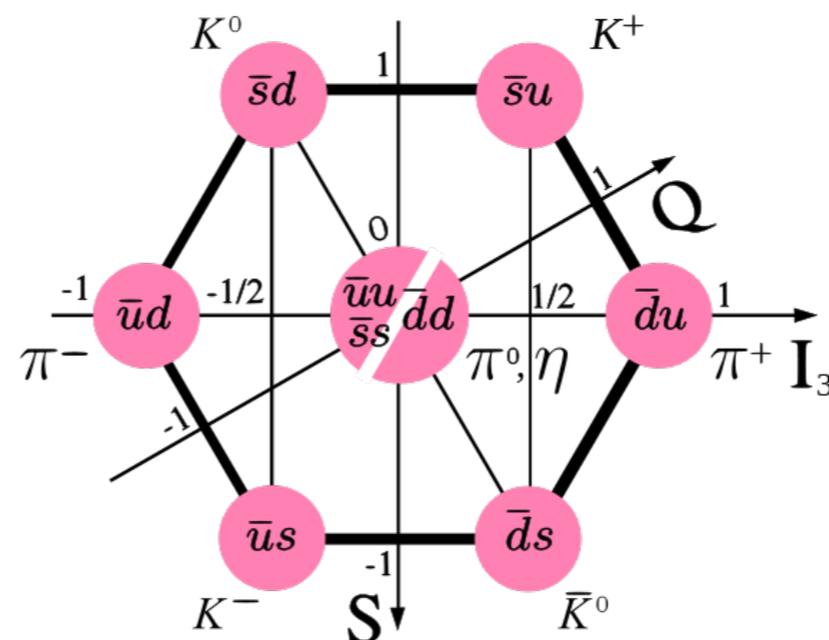
arXiv:1404.1903
accepted by PRL

“Three quarks for Muster Mark!”

- Bound states of quarks to form mesons and baryons were first proposed in 1964 by Gell-Mann and Zweig.
- $qq\bar{q}\bar{q}$ states are not *a priori* excluded.
- Light quark **spectroscopy** used to understand structure of these states.
 - Difficult due to wide overlapping states, background.
 - Highly relativistic constituents (u, d and s quarks).
- What about heavier quarks?



We then refer to the members $u^{\frac{2}{3}}$, $d^{-\frac{1}{3}}$, and $s^{-\frac{1}{3}}$ of the triplet as "quarks" q and the members of the anti-triplet as anti-quarks \bar{q} . Baryons can now be constructed from quarks by using the combinations (qqq) , $(qqq\bar{q})$, etc., while mesons are made out of $(q\bar{q})$, $(qq\bar{q}\bar{q})$, etc. It is assuming that the lowest



Charmonium spectroscopy ($c\bar{c}$)

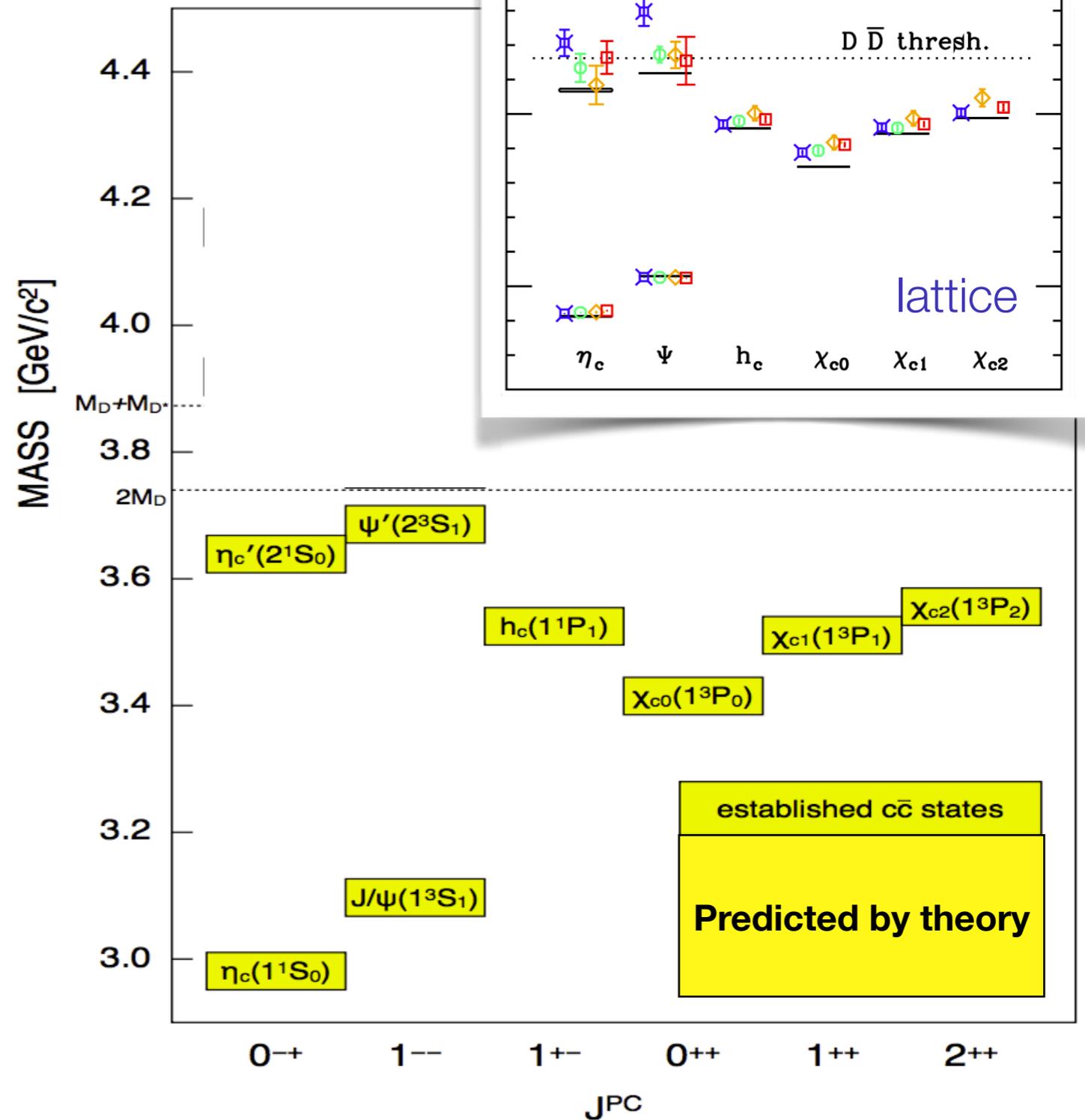
- Simpler system to analyse since c quark is heavier
 - non-relativistic calculations
 - potential models
 - lattice QCD
 - narrow, non-overlapping states below $D\bar{D}$ threshold
 - no mixing of $c\bar{c}$ with lighter $q\bar{q}$ states.

Classify using J^{PC}

$$J = L + S$$

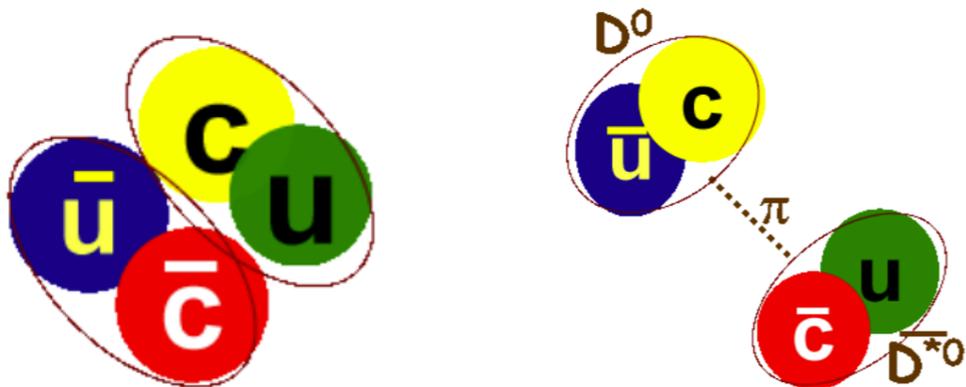
$$P = (-1)^{L+1}$$

$$C = (-1)^{L+S}$$

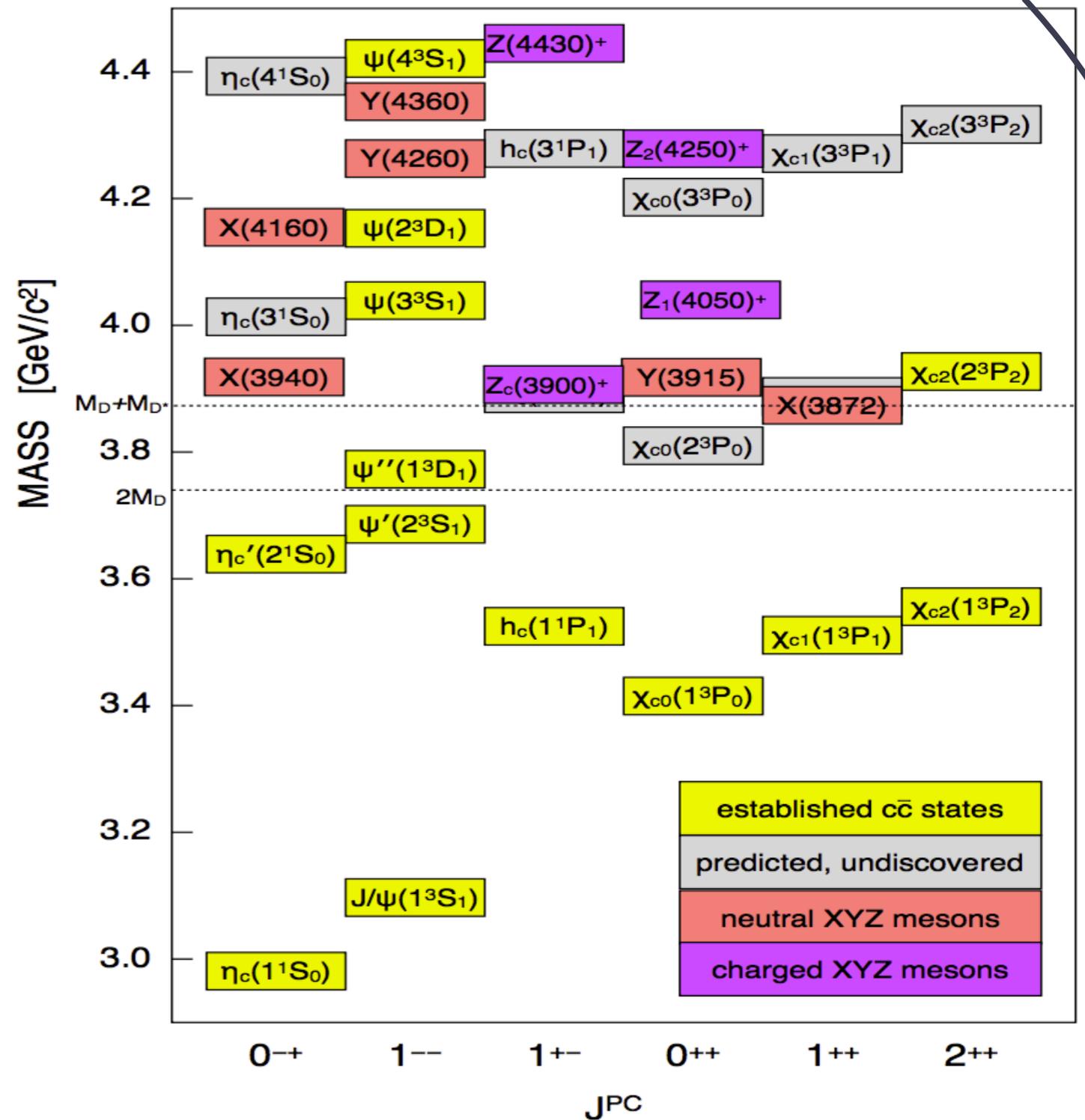


Exotic charmonium spectroscopy

- Many different exotic (XYZ) states have been seen.
 - BESIII, Belle/BaBar, CDF/D0
 - mass/width, decay, J^{PC}
- Are these $[qq][\bar{q}\bar{q}]$ (tetraquarks), mesonic molecules, threshold effects, hybrids...?
- No clear pattern: need experimental and theoretical study to understand strong interaction dynamics that can cause their production and structure.



Thresholds



Olsen arXiv:1403.1254

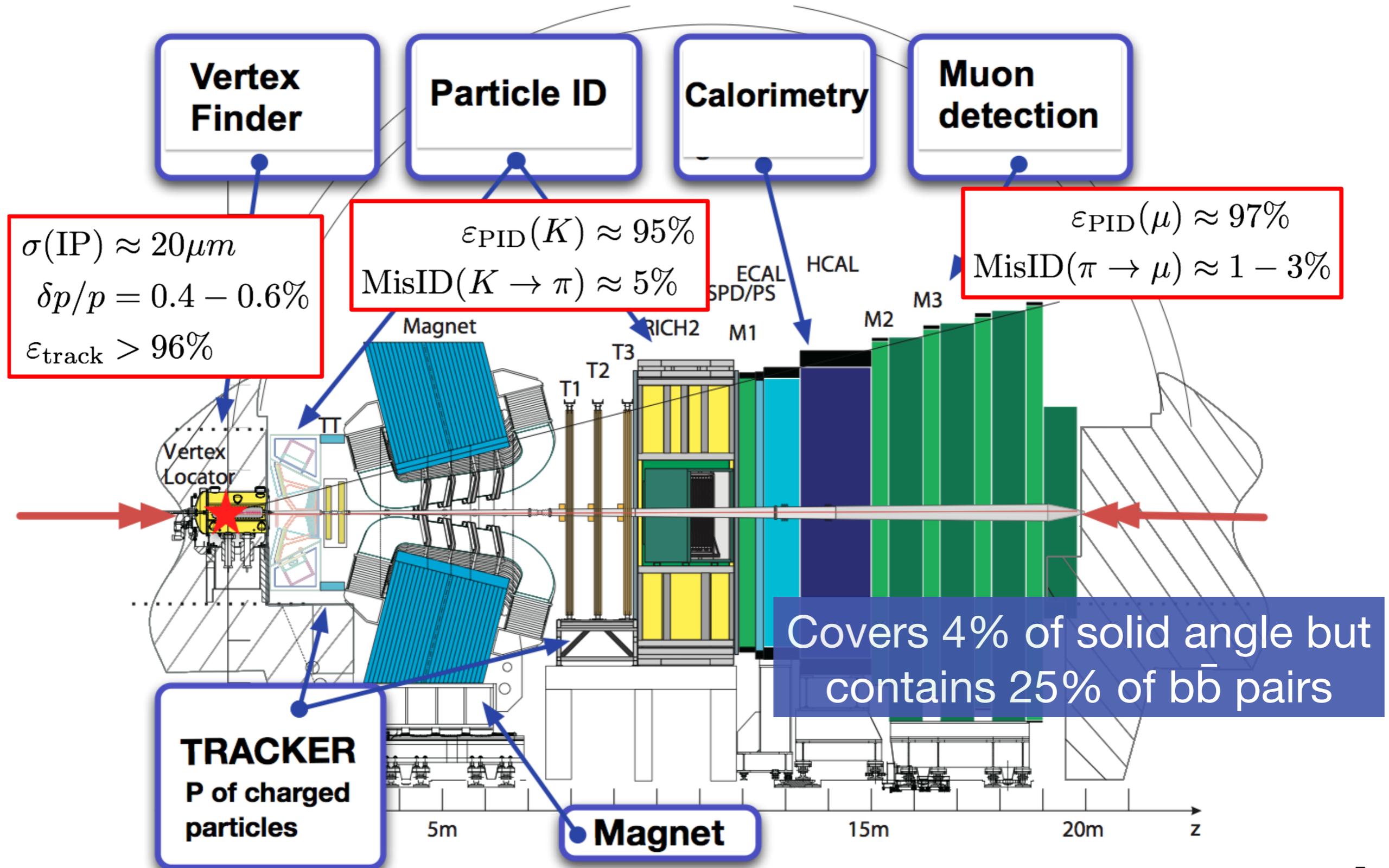
The LHCb experiment

- Rare B decays
- CP violation
- Charm physics
- (Exotic) spectroscopy
- QCD and electroweak

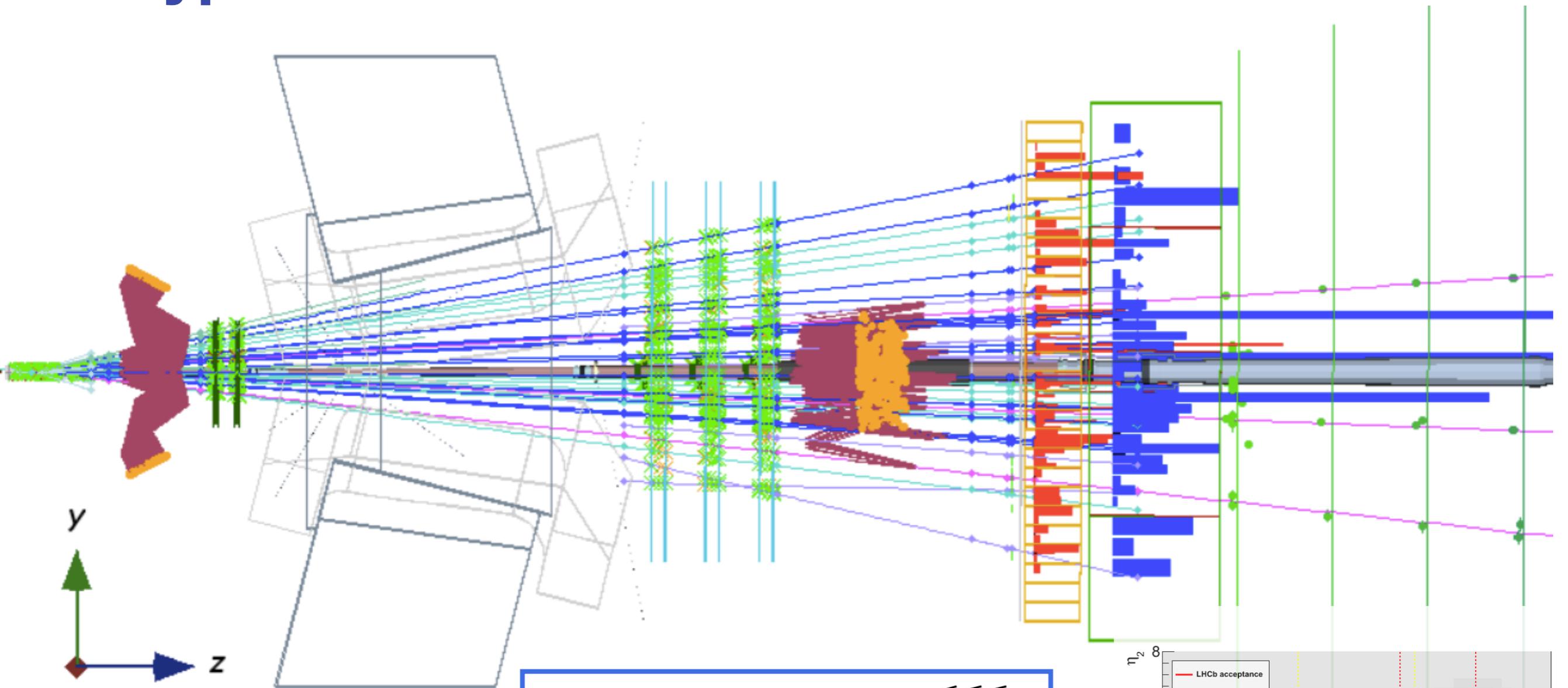


- ~900 physicists from 64 universities/labs in 16 countries.
- Running since 2010, **>180 papers published.**
- O(100k) **$b\bar{b}$** pairs produced/sec.

The LHCb detector



A typical LHCb event

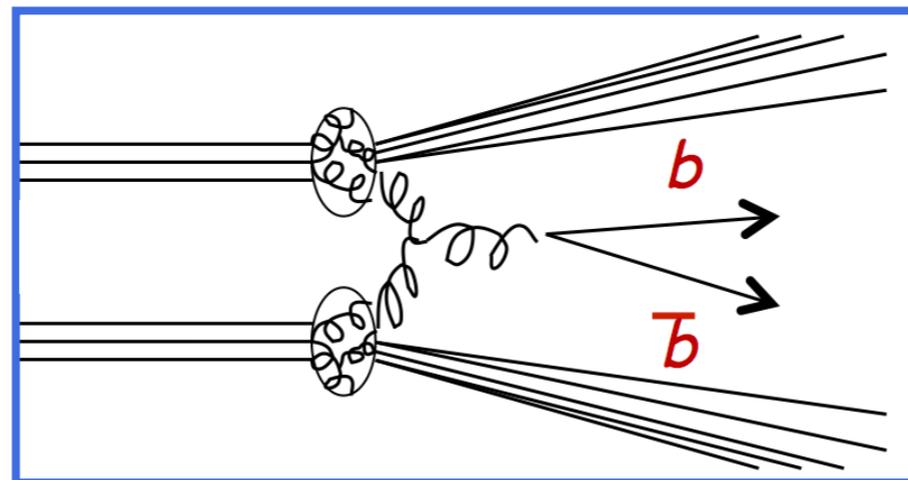


$$\langle nPVs \rangle \sim 2.0$$

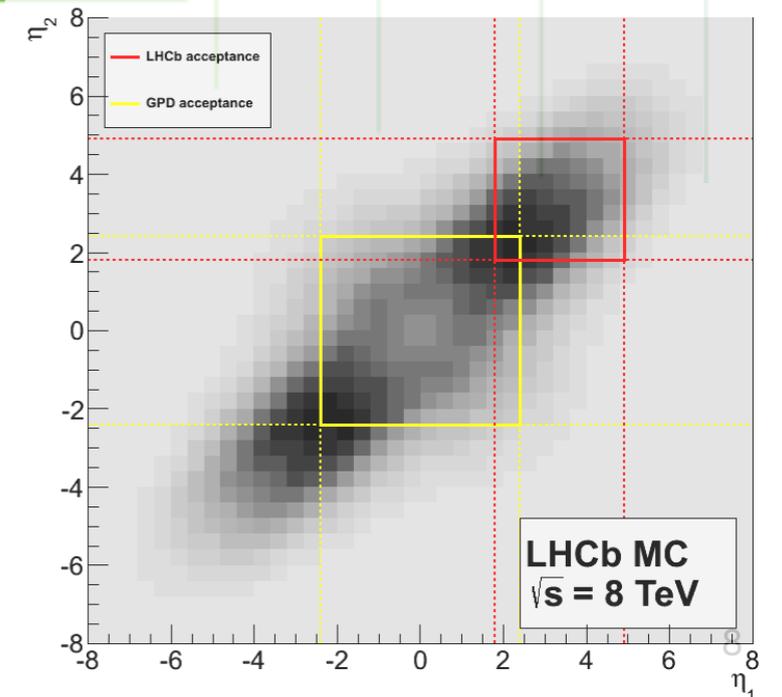
$$\langle nTracks \rangle \sim 200$$

$$\sigma(p\bar{p} \rightarrow b\bar{b}X) \sim 80\mu b$$

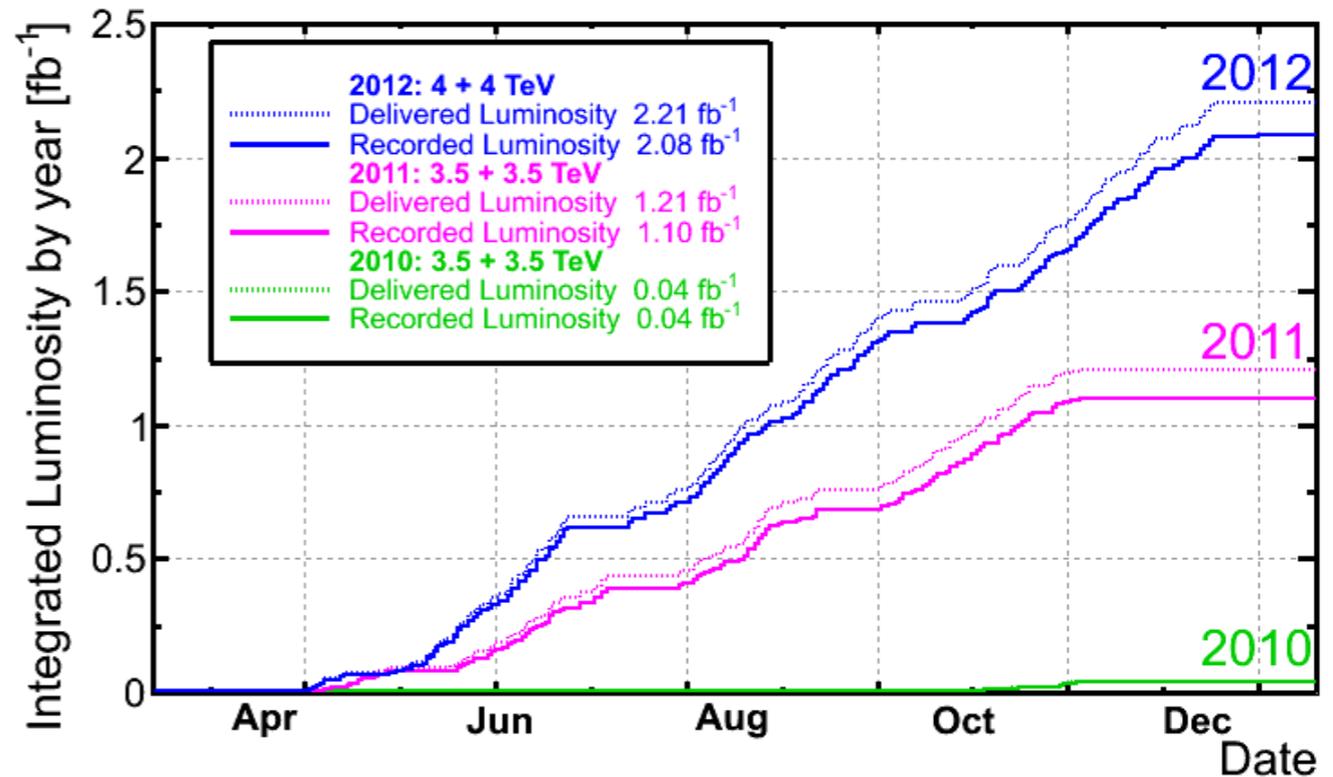
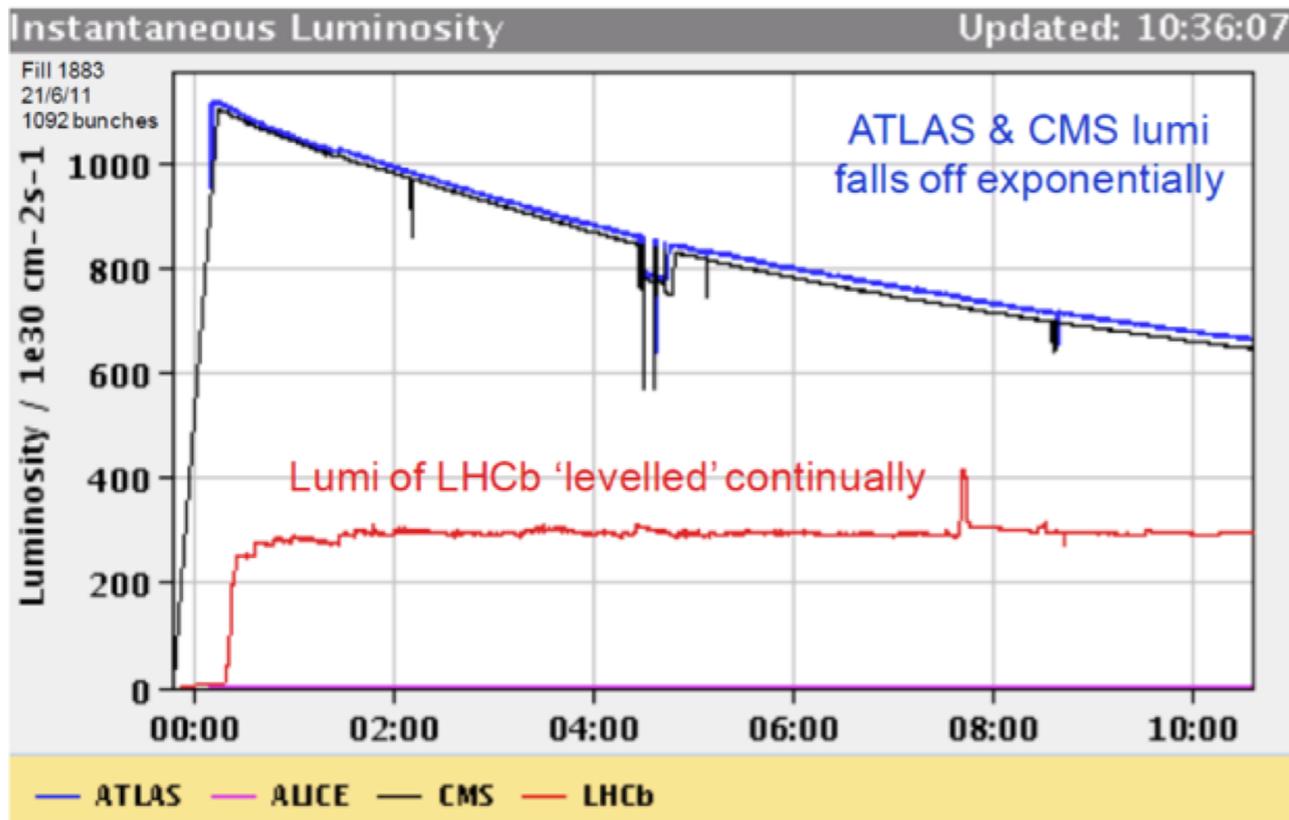
$$\sigma(c\bar{c}) \sim 1500\mu b$$



B hadrons fly ~1cm in the detector



Luminosity



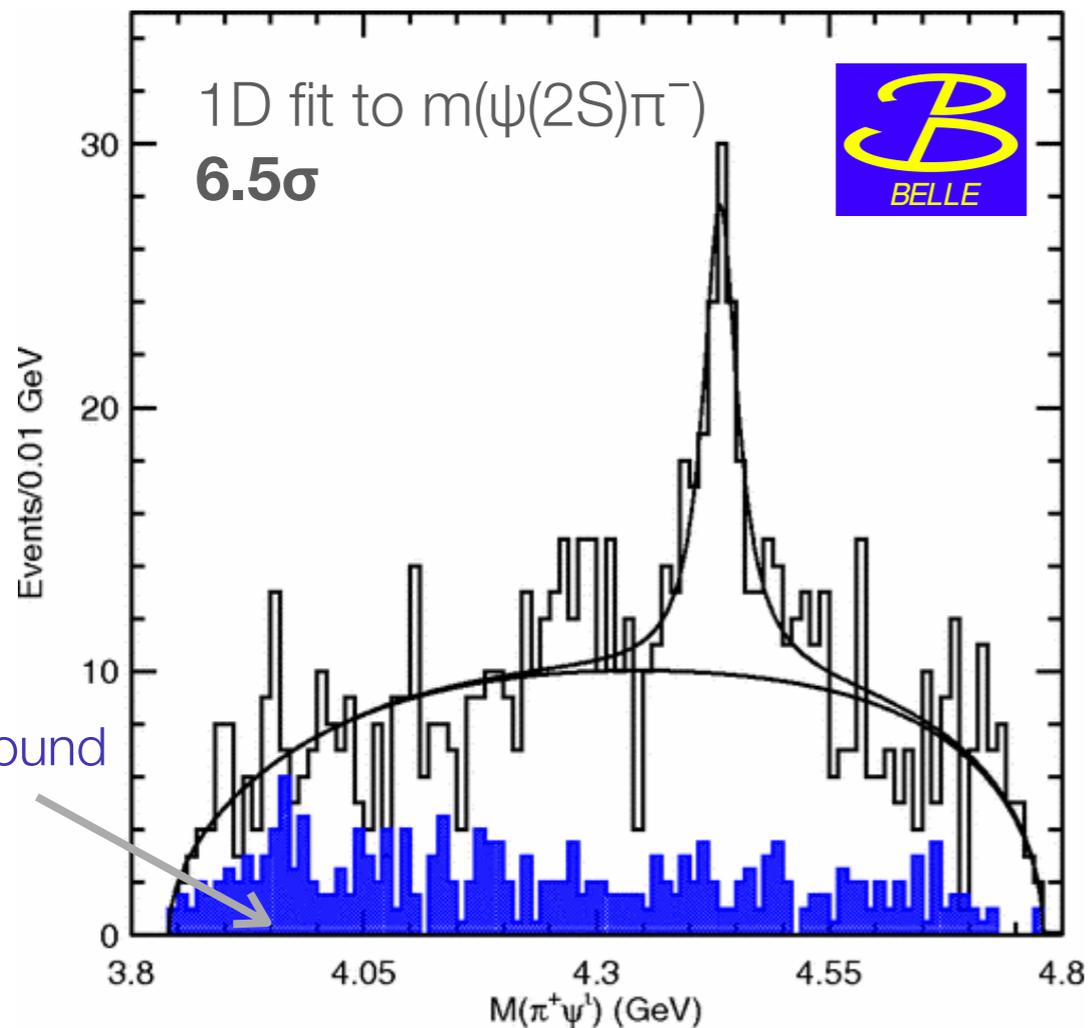
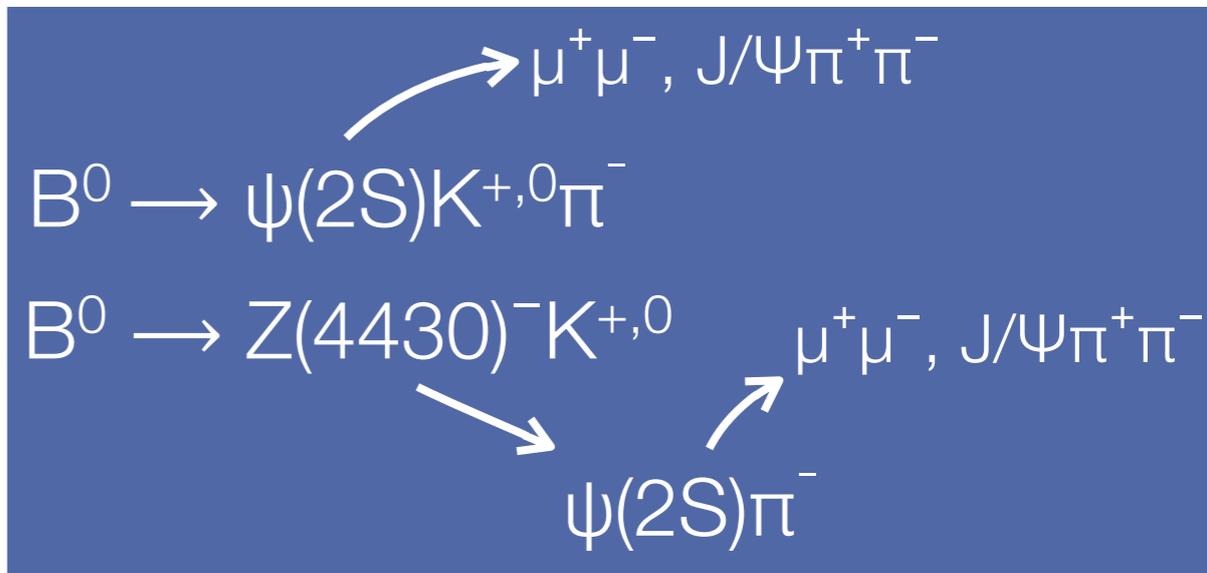
- LHCb designed to run at lower luminosity than ATLAS/CMS.
 - LHCb tracking is sensitive to pile-up.
- LHC pp beams are displaced to reduce instantaneous luminosity.
 - Stable running conditions.

$$\langle L \rangle_{2011} = 2.7 \times 10^{32} \text{ Hz/cm}^2$$

$$\langle L \rangle_{2012} = 4.0 \times 10^{32} \text{ Hz/cm}^2$$

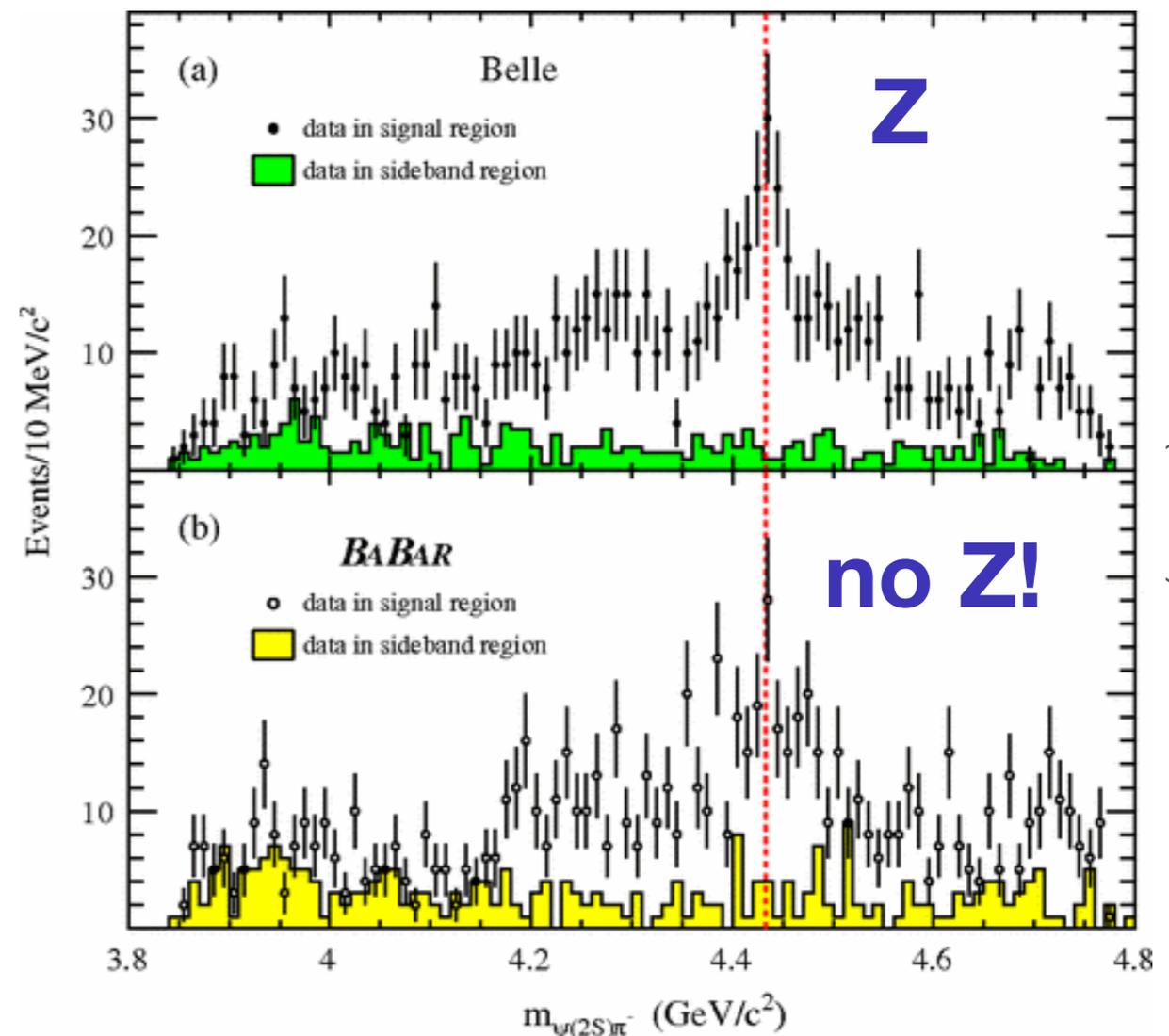
History of the $Z(4430)^-$

- Belle observed $Z(4430)^-$ from sample of $\sim 2k B^0 \rightarrow \psi(2S)K^{+,0}\pi^-$
- Charged state \Rightarrow minimal quark content of **$c\bar{c}u\bar{d}$**



$$M = 4433 \pm 4 \pm 2 \text{ MeV}/c^2$$

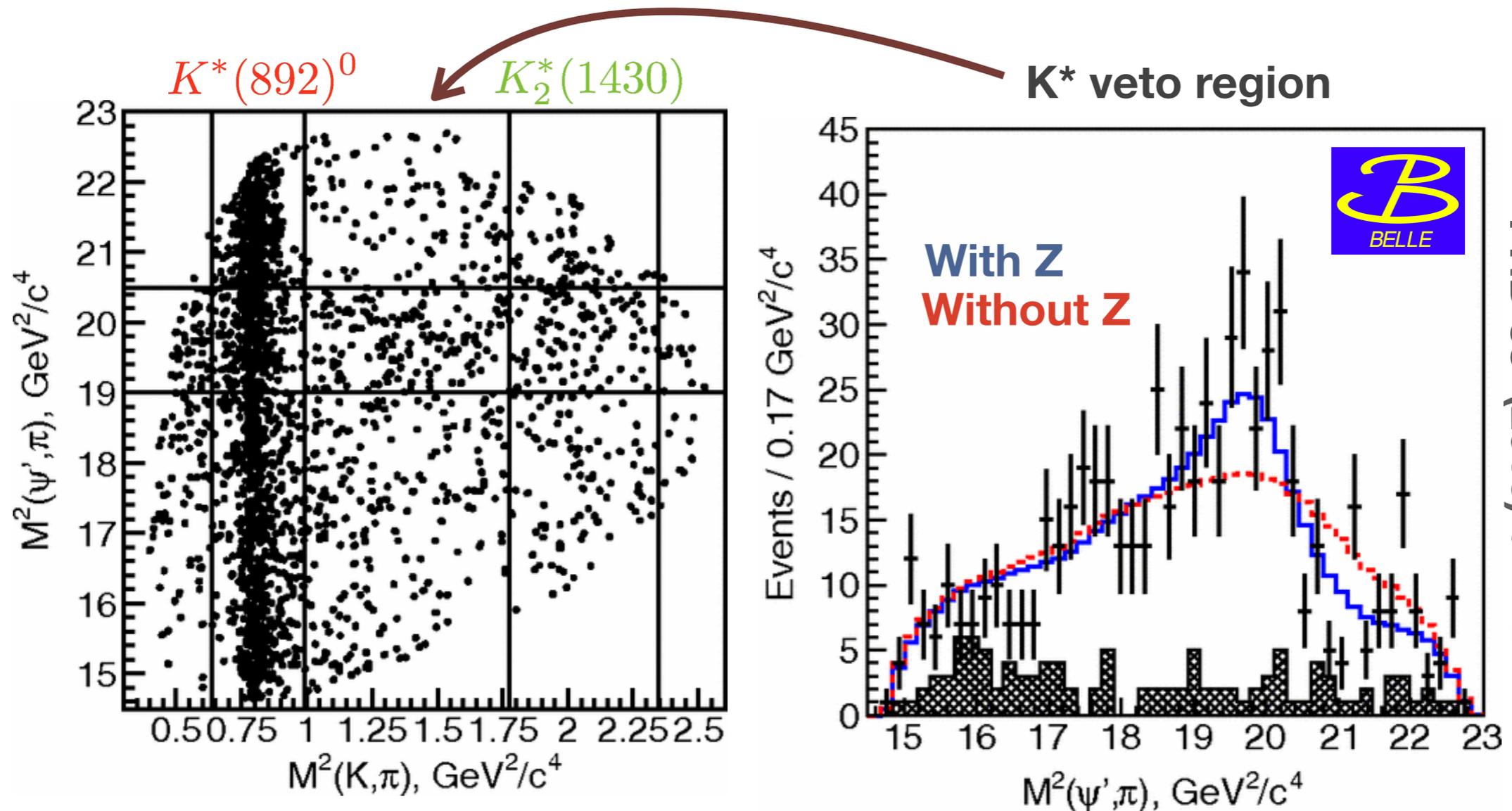
$$\Gamma = 45_{-13}^{+18+30} \text{ MeV}/c^2$$



Not observed by BaBar!

History of the $Z(4430)^-$

- Belle **PRL 100 (2008) 142001** 1D fit to $m(\psi(2S)\pi^-)$ **6.5 σ**
- BaBar **PRD 79 (2009) 112001** **Not observed!**
- Belle **PRD 80 (2009) 031104** 2D Dalitz fit to $m(\psi(2S)\pi^-)$ vs $m(K^+\pi^-)$ **6.4 σ**
- Belle **PRD 88 (2013) 074026** 4D Dalitz fit **6.4 σ**

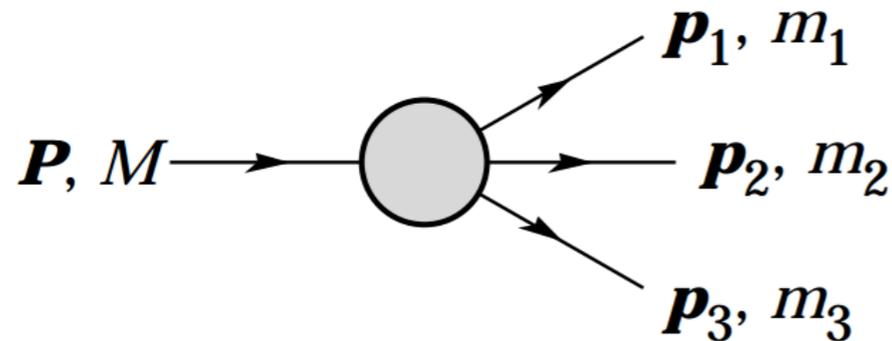


$$M = 4485_{-22-11}^{+22+28} \text{ MeV}/c^2$$

$$\Gamma = 200_{-46-35}^{+41+26} \text{ MeV}/c^2$$

PRD 88 (2013) 074026

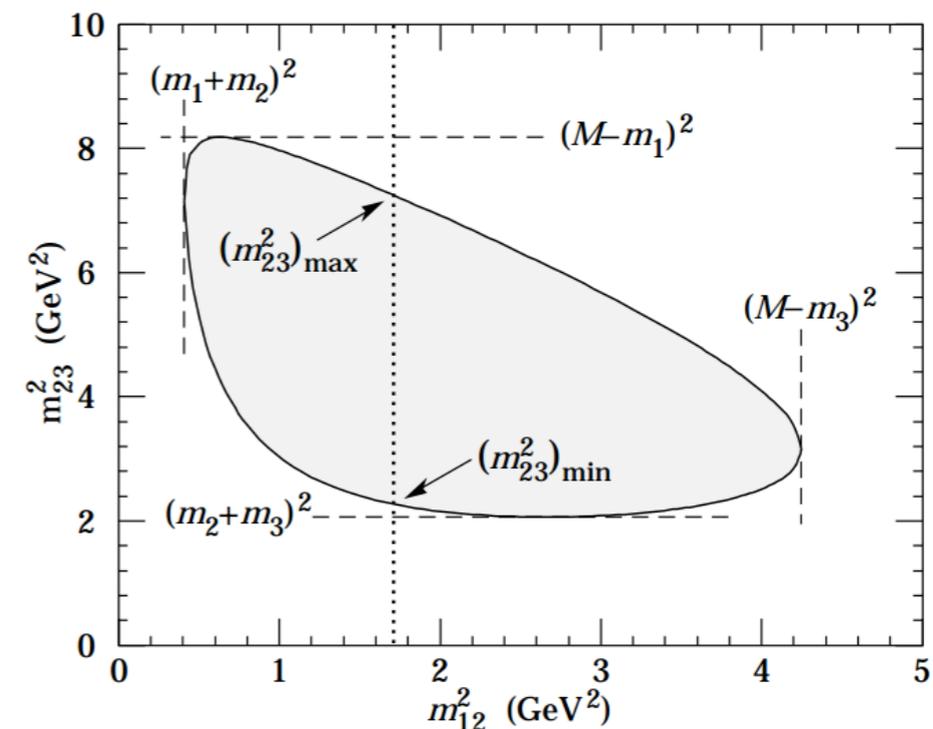
Reminder about Dalitz plots - 3 body decay



$$d\Gamma = \frac{1}{(2\pi)^3} \frac{1}{32M^3} |\overline{\mathcal{M}}|^2 dm_{12}^2 dm_{23}^2$$

Constraints	Degrees of freedom
3 four-vectors	+12
All decay in same plane (p)	-3
E	-3
Energy + momentum conservation	-3
Rotate system in plane	-1
Total	+2

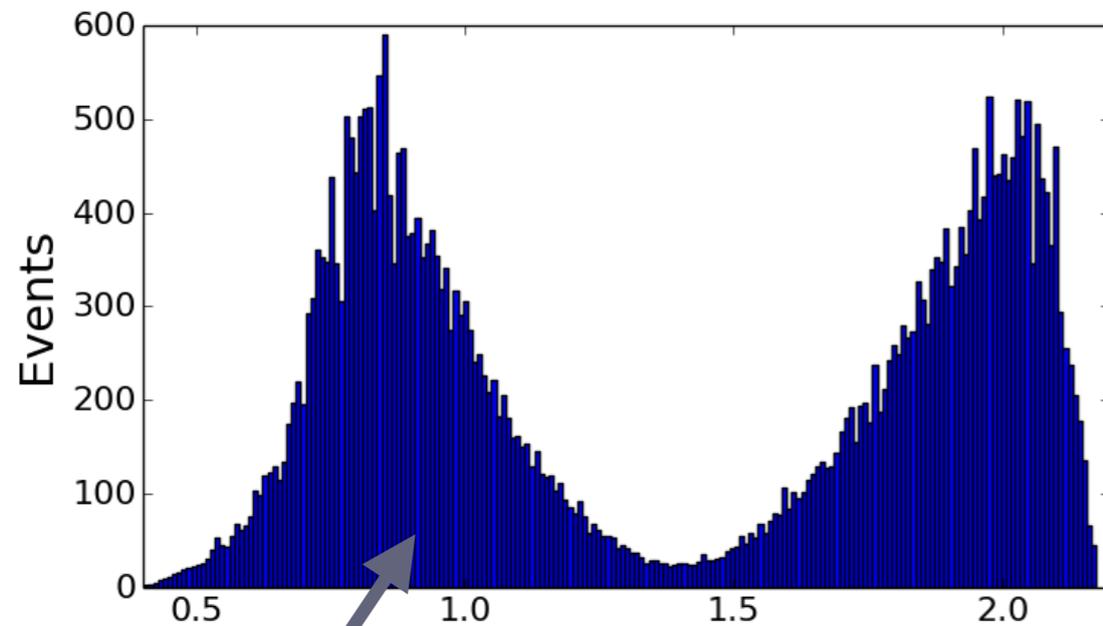
- Configuration of decay depends on ang. mom. of decay products.
- All dynamical information contained in $|\overline{\mathcal{M}}|^2$.
- Density plot of m_{12}^2 vs. m_{23}^2 to infer information on $|\overline{\mathcal{M}}|^2$.



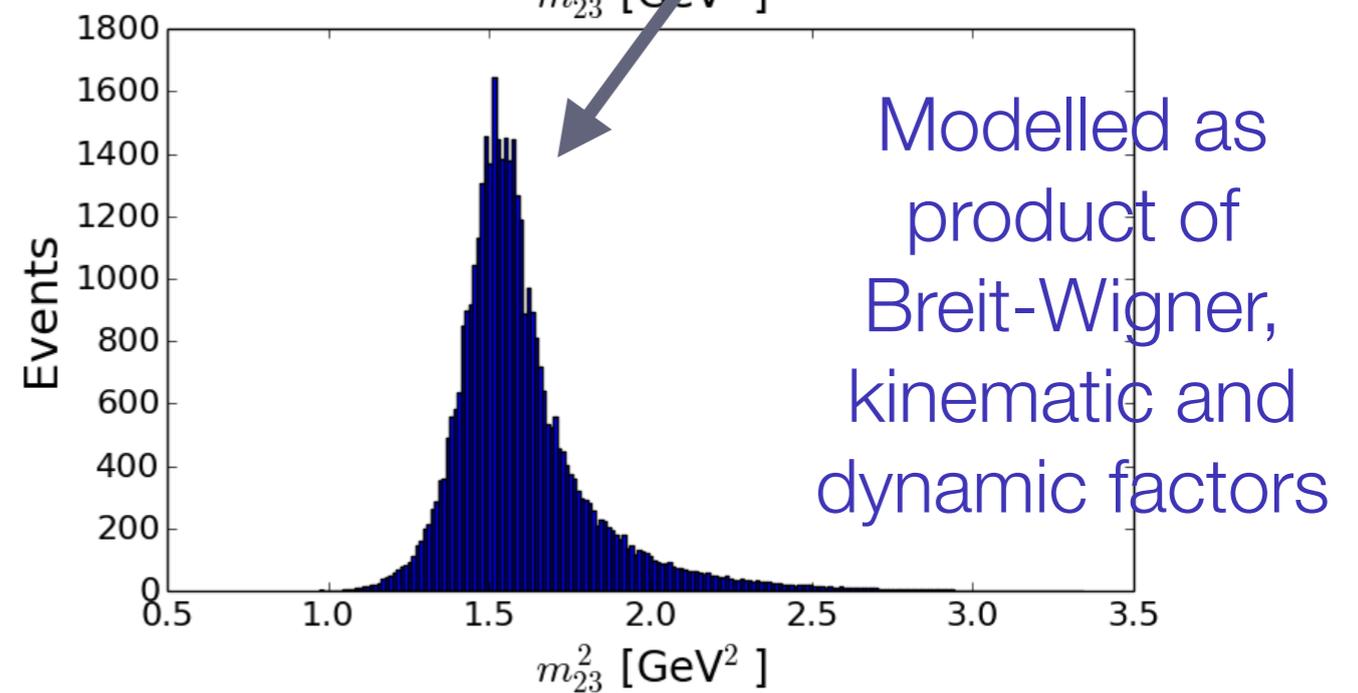
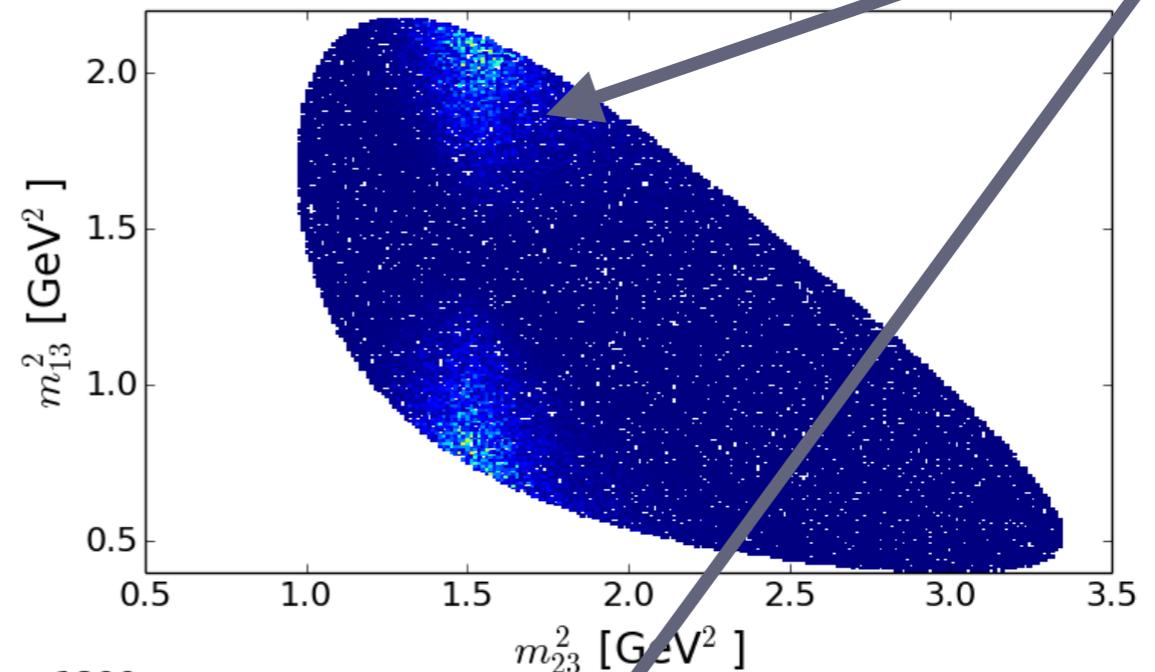
Reminder about Dalitz plots

$$d\Gamma = \frac{1}{(2\pi)^3} \frac{1}{32M^3} |\overline{\mathcal{M}}|^2 dm_{12}^2 dm_{23}^2$$

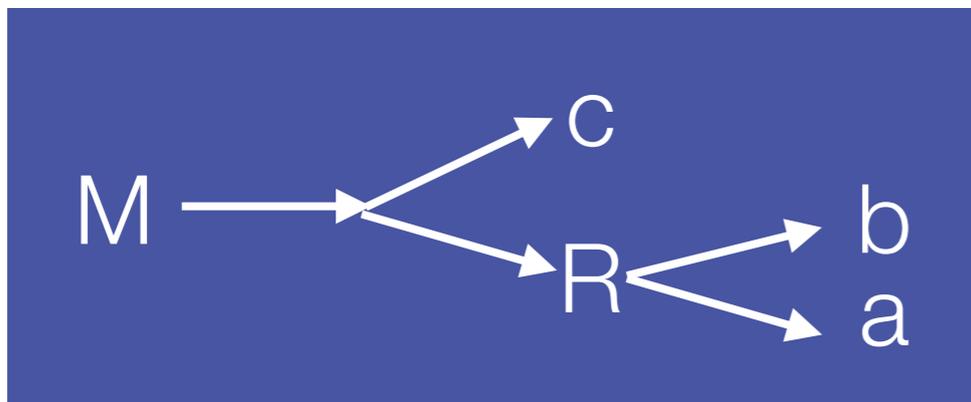
Spin-1 resonance



Peaks in distribution
do not correspond to a
real resonance - just a reflection



Modelled as
product of
Breit-Wigner,
kinematic and
dynamic factors



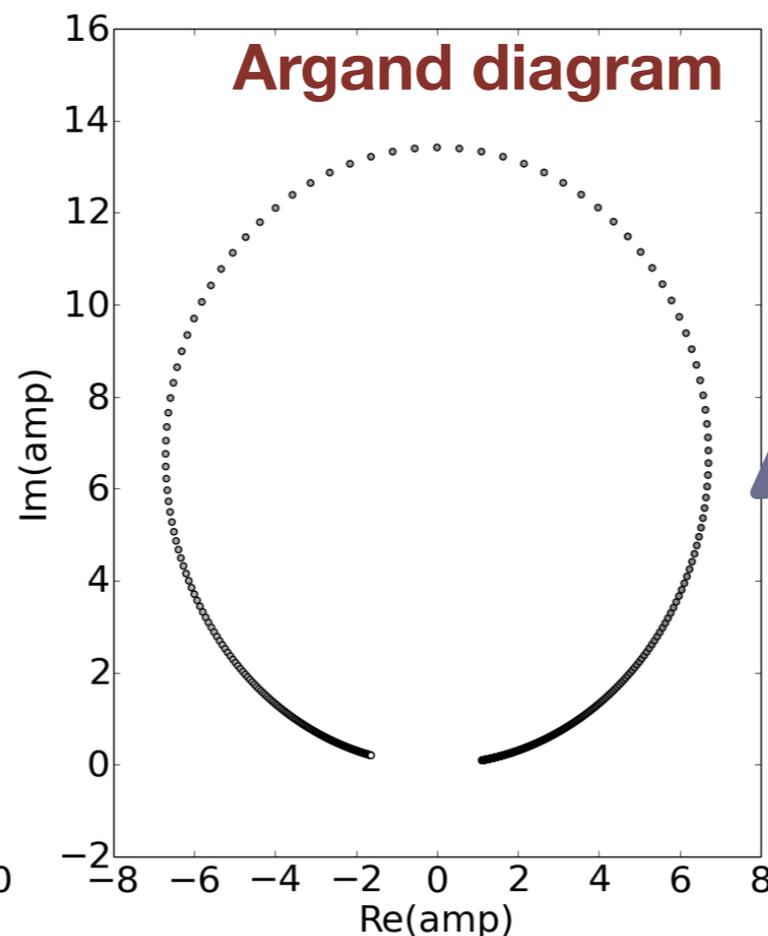
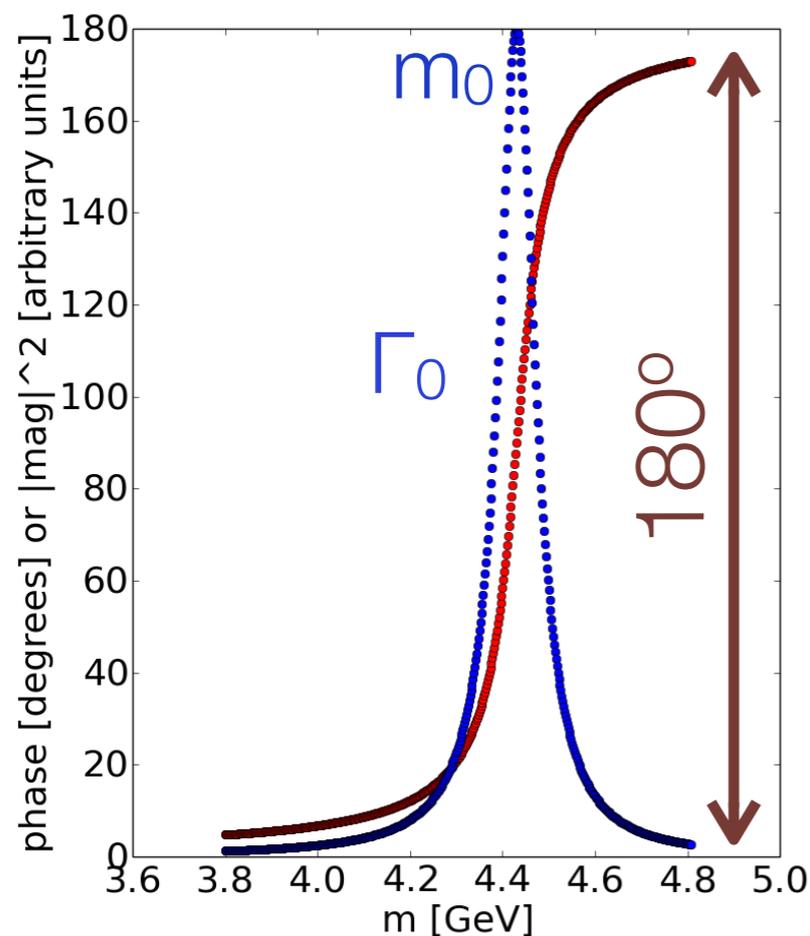
Breit-Wigner amplitude

R → ab

- Often model resonances with mass (m_0), width (Γ_0) using a relativistic Breit-Wigner function.
- q is daughter particle momentum in rest frame of resonance.
- B_L are Blatt-Weisskopf functions for the orbital angular momentum (L) barrier factors.
- Amplitude = $|BW|^2$

$$BW(m|m_0, \Gamma_0) = \frac{1}{m_0^2 - m^2 - im_0\Gamma(m)}$$

$$\Gamma(m) = \Gamma_0 \left(\frac{q}{q_0} \right)^{2L_{K^*}+1} \frac{m_0}{m} B'_{L_{K^*}}(q, q_0, d)^2$$

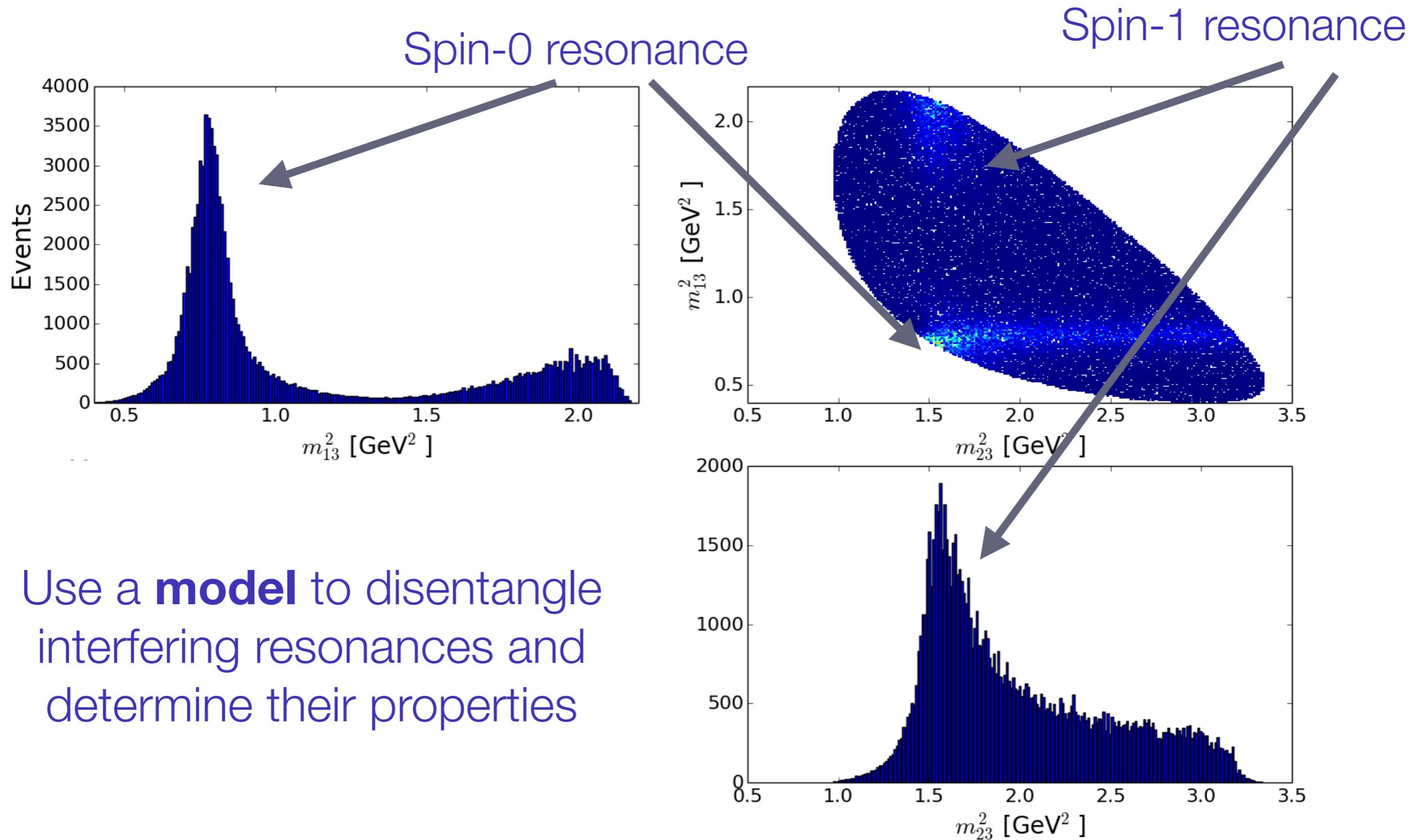


Circular trajectory in complex plane is characteristic of resonance

Phase change of 180° across the pole

Reminder about Dalitz plots

$$d\Gamma = \frac{1}{(2\pi)^3} \frac{1}{32M^3} |\overline{\mathcal{M}}|^2 dm_{12}^2 dm_{23}^2$$

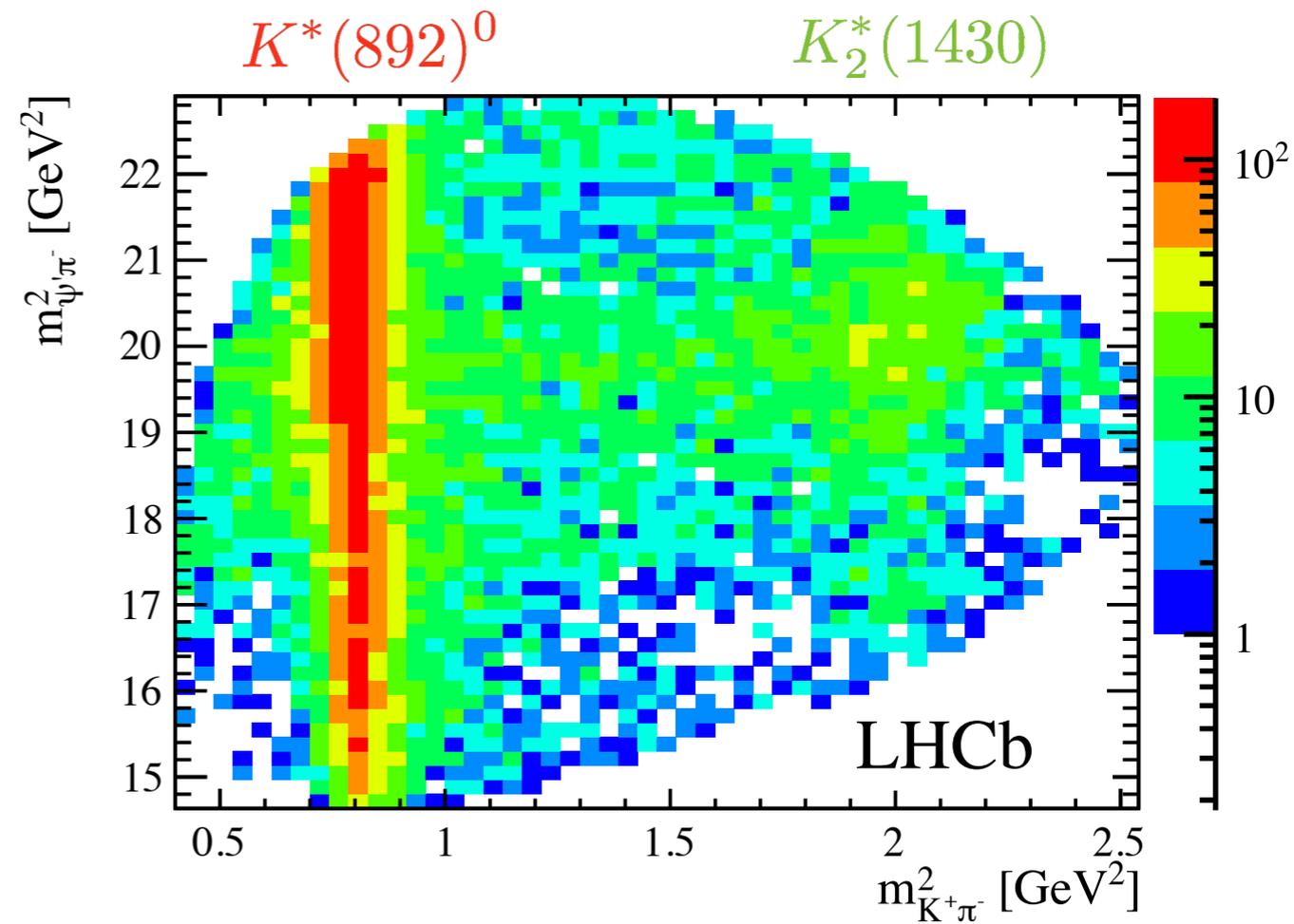
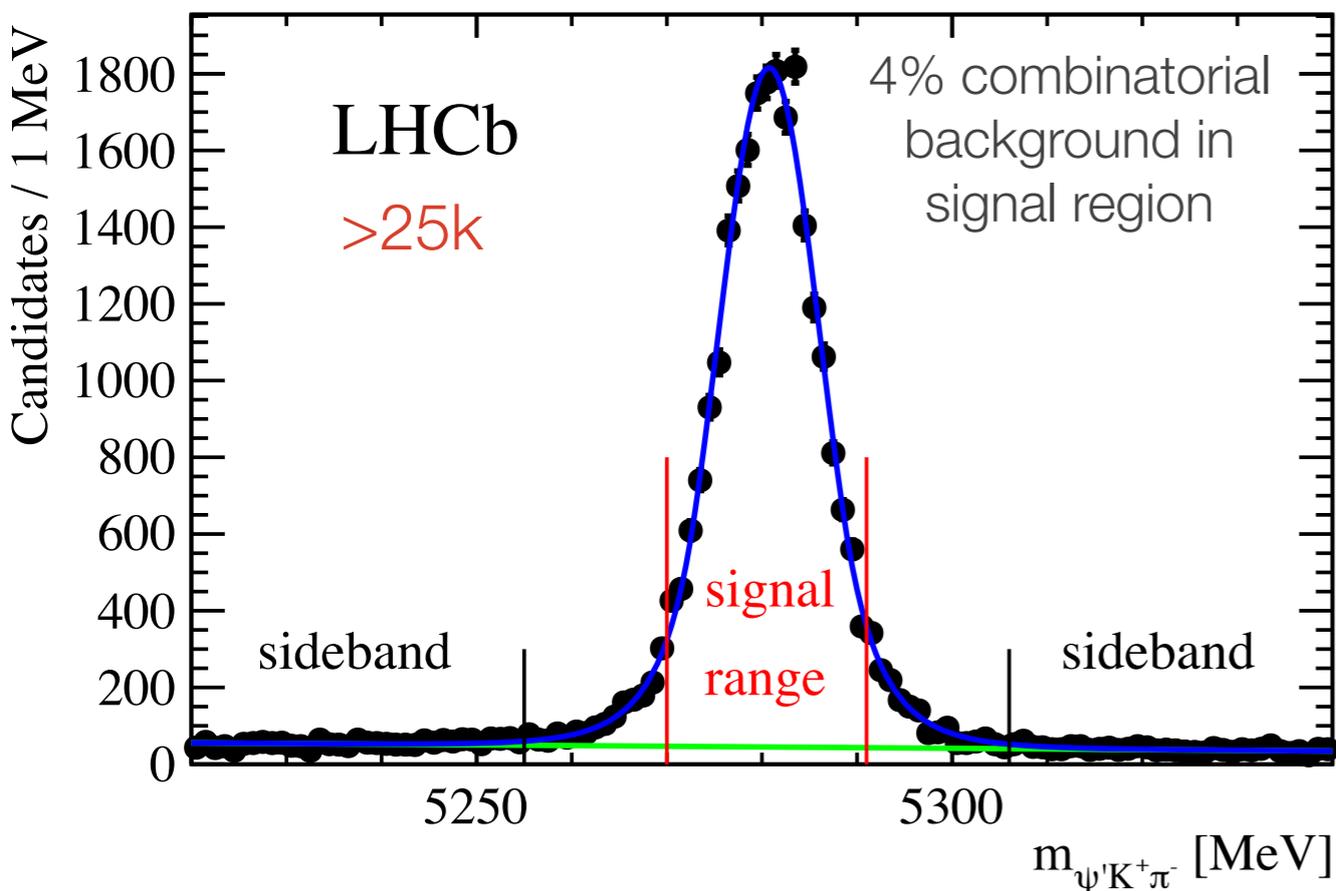


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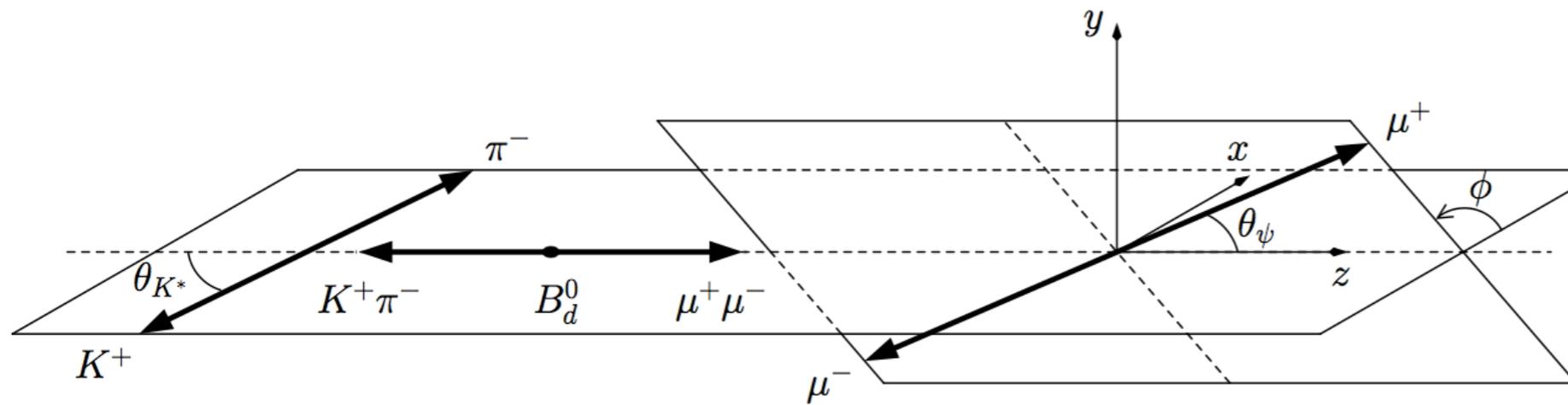
- LHCb has sample of $>25k$ $B^0 \rightarrow \psi(2S)K^+\pi^-$ candidates.
 - Factor 10 more than Belle/BaBar.
- Selection: most events come through dimuon trigger (eff \sim 90%)
- Typical B pT \sim 6GeV, μ pT \sim 2GeV, K pT \sim 1GeV
- Use sidebands to build 4D model of combinatorial background.
 - Backgrounds from mis-ID physics decays is small - excellent LHCb PID!

$$\psi(2S) \rightarrow \mu^+ \mu^-$$



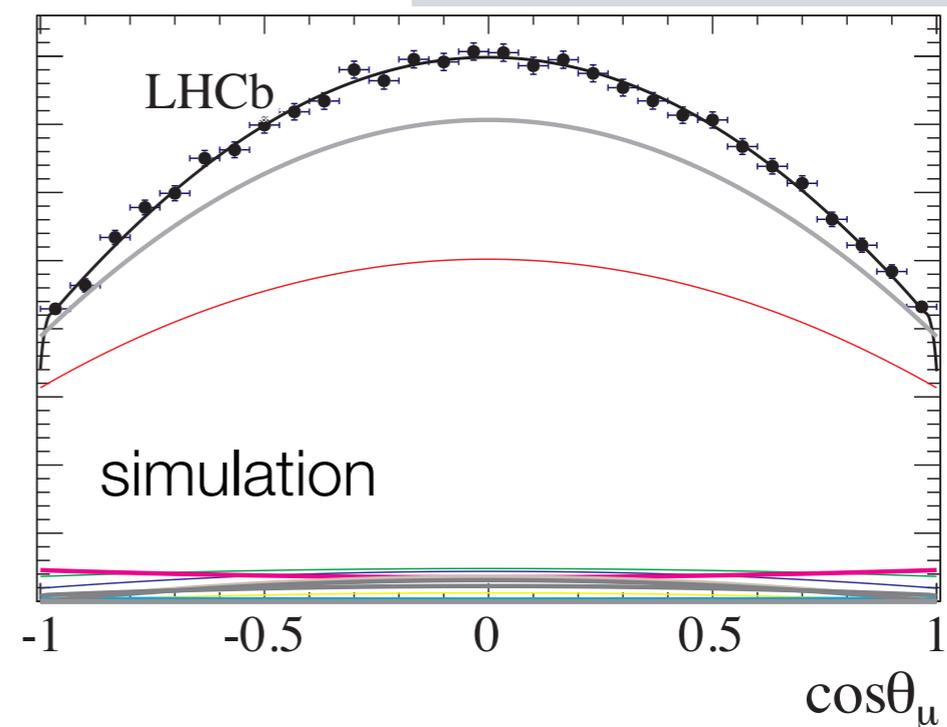
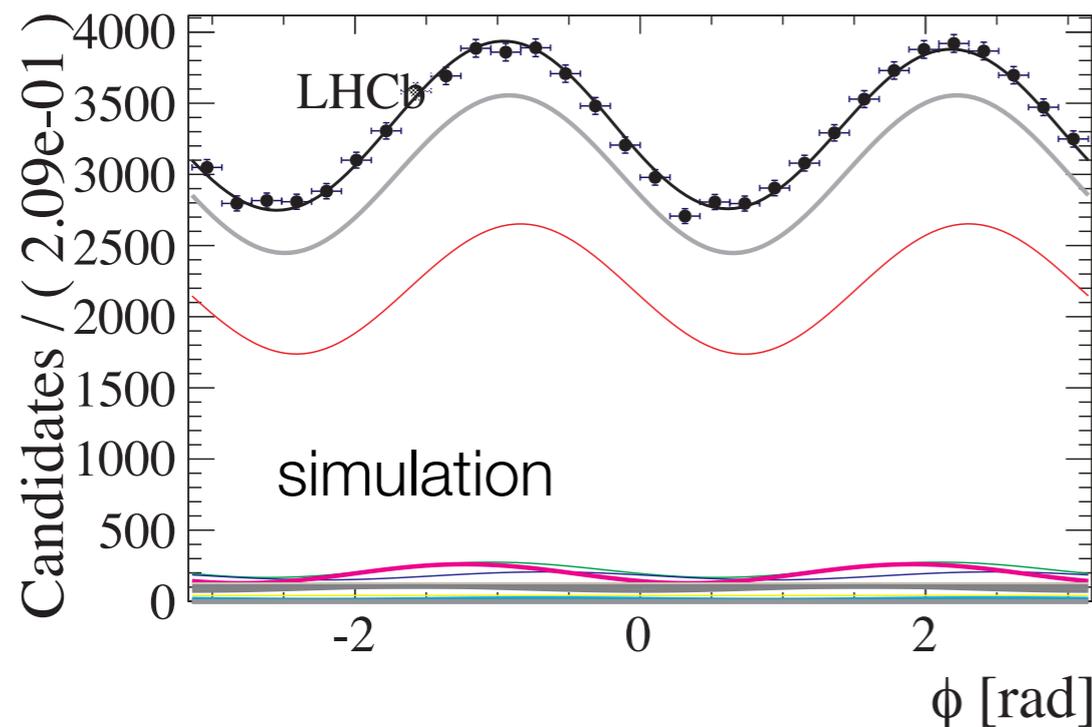
Only 2 of the 4 dimensions...

4D Dalitz plot (scalar \rightarrow vector scalar scalar)



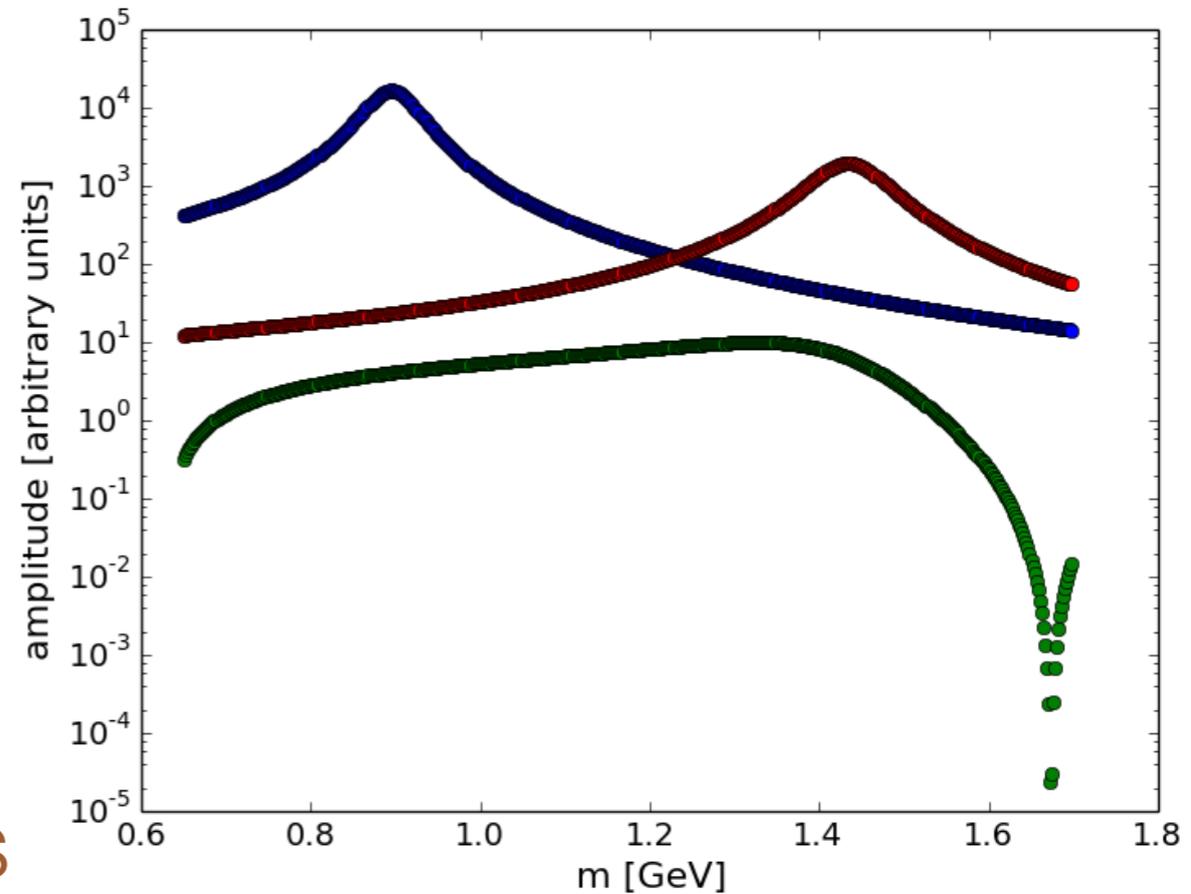
- $B^0 \rightarrow \psi(2S) K^+ \pi^-$, $\psi(2S) \rightarrow \mu^+ \mu^-$
- Need to use the angular information, in addition to $m(\psi(2S)\pi^-)^2$ vs $m(K^+\pi^-)^2$, to understand $|\mathcal{M}|^2$.

Constraints	Degrees of freedom
3 four-vectors	+12
All decay in same plane (p)	-3
E	-3
Energy + momentum conservation	-3
Rotate system in plane	-1
Vector helicity	+2
Total	+4



Amplitude model

- Use the Isobar approach, build amplitude from sum of overlapping and interfering Breit-Wigner resonances.



Sum over the k resonances

$$|\mathcal{M}|^2 = \sum_{\Delta\lambda_\mu = -1,1} \left| \sum_{\lambda_\psi = -1,0,1} \sum_k A_{k,\lambda_\psi}(m_{K\pi}, \Omega | m_{0k}, \Gamma_{0k}) \right|^2$$

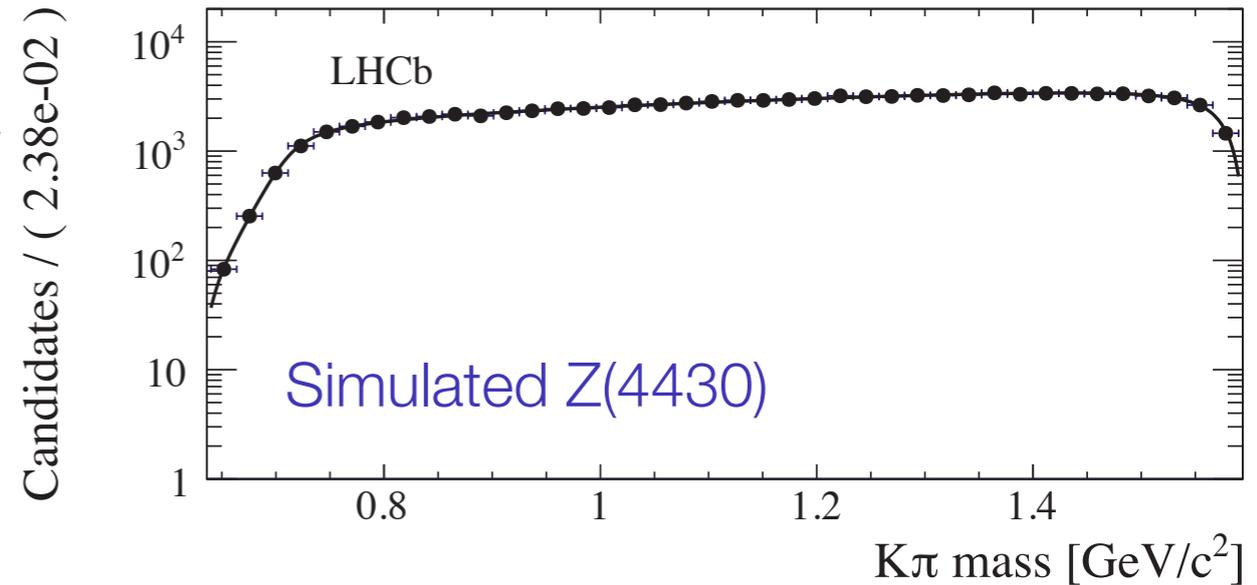
In 4D fit, $\mu^+\mu^-$ are final state particles: thus different dimuon helicity amplitudes are incoherent (cannot interfere)

Now different ψ helicity amplitudes interfere

Complex amplitude that encodes the mass and angular dependence

Amplitude model - adding in the Z(4430)

- Adding the Z(4430) component is a bit more difficult since it has different helicity frame compared to $K^+\pi^-$ resonances.
- It has a BW shape in $m_{\psi(2S)\pi^-}$ mass, but is basically flat in $m_{K^+\pi^-}$.
- Low Q-value in decay, so ignore D-wave contribution $\Rightarrow A_{Z,-1} = A_{Z,0} = A_{Z,+1}$



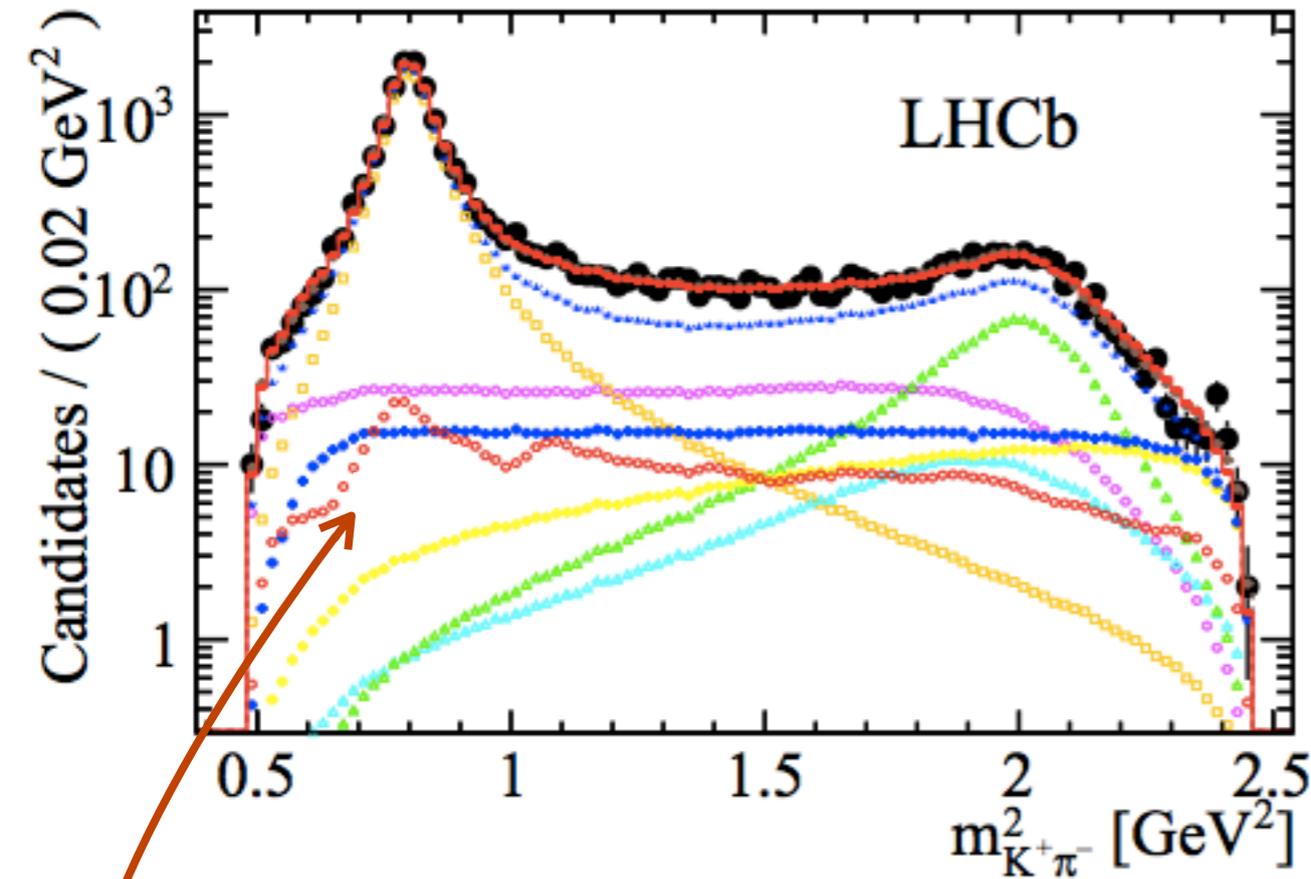
$$|\mathcal{M}|^2 = \sum_{\Delta\lambda_\mu = -1,1} \left| \sum_{\lambda_\psi = -1,0,1} \sum_k A_{k,\lambda_\psi}(m_{K\pi}, \Omega | m_{0k}, \Gamma_{0k}) \right. \\ \left. + \sum_{\lambda_\psi^Z = -1,0,1} A_{Z,\lambda_\psi^Z}(m_{\psi\pi}, \Omega^Z | m_{0Z}, \Gamma_{0Z}) e^{i\Delta\lambda_\mu \alpha} \right|^2$$

Z(4430) component interferes with the $K^+\pi^-$ sector

Rotation by α to different helicity frame

Which resonances should we add?

From PDG



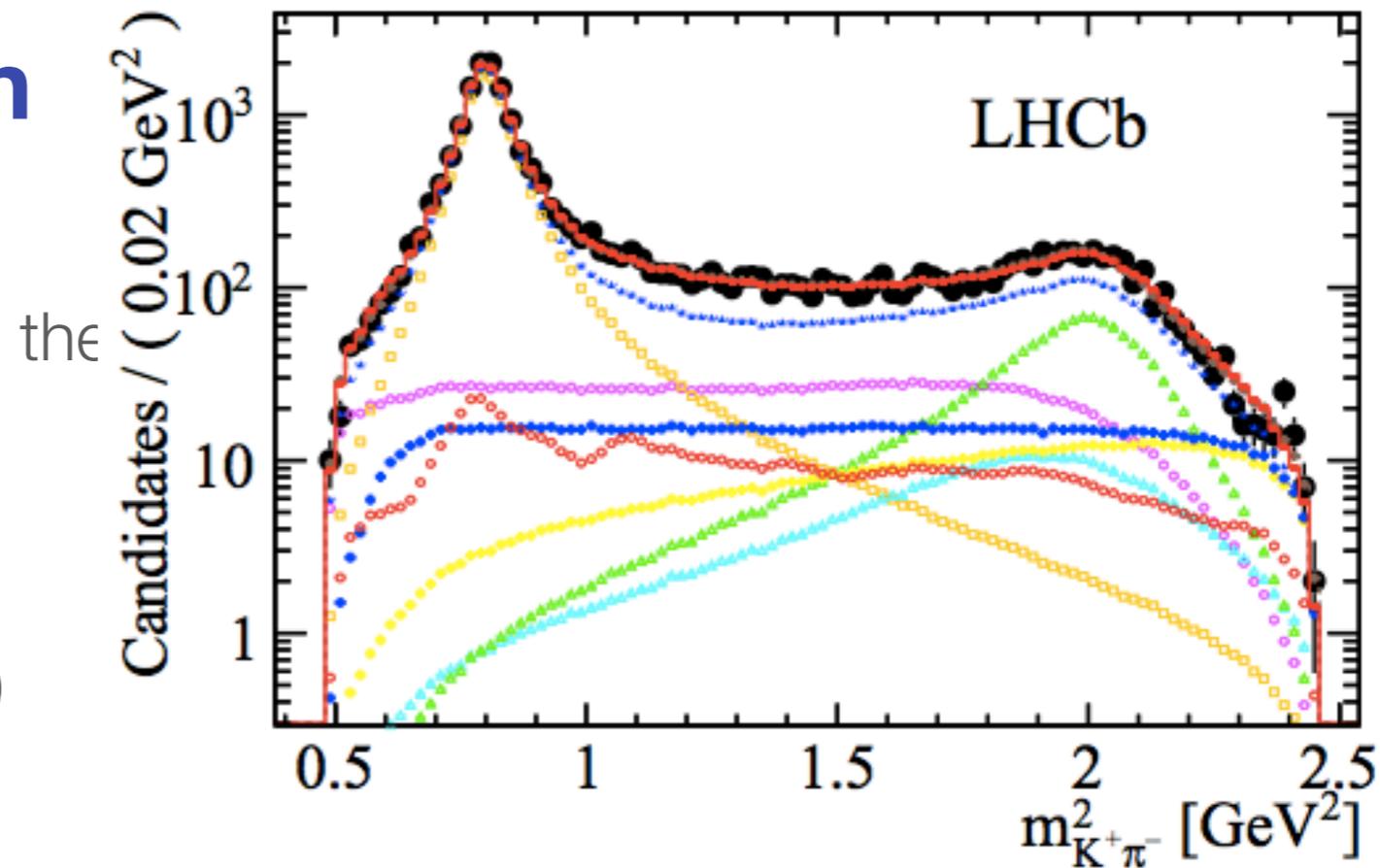
Resonance	J^P	Likely $n^{2S+1}L_J$	Mass (MeV)	Width (MeV)
$K_0^*(800)^0$ (κ)	0^+	—	682 ± 29	547 ± 24
$K^*(892)^0$	1^-	1^3S_1	895.94 ± 0.26	48.7 ± 0.7
$K_0^*(1430)^0$	0^+	1^3P_0	1425 ± 50	270 ± 80
$K_1^*(1410)^0$	1^-	2^3S_1	1414 ± 15	232 ± 21
$K_2^*(1430)^0$	2^+	1^3P_2	1432.4 ± 1.3	109 ± 5
$B^0 \rightarrow \psi(2S)K^+\pi^-$ phase space limit			1593	
$K_1^*(1680)^0$	1^-	1^3D_1	1717 ± 27	322 ± 110
$K_3^*(1780)^0$	3^-	1^3D_3	1776 ± 7	159 ± 21
$K_0^*(1950)^0$	0^+	2^3P_0	1945 ± 22	201 ± 78
$K_4^*(2045)^0$	4^+	1^3F_4	2045 ± 9	198 ± 30
$B^0 \rightarrow J/\psi K^+\pi^-$ phase space limit			2183	
$K_5^*(2380)^0$	5^-	1^3G_5	2382 ± 9	178 ± 32

- $K^+\pi^-$ spectrum contains many overlapping resonances.
 - Each resonance has a complex amplitude for **each** helicity component, this impacts the $m_{\psi(2S)\pi^-}$ distribution.
 - Measure all amplitudes relative to $K^*(892)$ helicity-0 component.
- Nominal result includes all resonances up to $K_1^*(1680)$.
- Main source of **systematic uncertainties** comes from varying model to include higher $K^+\pi^-$ spin-states.

Background from sidebands of B mass

S-wave parameterisation

- Z(4430) has largest effect $\sim 1.5\text{GeV}$
- Important to understand **K π S-wave** in this region
- **Isobar model** is default
 - BW amplitude for $K^*(1430)+K_0(800)$
 - Non-resonant contribution
- LASS model as cross-check
 - Does not violate unitarity
 - Sum of elastic scattering, destructively interfering with $K^*(1430)$.

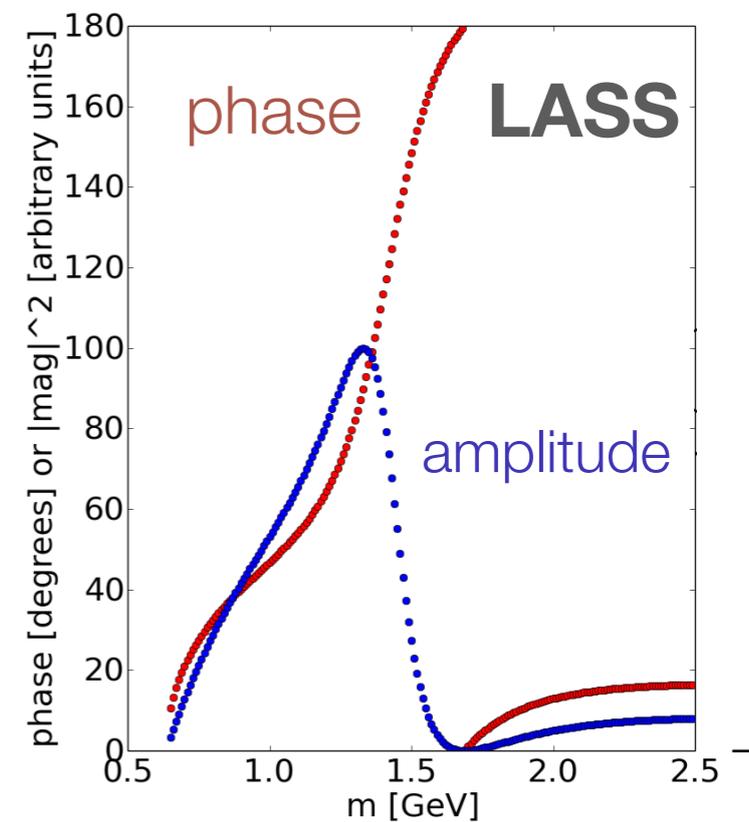


Slowly varying
NR contribution

$$\frac{1}{\cot \delta_B(m_{K\pi}) - i} + e^{2i\delta_B(m_{K\pi})} \frac{1}{\cot \delta_R(m_{K\pi}) - i}$$

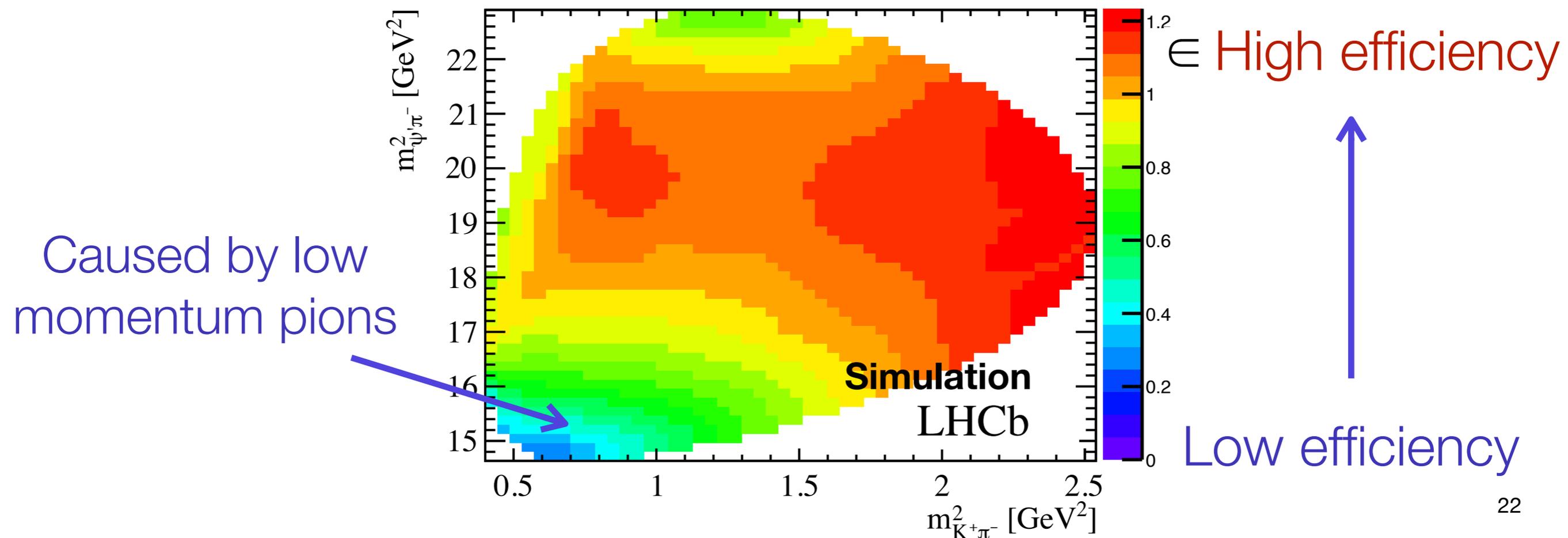
BW amplitude
for K(1430)

$$\cot \delta_B(m_{K\pi}) = \frac{1}{a q} + \frac{1}{2} r q \quad \cot \delta_R(m_{K\pi}) = \frac{m_0^2 - m_{K\pi}^2}{m_0 \Gamma(m_{K\pi})}$$



Reconstruction and selection efficiency

- Unfortunately, LHCb is not 100% efficient at reconstructing the decay particles in 4D space.
- Extract efficiency model from events simulated uniformly in phase space and passed through detector reconstruction.
- Also, remove events near edge of Dalitz boundary since efficiency not well modelled there.
- 2D representation...



Fitting the model to the data

- Likelihood fit to measure **~50** free parameters: amplitudes, phases, resonance mass/widths.

$$-\ln L(\vec{\omega}) = -\sum_i^{N_{\text{data}}} \ln P_{\text{tot}}^u(\vec{v}_i|\vec{\omega}) = -\sum_i^{N_{\text{data}}} \ln (|\mathcal{M}(\vec{v}_i|\vec{\omega})|^2 \epsilon(\vec{v}_i)/I(\vec{\omega}))$$

PDF (grey arrow pointing to P_{tot}^u)
 Observables (mass, angles) (blue arrow pointing to \vec{v}_i)
 Parameters (red arrow pointing to $\vec{\omega}$)
 Efficiency (green arrow pointing to $\epsilon(\vec{v}_i)$)

- In any amplitude fit, difficulty comes from **integrating** the matrix element.
- Solution: sum over fully simulated, reconstructed phase space MC.
 - This automatically includes the efficiency in the calculation.
 - Alternative approach that explicitly parameterises the 4D efficiency.

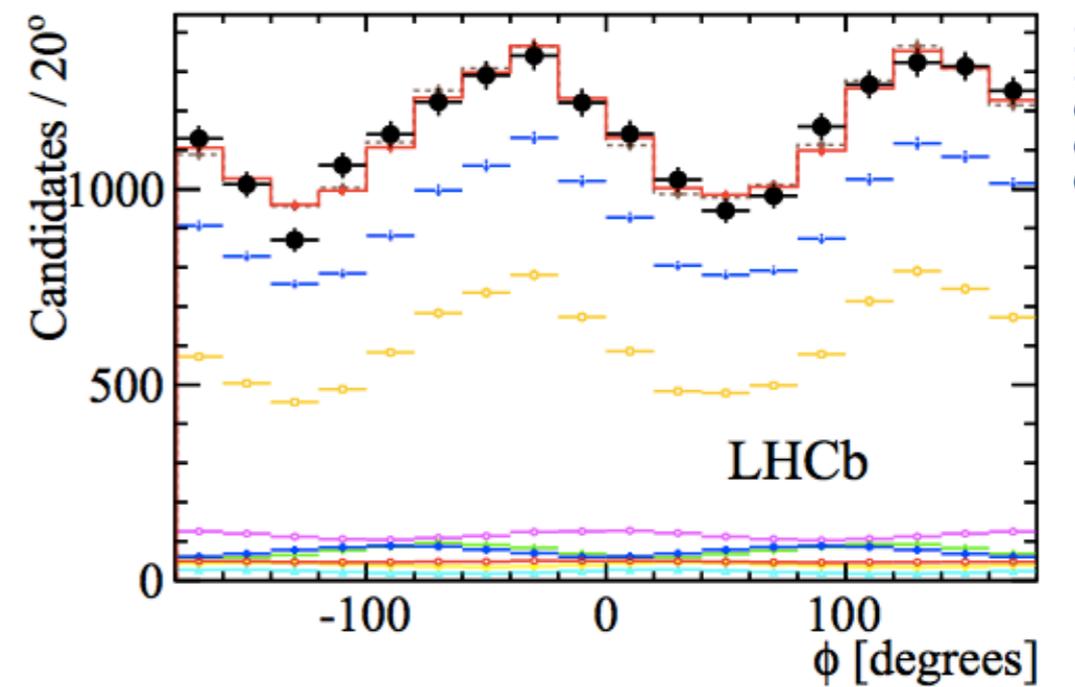
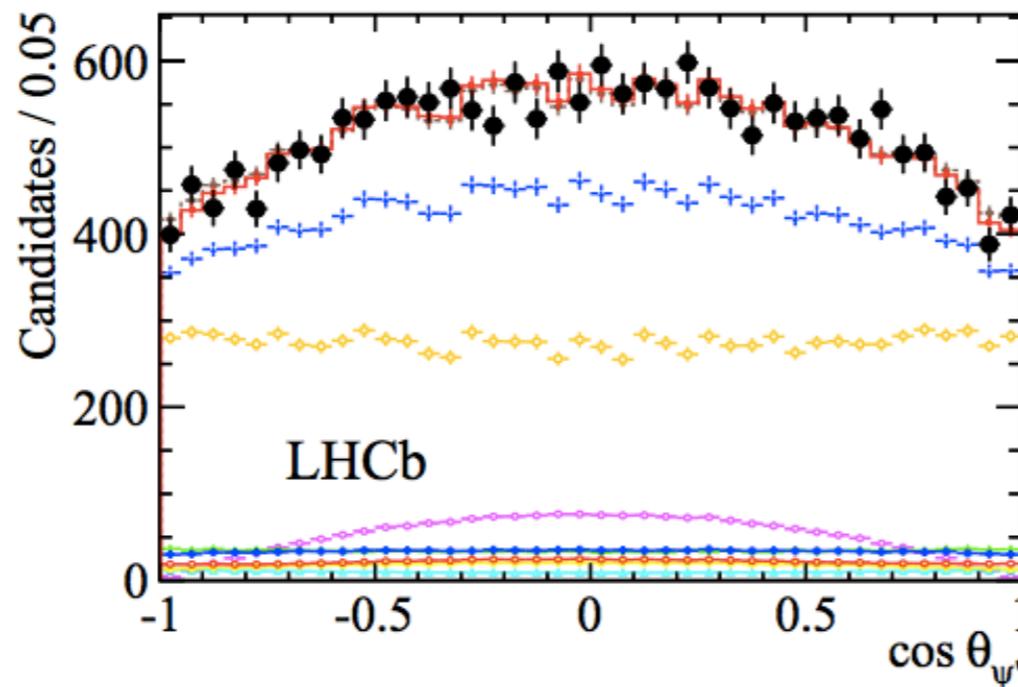
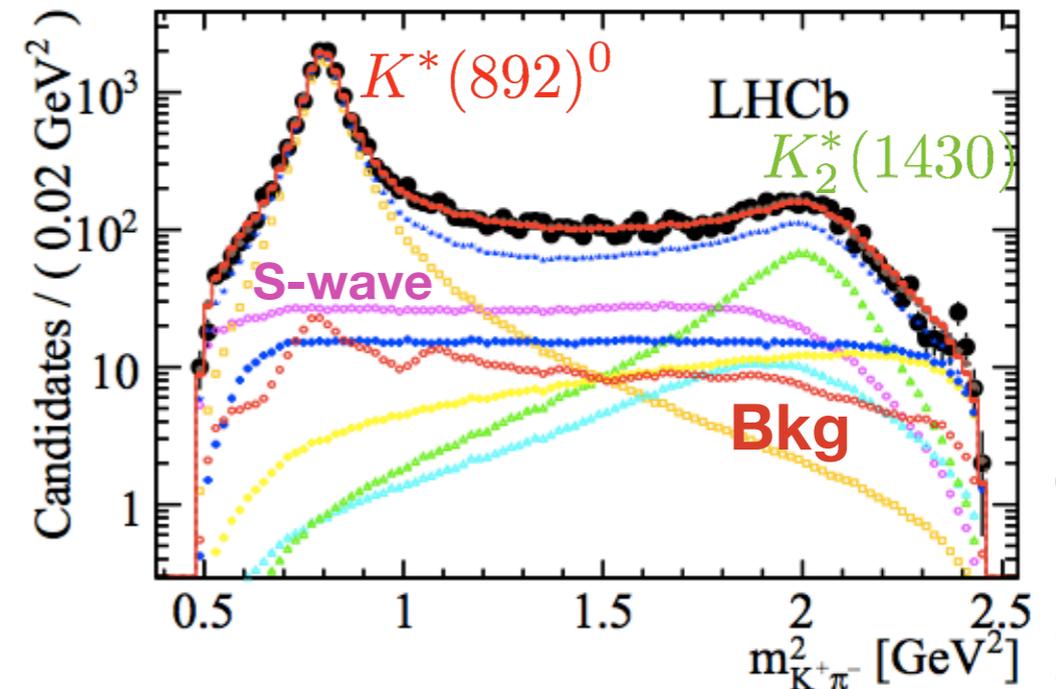
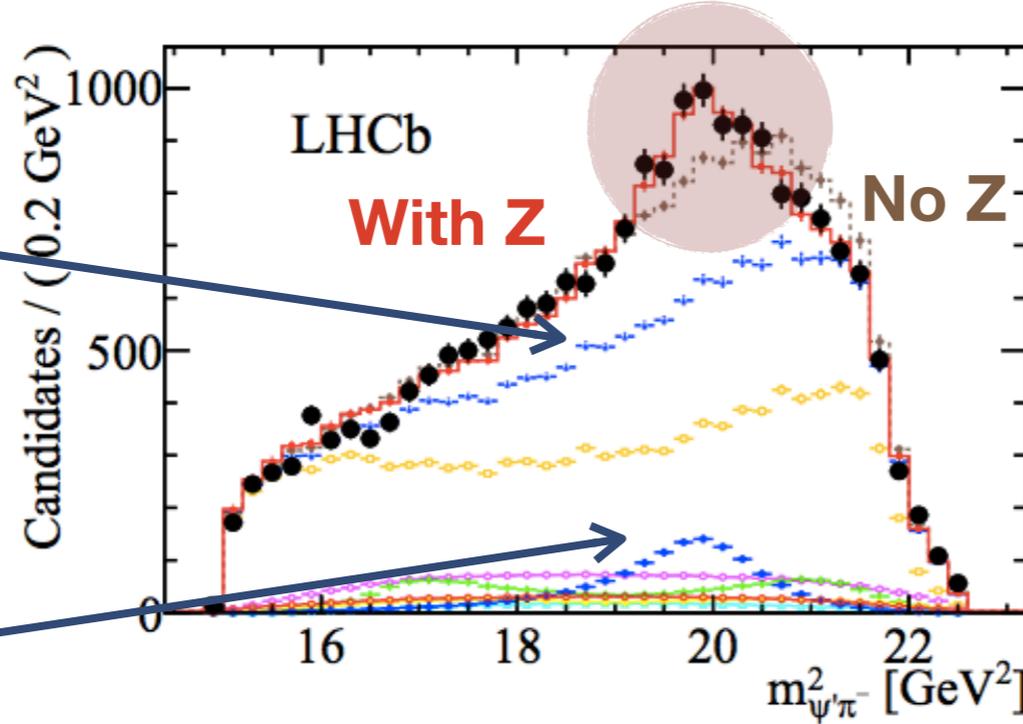
$$I(\vec{\omega}) = \sum_i^{N_{\text{MC}}} |\mathcal{M}(\vec{v}_i|\vec{\omega})|^2$$

Try different models for $K^+\pi^-$ and $Z(4430)$, compare values of \mathcal{L} .

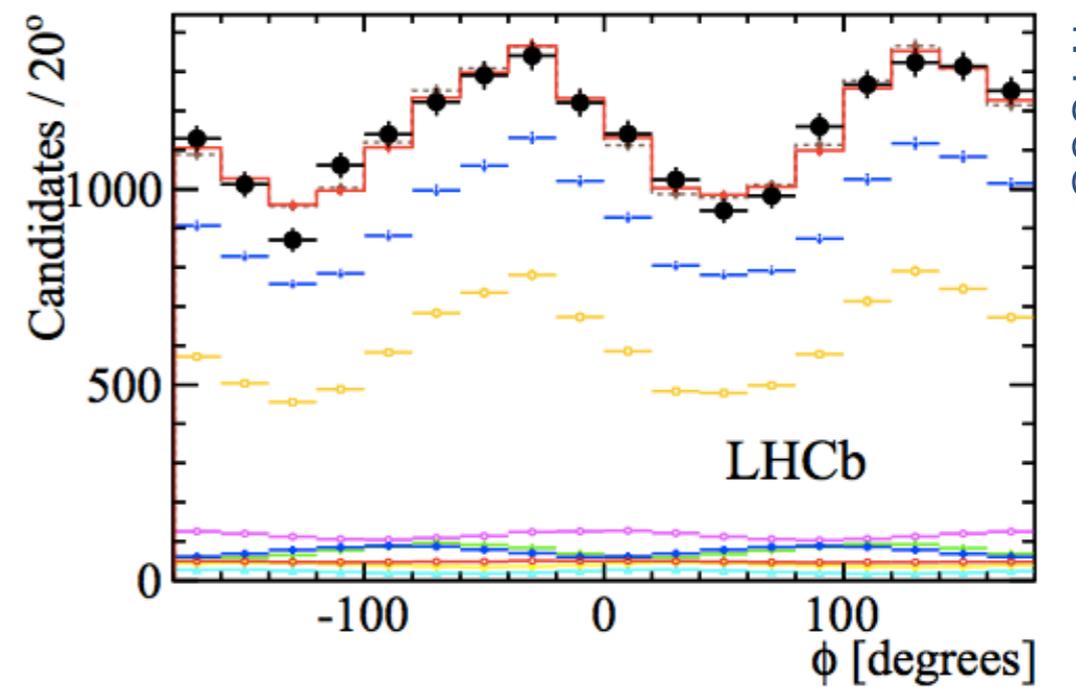
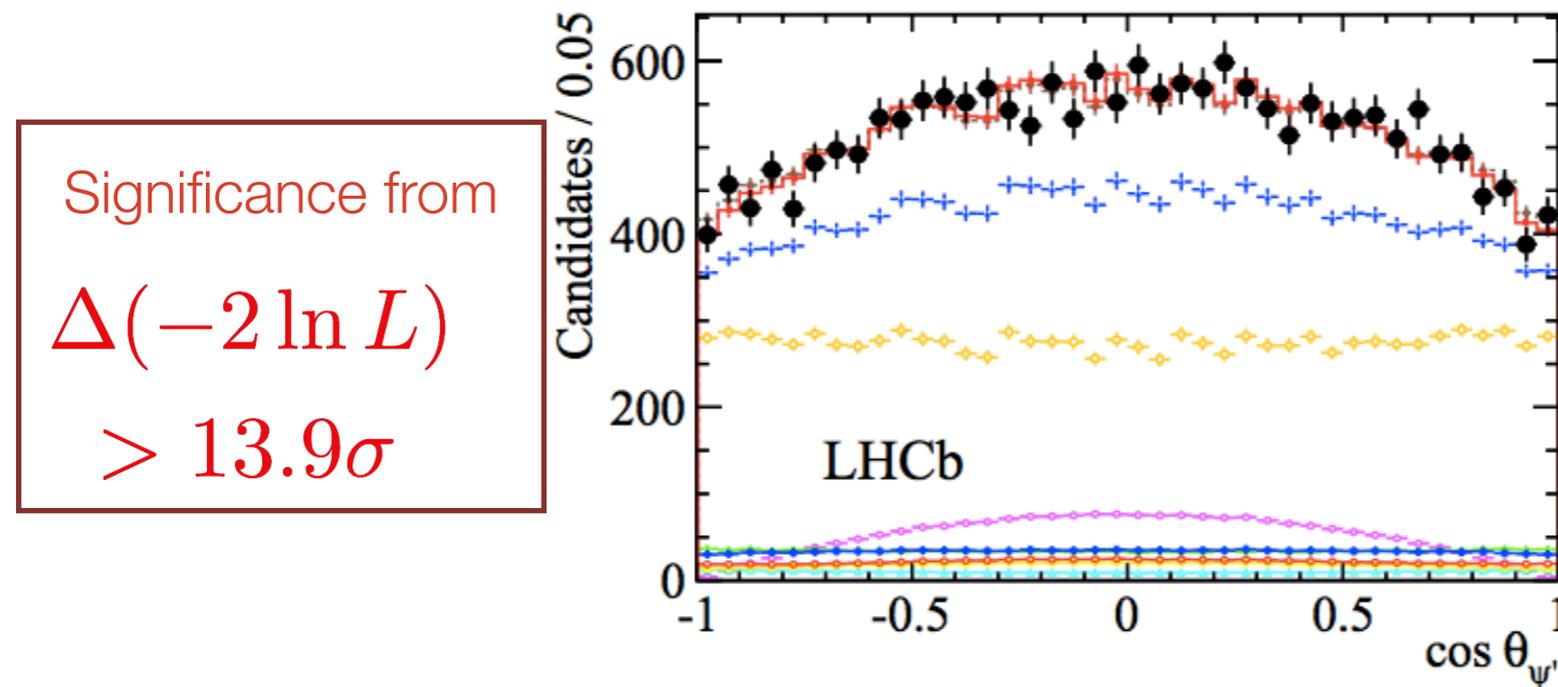
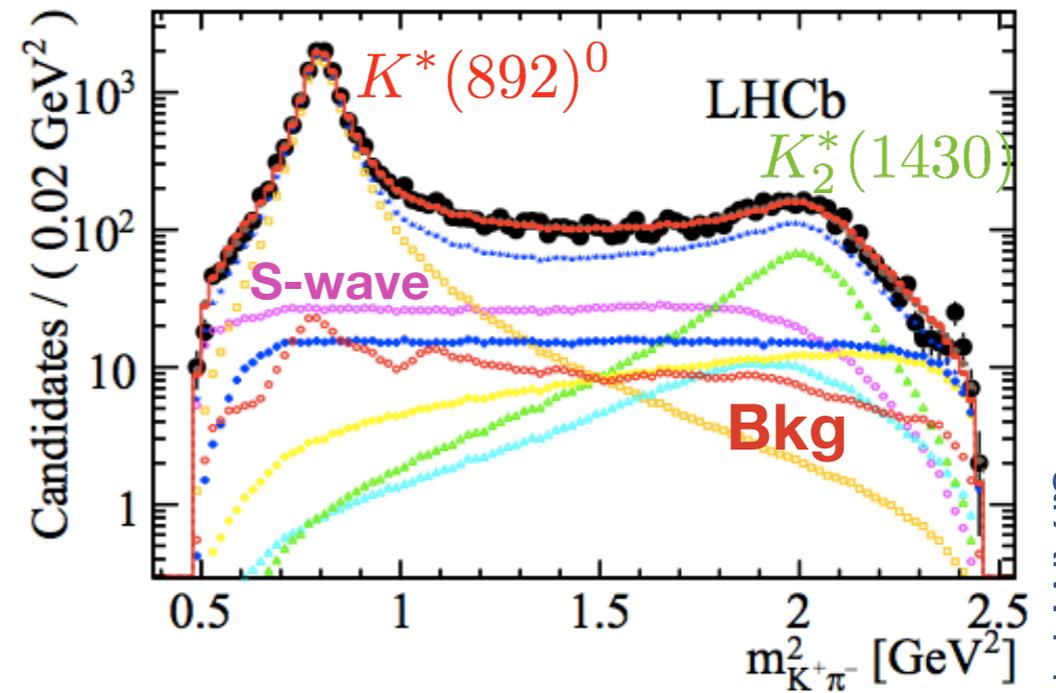
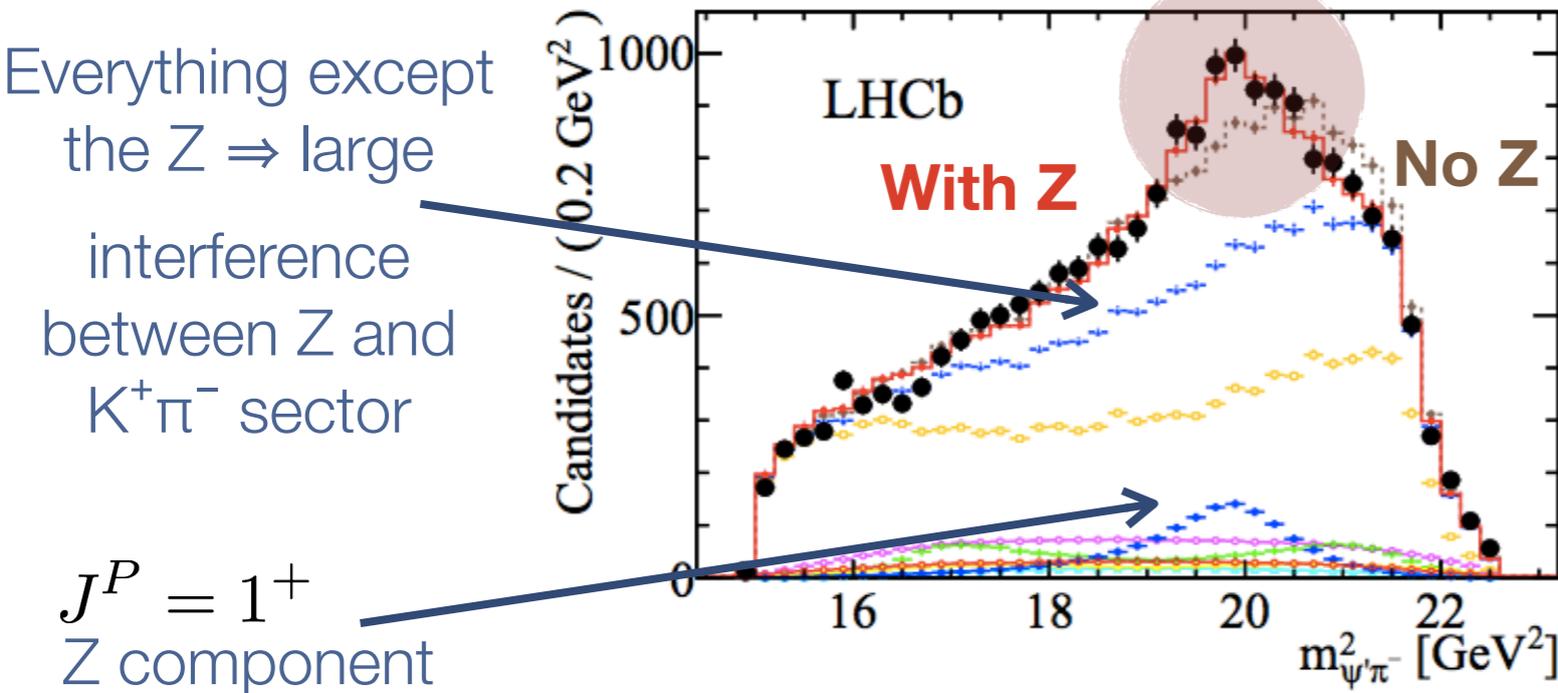
Projections of 4D amplitude fit

Everything except
the Z \Rightarrow large
interference
between Z and
 $K^+\pi^-$ sector

$J^P = 1^+$
Z component



Projections of 4D amplitude fit

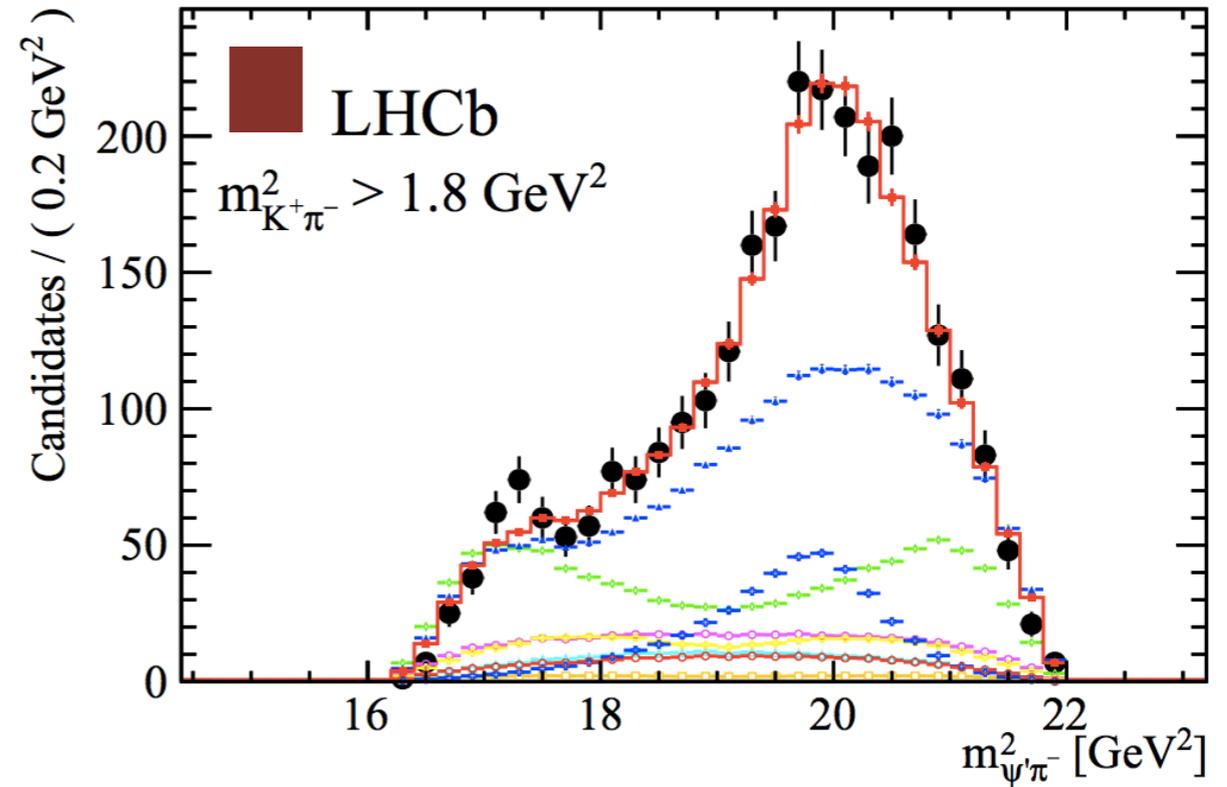
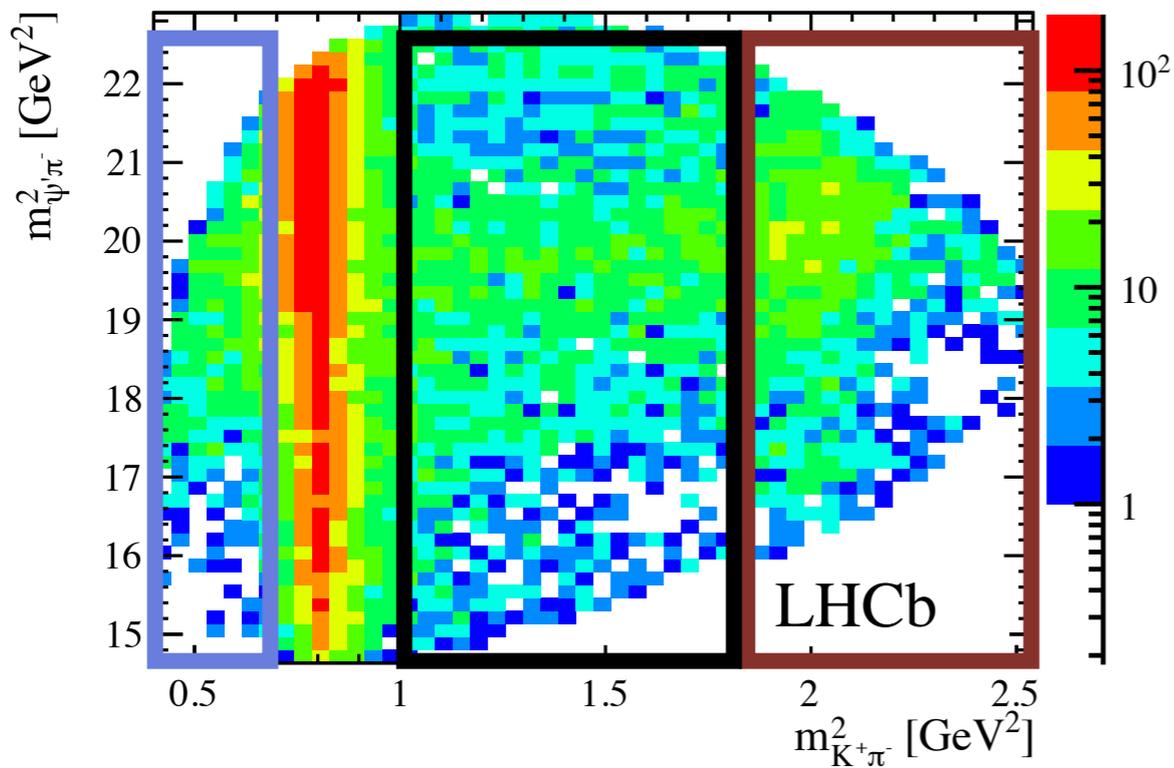
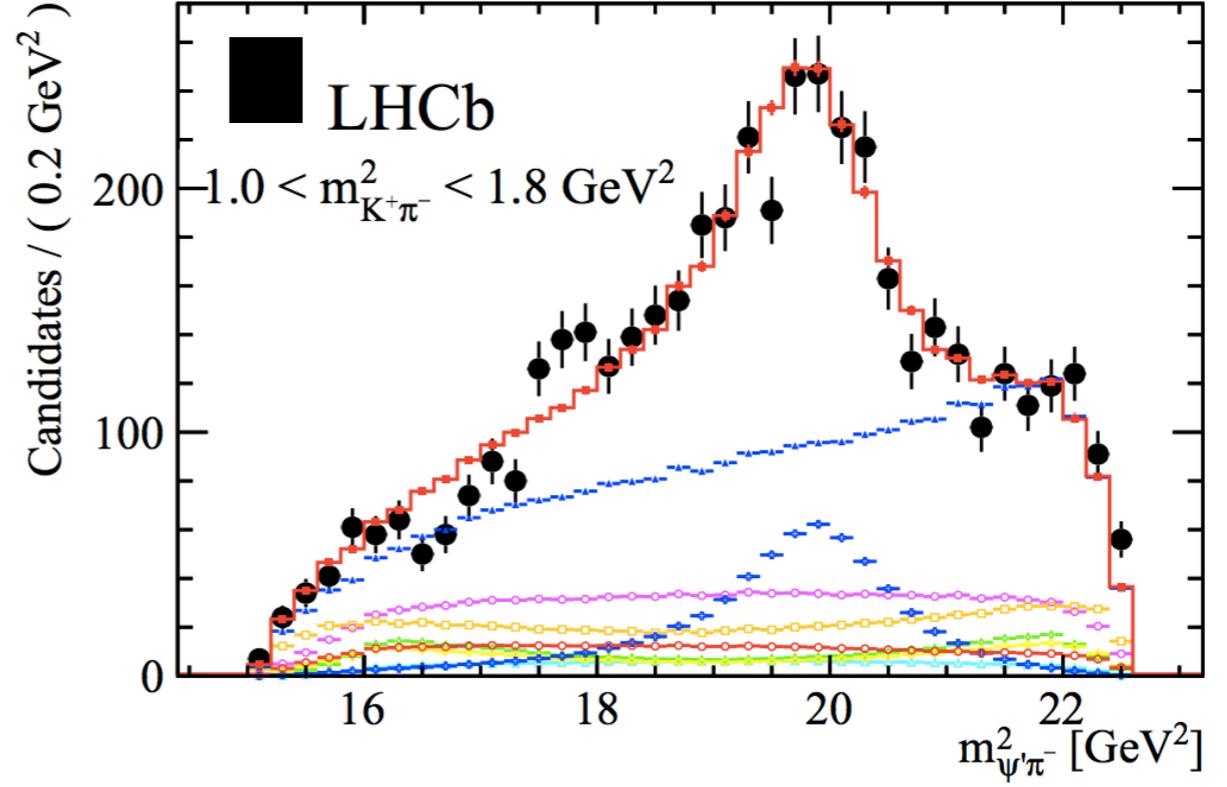
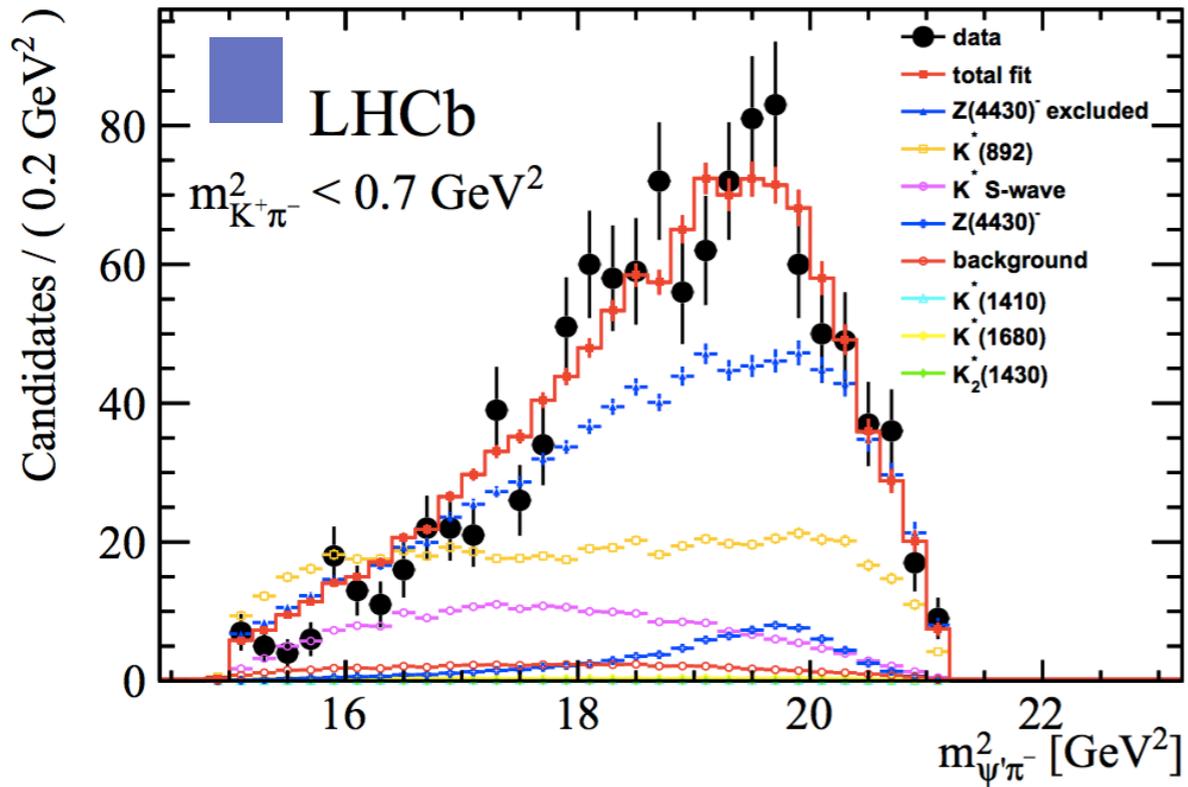


Fitted parameters

$M_Z = 4475 \pm 7 \begin{smallmatrix} +15 \\ -25 \end{smallmatrix} \text{ MeV}$
 $\Gamma_Z = 172 \pm 13 \begin{smallmatrix} +37 \\ -34 \end{smallmatrix} \text{ MeV}$
 $f_Z = (5.9 \pm 0.9 \begin{smallmatrix} +1.5 \\ -3.3 \end{smallmatrix})\%$

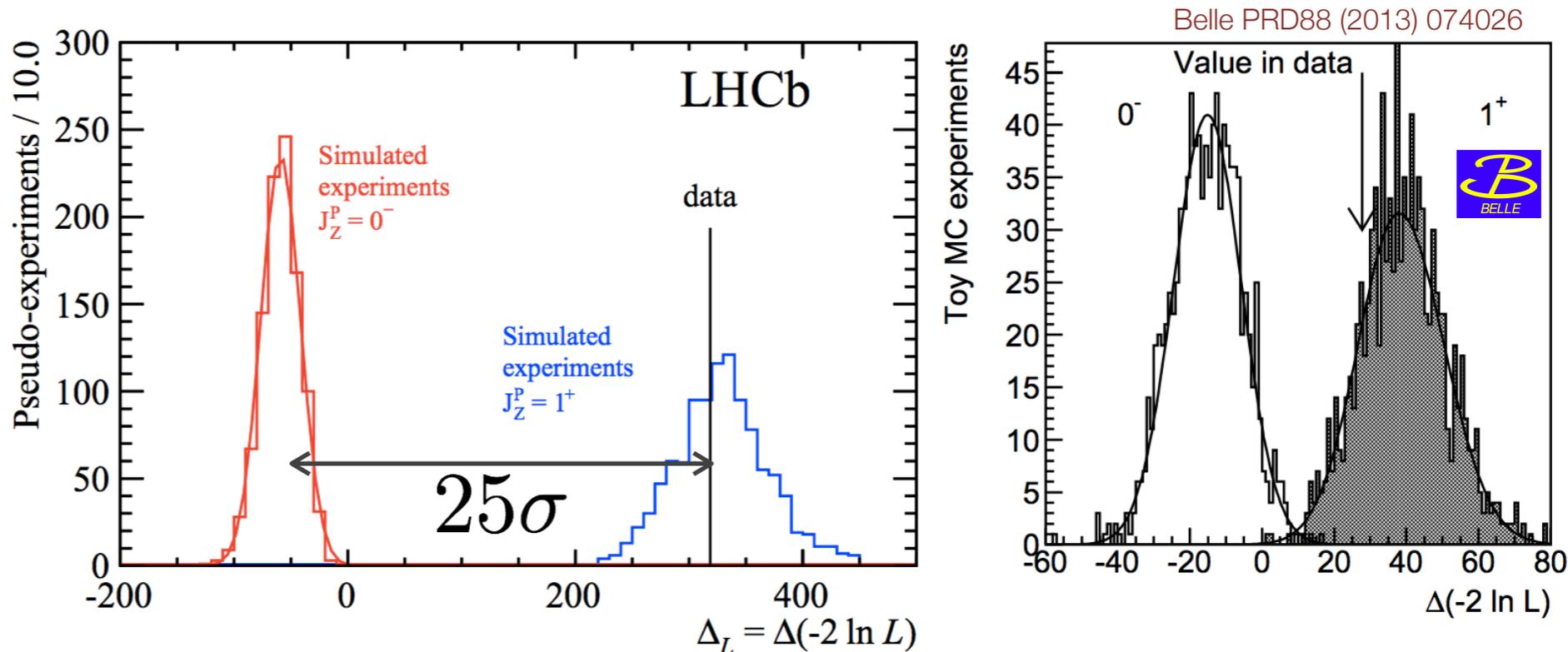
- Goodness of fit confidence level = 12%
- 4% with no $K_1^*(1410)$, 12% with $K_3^*(1780)$

Fit projections in slices of $m_{K^+\pi^-}$



Spin determination and resonant behaviour

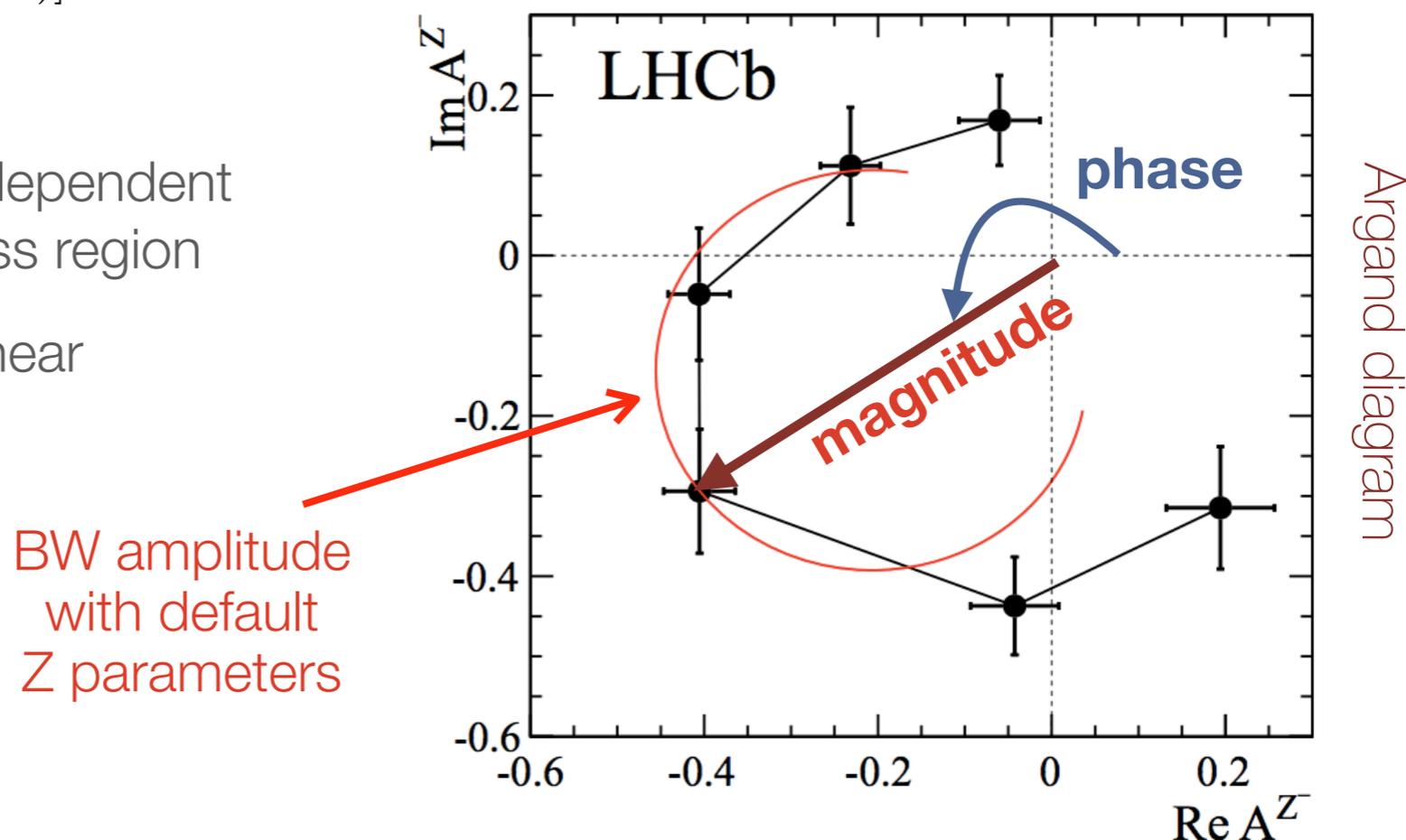
- Build different $|M|^2$ corresponding to different J^P values.
- $J^P=1^+$ assignment favoured (confirms Belle)
- Rule out other J^P with large significance ($> 9\sigma$ after systematics)



$$\Delta(-2 \ln L) = [-2 \ln L(0^-)] - [-2 \ln L(1^+)]$$

- Replace BW amplitude with 6 independent complex numbers in $Z(4430)$ mass region
- Observe rapid change of phase near maximum of magnitude
- Resonance!

arXiv:1404.1903
accepted by PRL



Systematics: second exotic Z?

- Investigated the possibility of a second exotic component.
- Fit confidence level increases to 26%.
- Need larger samples to characterise this state.

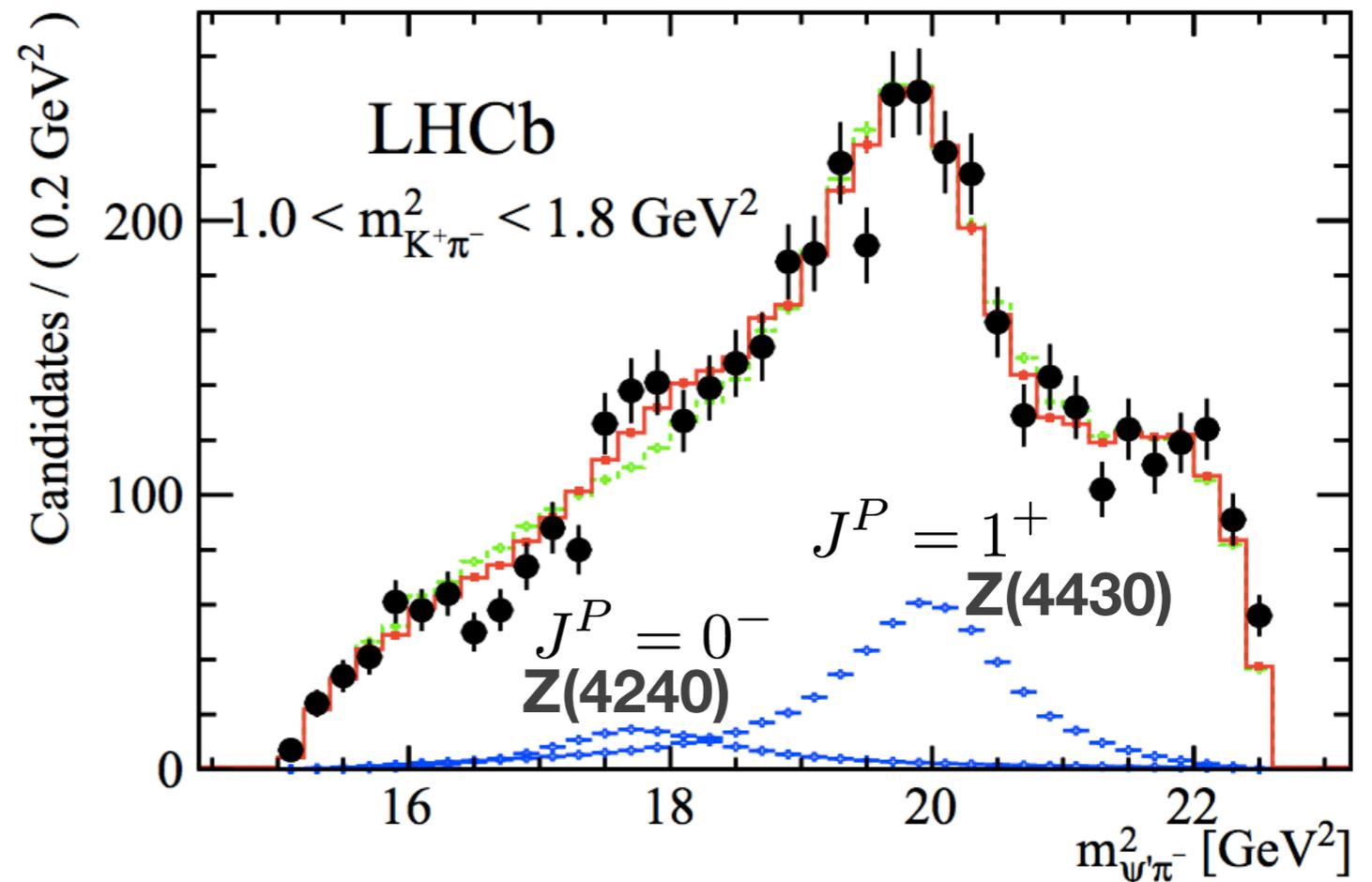
Significance from
 $\Delta(-2 \ln L)$
 6σ

Fitted parameters

$$M_{Z_0} = 4239 \pm 18 \begin{matrix} +45 \\ -10 \end{matrix} \text{ MeV}$$

$$\Gamma_{Z_0} = 220 \pm 47 \begin{matrix} +108 \\ -74 \end{matrix} \text{ MeV}$$

$$f_{Z_0} = (1.6 \pm 0.5 \begin{matrix} +1.9 \\ -0.4 \end{matrix})\%$$



- Many checks performed to determine stability of the result and evaluate systematic errors on m_z , Γ_z , f_z .
- Main systematics come from assumption on $K^+\pi^-$ Isobar model, efficiency and $(q/m_{K^+\pi^-})^L$ vs. q^L

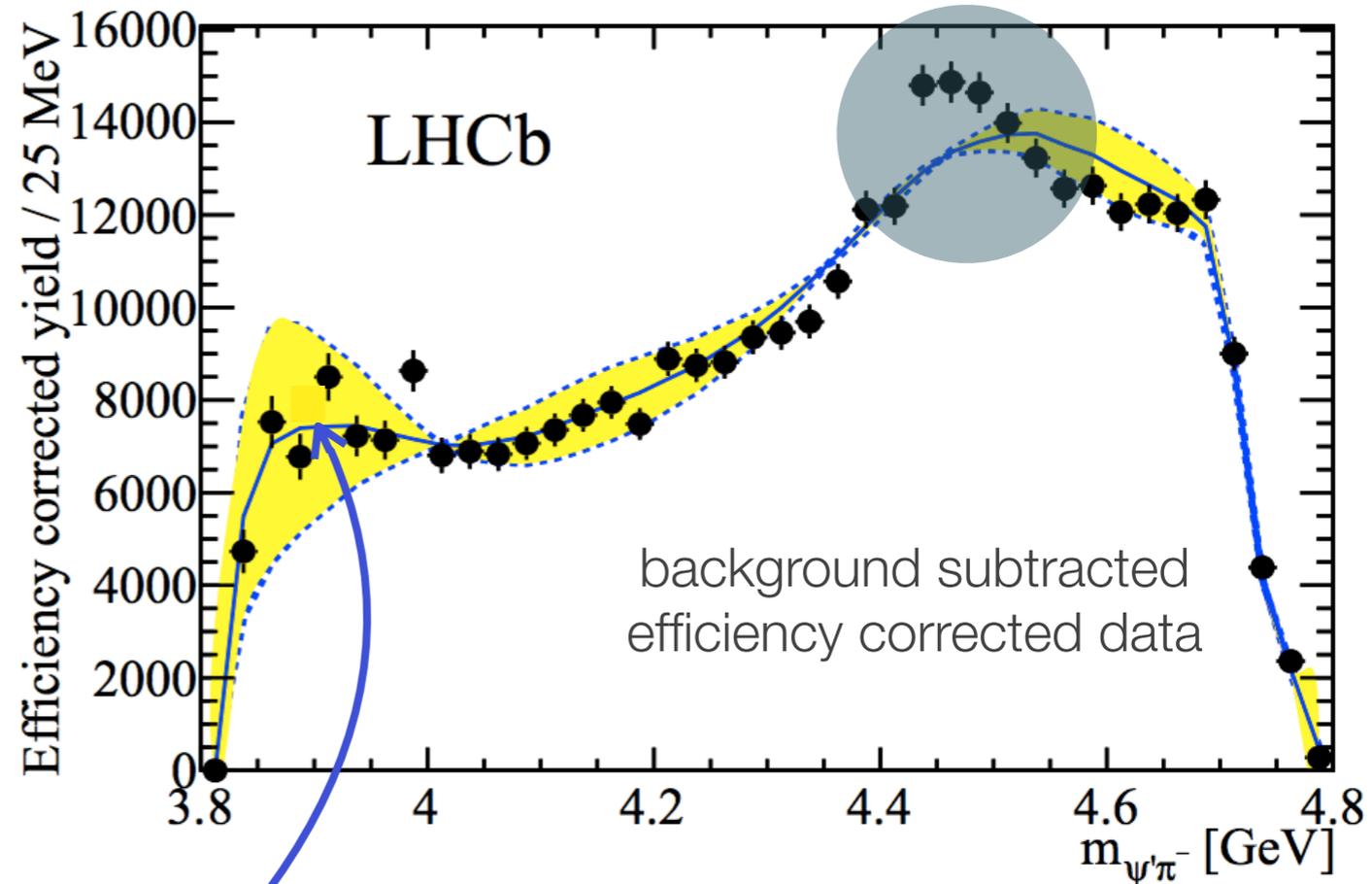
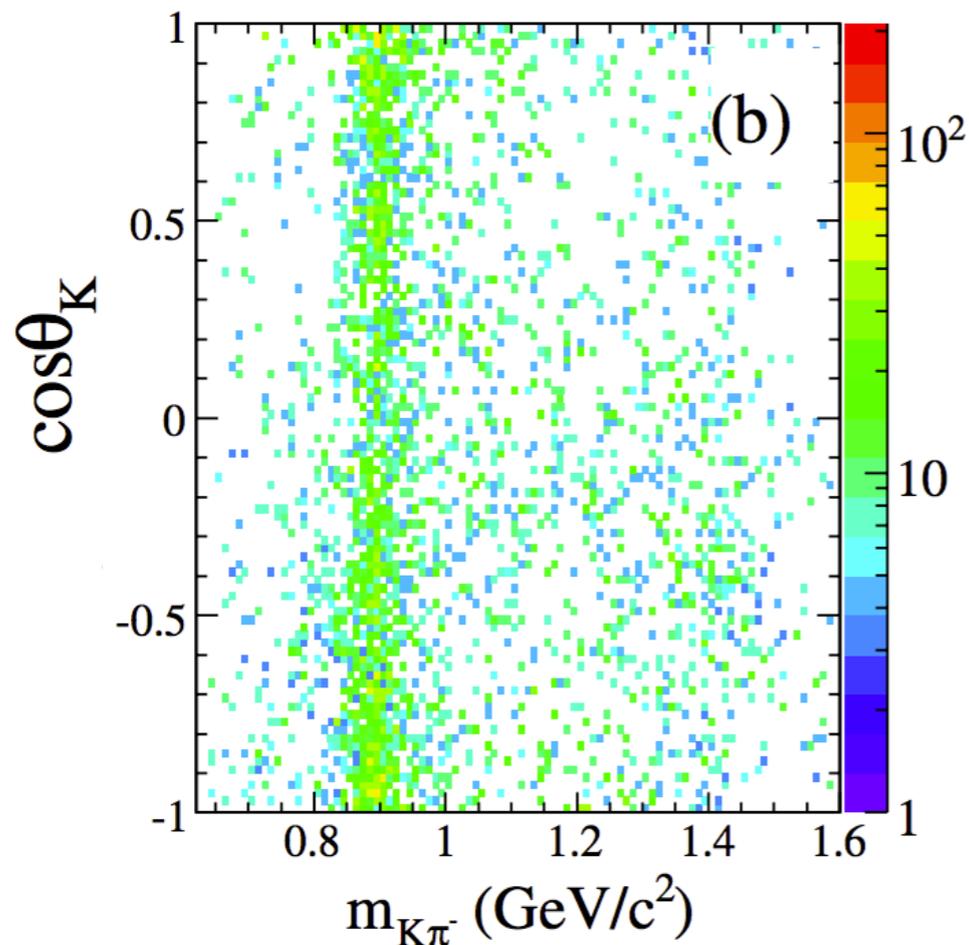
Model independent analysis

Can reflection of the structures in $m(K\pi)$ and $\cos\theta_K$ reproduce the $m(\Psi(2S)\pi)$ distribution?

NO!

BaBar data for $B^0 \rightarrow \psi(2S)K\pi^-$

PRD 79 (2009) 112001



- Does not make any assumption on the underlying K^* resonances in the system, only restricts their maximal spin ($J \leq 2$).
- Weight phase space **simulated events** with the spherical harmonic moments of $\cos\theta_K$
- Moments of K^* resonances are unable to explain observed distribution.

$$Y_1^0 = \sqrt{\frac{3}{4\pi}} \cos\theta$$

$$Y_1^1 = -\sqrt{\frac{3}{8\pi}} \sin\theta e^{i\phi}$$

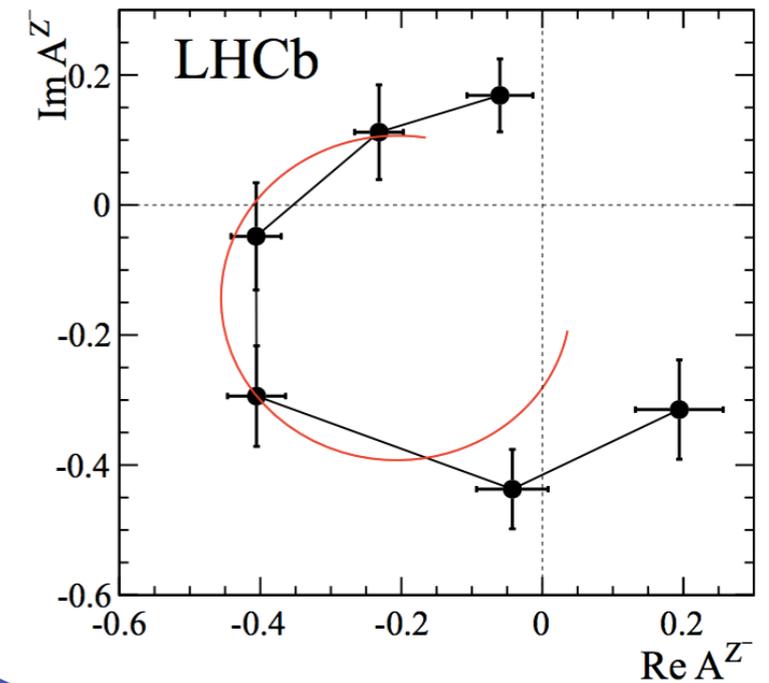
$$Y_2^0 = \sqrt{\frac{5}{4\pi}} \left(\frac{3}{2} \cos^2\theta - \frac{1}{2} \right)$$

$$Y_2^1 = -\sqrt{\frac{15}{8\pi}} \sin\theta \cos\theta e^{i\phi}$$

$$Y_2^2 = \frac{1}{4} \sqrt{\frac{15}{2\pi}} \sin^2\theta e^{2i\phi}$$

A bit more context...

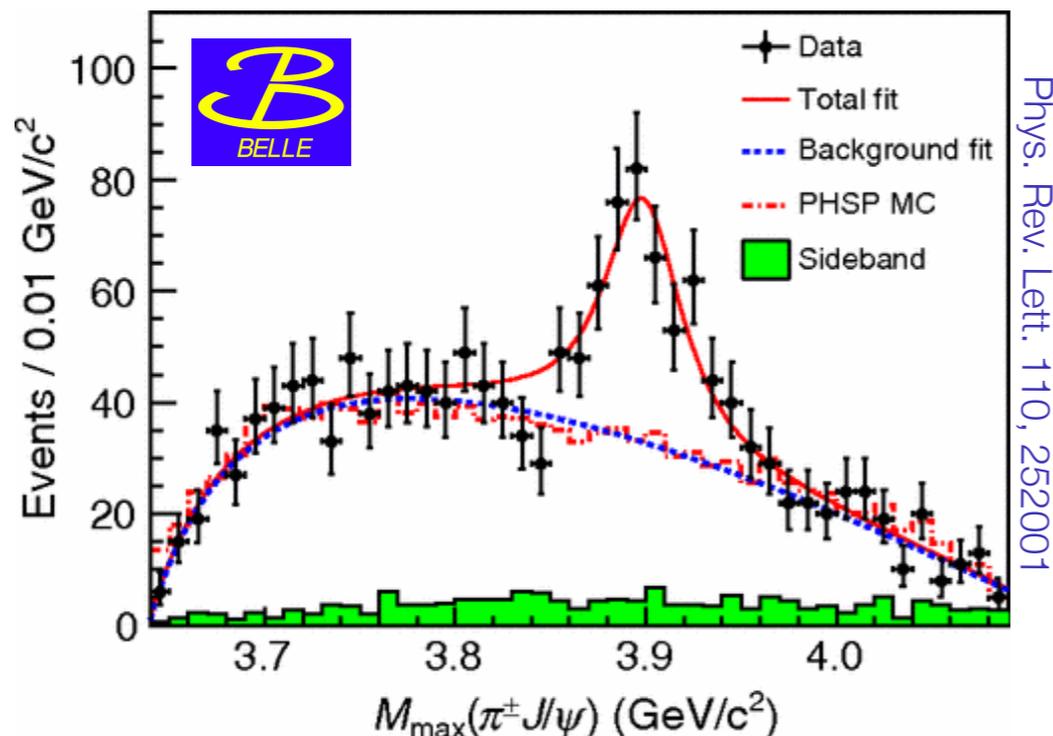
- This result confirms the existence of the $Z(4430)$, measures $J^P=1^+$ and, for the first time, demonstrates the **resonant behaviour**.
- $P=+$ rules out interpretation in terms of $\bar{D}^*(2007)D^*_2(2460)$ molecule or threshold effect.
- Four quark bound state is a remaining explanation.
- Last year BESIII and Belle observed another **exotic charged** state.



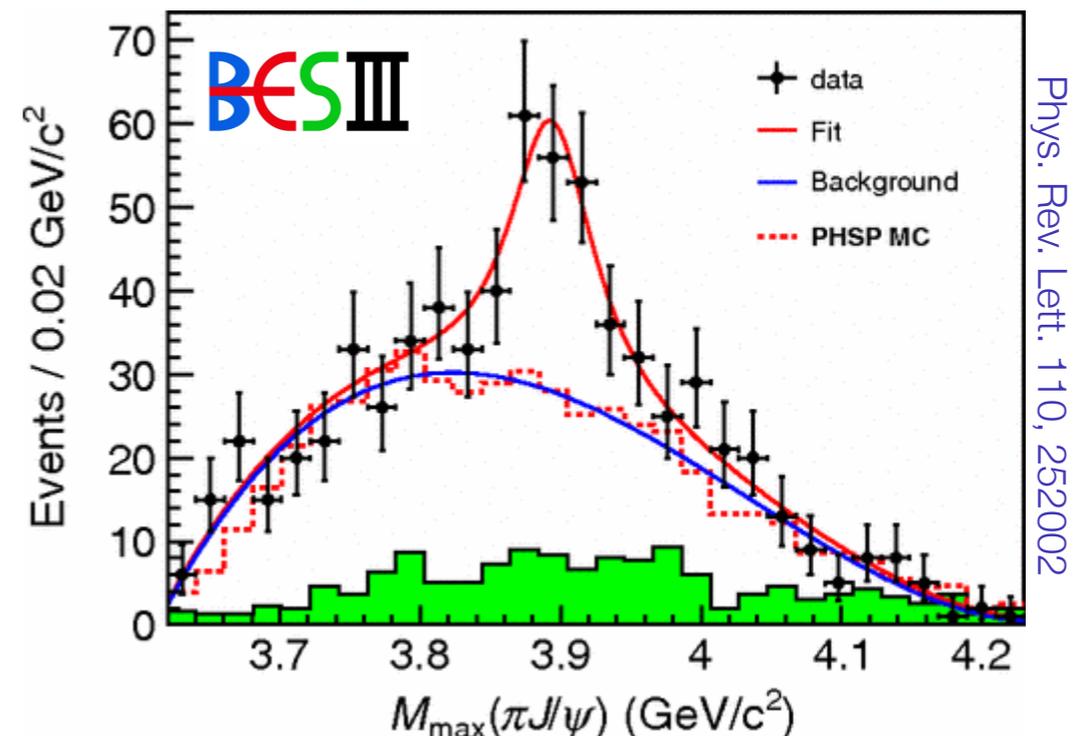
Rosner, Phys. Rev. D76 (2007) 114002
Bugg, J. Phys. G35 (2008) 075005

$Z_c(3900)$ in $e^+e^- \rightarrow \pi^+\pi^-J/\psi$

$M = (3894.5 \pm 6.6 \pm 4.5) \text{ MeV}/c^2$
 $\Gamma = (63 \pm 24 \pm 26) \text{ MeV}/c^2$



Phys. Rev. Lett. 110, 252001

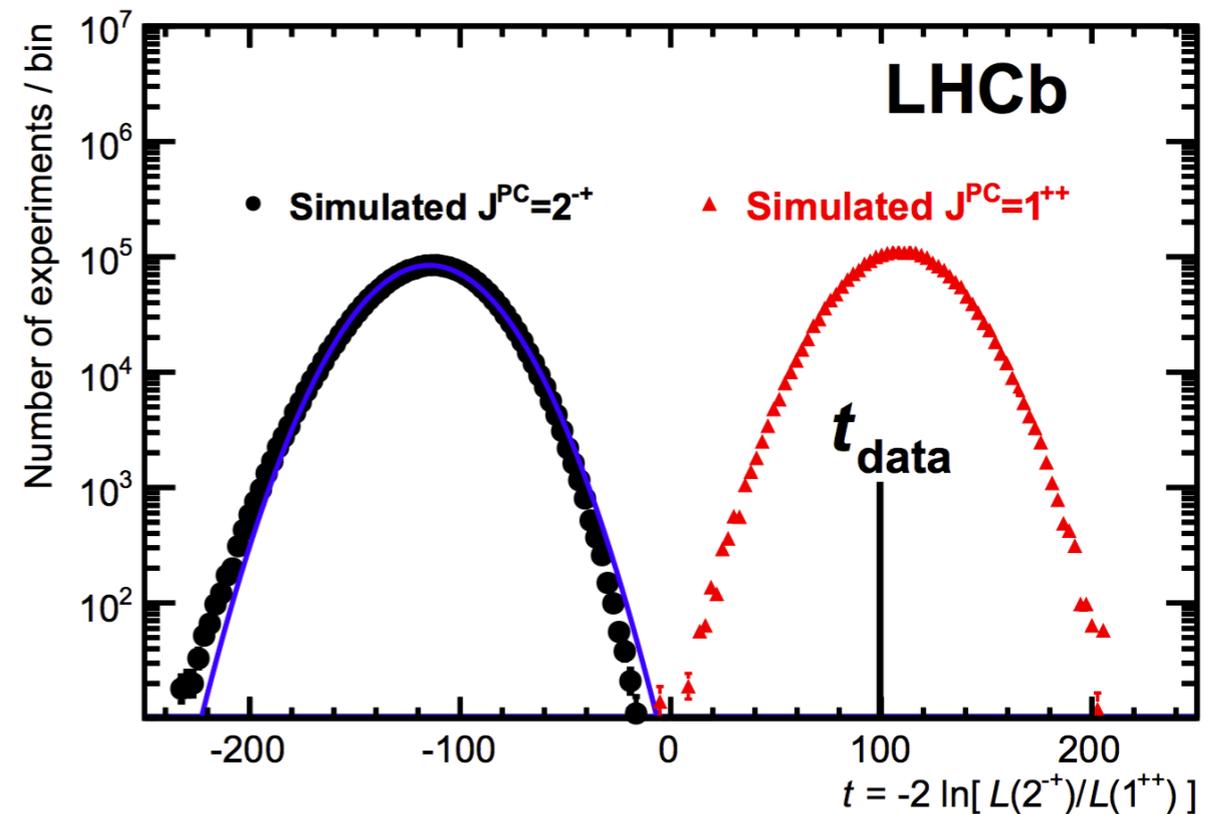
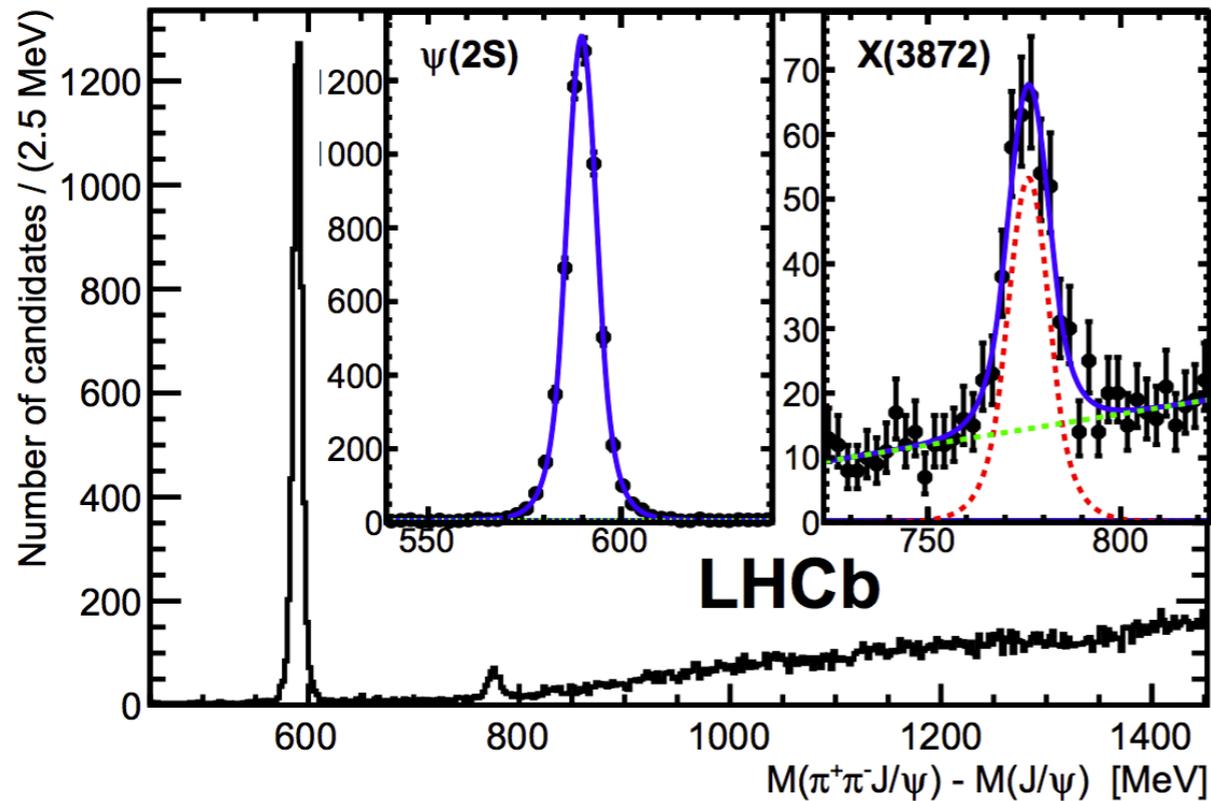


Phys. Rev. Lett. 110, 252002

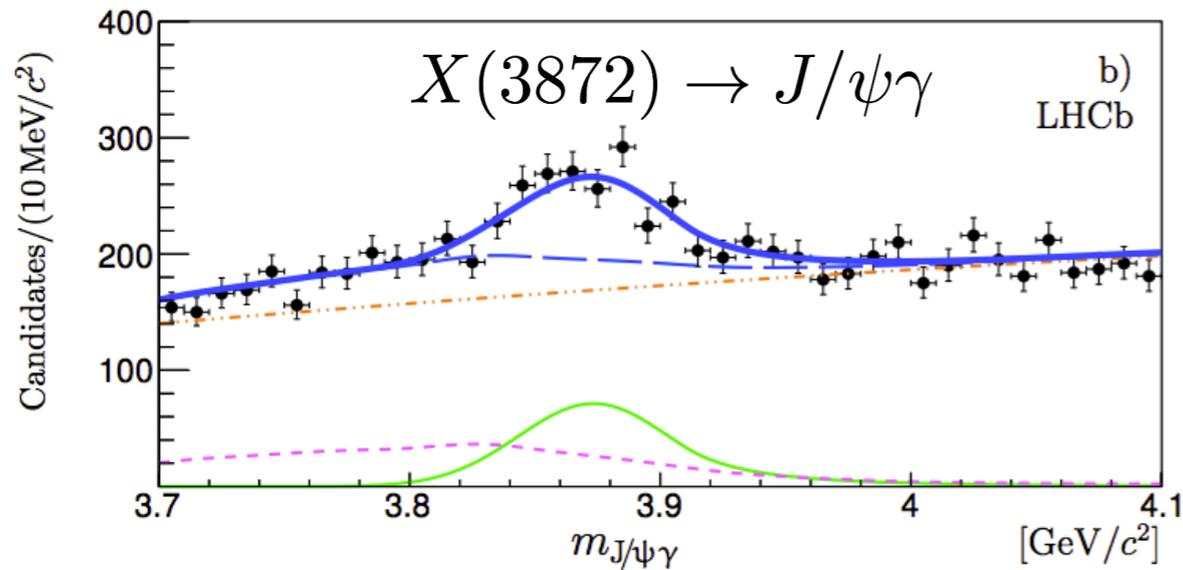
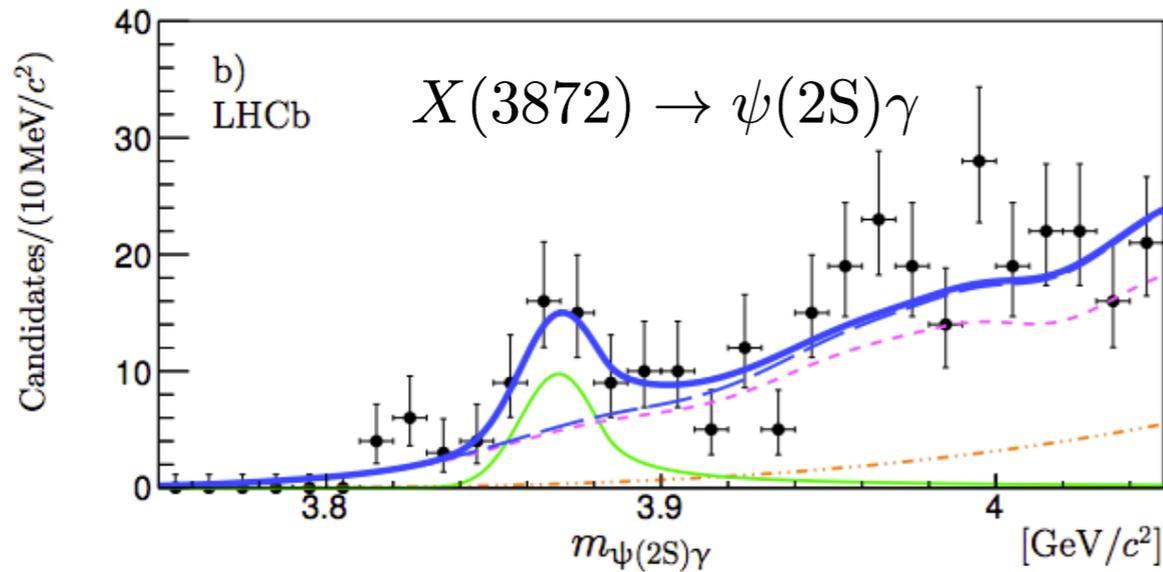
1D fit to $m(\pi J/\psi)$ only

A well known exotic meson: X(3872)

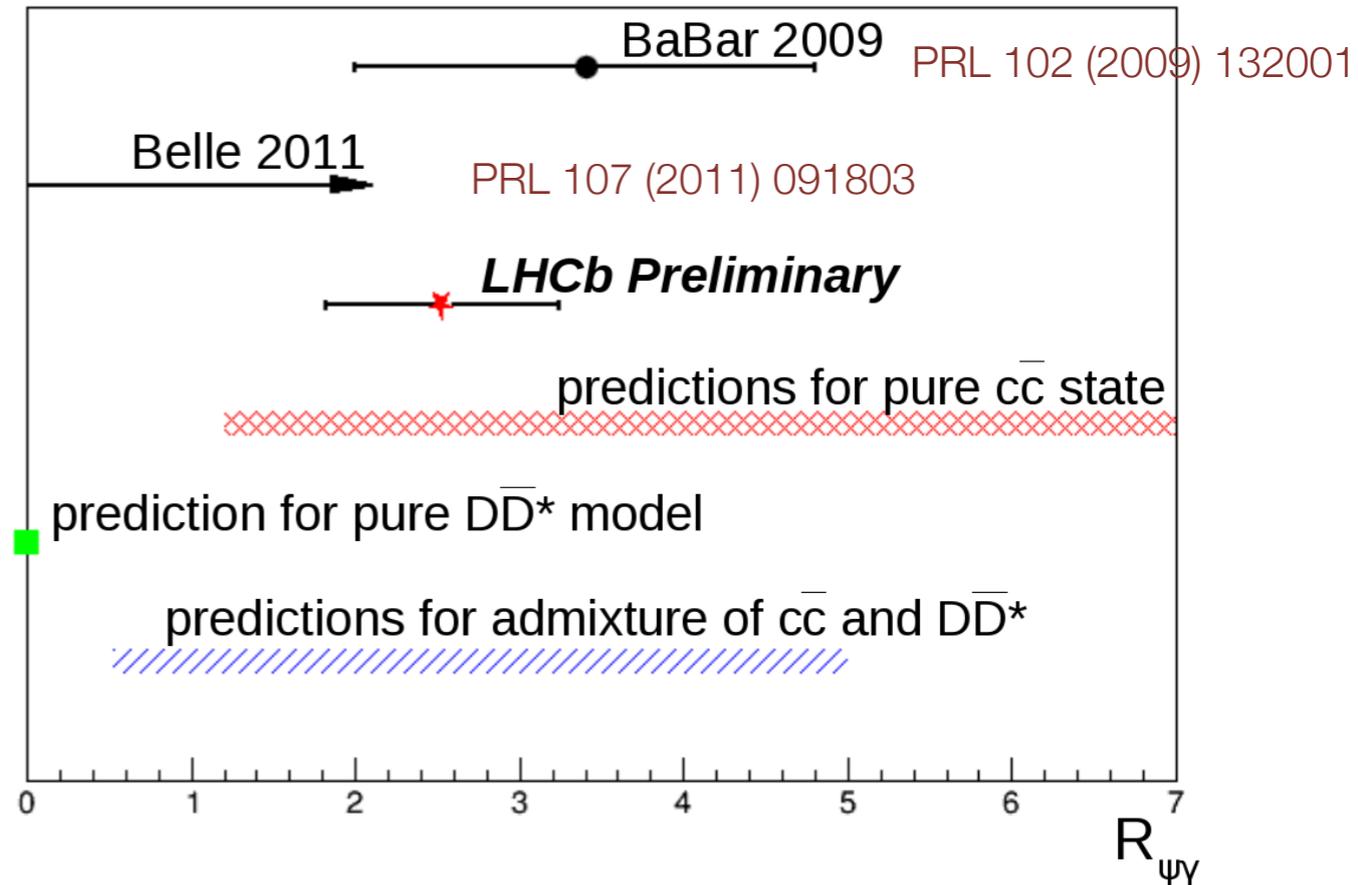
- Observed by many experiments, first by Belle (PRL 91 (2003) 262001 - 894 citations!)
- $B^+ \rightarrow X(3872)K^+$, $X(3872) \rightarrow J/\psi\pi^+\pi^-$
- Use well-known $\psi(2S)$ resonance to calibrate
- Measure $J^{PC} = 1^{++}$ - favours exotic interpretation
- Could be some combination of $c\bar{c}u\bar{u}$ quarks or **DD*** molecule



A well known exotic meson: X(3872)



- LHCb has evidence for X(3872) in decays of $B^+ \rightarrow \psi\gamma K^+$, $\psi \rightarrow \mu^+\mu^-$
- Pure DD* molecule interpretation disfavoured



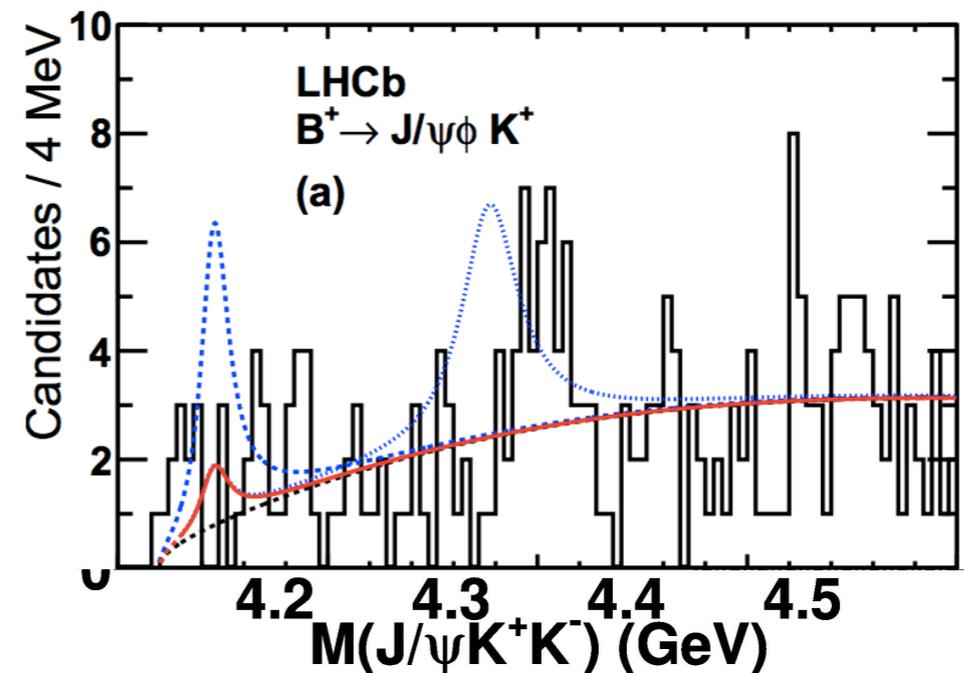
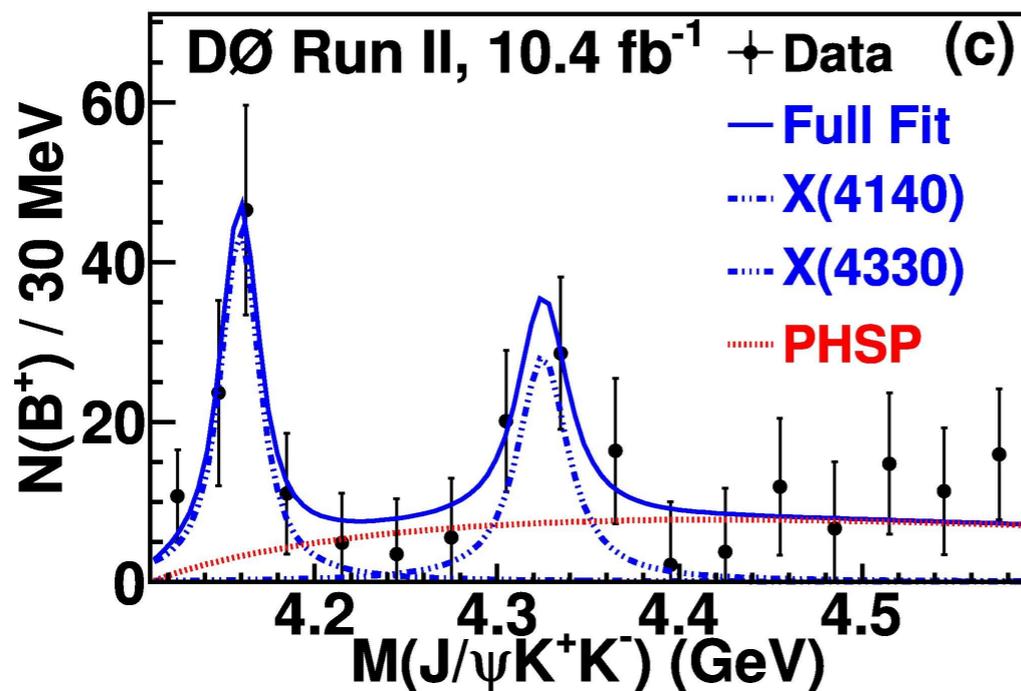
$$R_{\psi\gamma} = \frac{\mathcal{B}(X(3872) \rightarrow \psi(2S)\gamma)}{\mathcal{B}(X(3872) \rightarrow J/\psi\gamma)} = 2.46 \pm 0.64 \pm 0.29$$

An enigma... the X(4140)

$$B^{\pm/0} \rightarrow XK^{\pm/0} \quad X \rightarrow J/\psi\phi$$

Experiment	Mass (MeV)	Width (MeV)	σ	Published?	Ref.
CDF	$4143.0 \pm 2.9 \pm 1.2$	11.7	3.8	Y	Phys. Rev. Lett. 102 , 242002
CDF	4143.4	15.3	>5	N	Public Note 10244
D0	$4159.0 \pm 4.3 \pm 6.6$	19.9 ± 12.6	3.1	Y	Phys. Rev. D 89 , 012004
CMS	$4148.0 \pm 2.4 \pm 6.3$	28	>5	N	arXiv:1309.6920
Belle	-	-	-	Y	Phys. Rev. Lett. 104 , 112004
LHCb	-	-	-	Y	Phys. Rev. D 85 , 091103(R)
BaBar	-	-	-	N	-

• Could be some hybrid state: $c\bar{c}s\bar{s}$



Light quark spectroscopy using $B^0 \rightarrow J/\psi \pi^+ \pi^-$

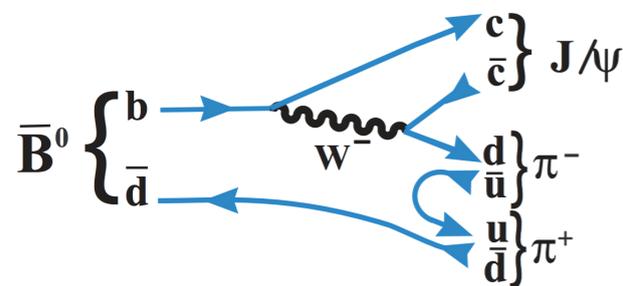
- Study substructure of light mesons that decay to $\pi^+ \pi^-$.
- Mass ordering is reversed between the scalar and vector mesons nonets.

Isospin	$I = 0$	$I = 1/2$	$I = 0$	$I = 1$
Scalar mesons	$f_0(500)$	$\kappa(800)$	$f_0(980)$	$a_0(980)$
Vector mesons	$\phi(1020)$	$K^*(892)^0$	$\omega(783)$	$\rho(776)$

- Are the scalar mesons ($f_0(500)$, $f_0(980)$) $q\bar{q}$ or **tetraquarks** or some mixture?

Scalar meson mixing

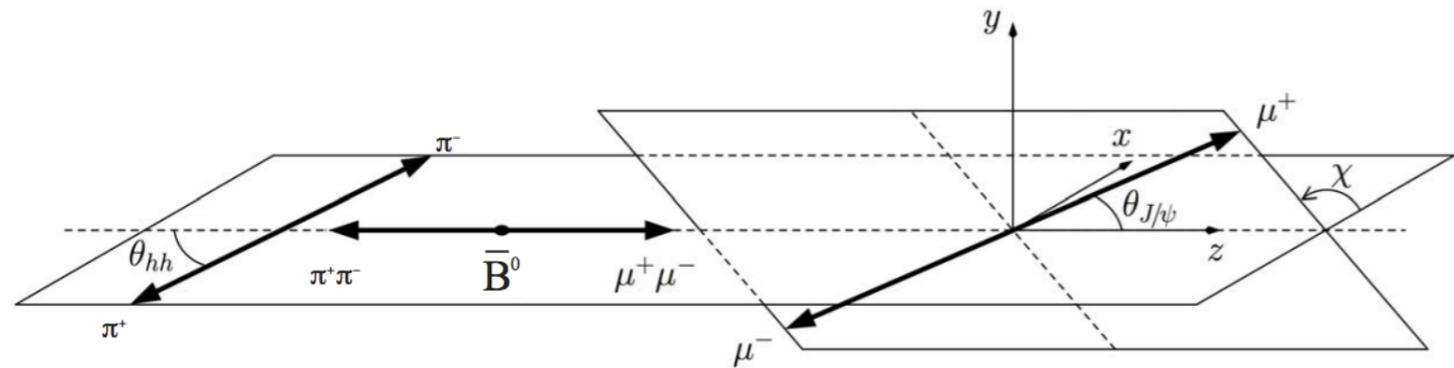
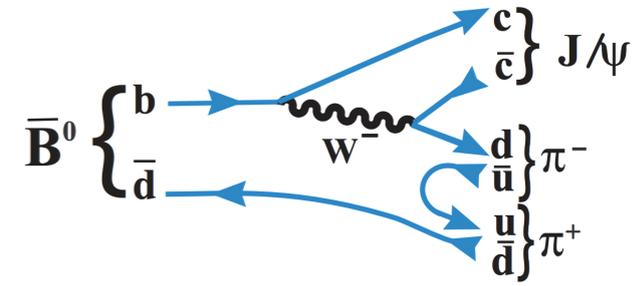
$$\begin{aligned}
 |f_0(980)\rangle &= \cos \varphi_m |s\bar{s}\rangle + \sin \varphi_m |n\bar{n}\rangle \\
 |f_0(500)\rangle &= -\sin \varphi_m |s\bar{s}\rangle + \cos \varphi_m |n\bar{n}\rangle, \\
 \text{where } |n\bar{n}\rangle &\equiv \frac{1}{\sqrt{2}} (|u\bar{u}\rangle + |d\bar{d}\rangle).
 \end{aligned}$$



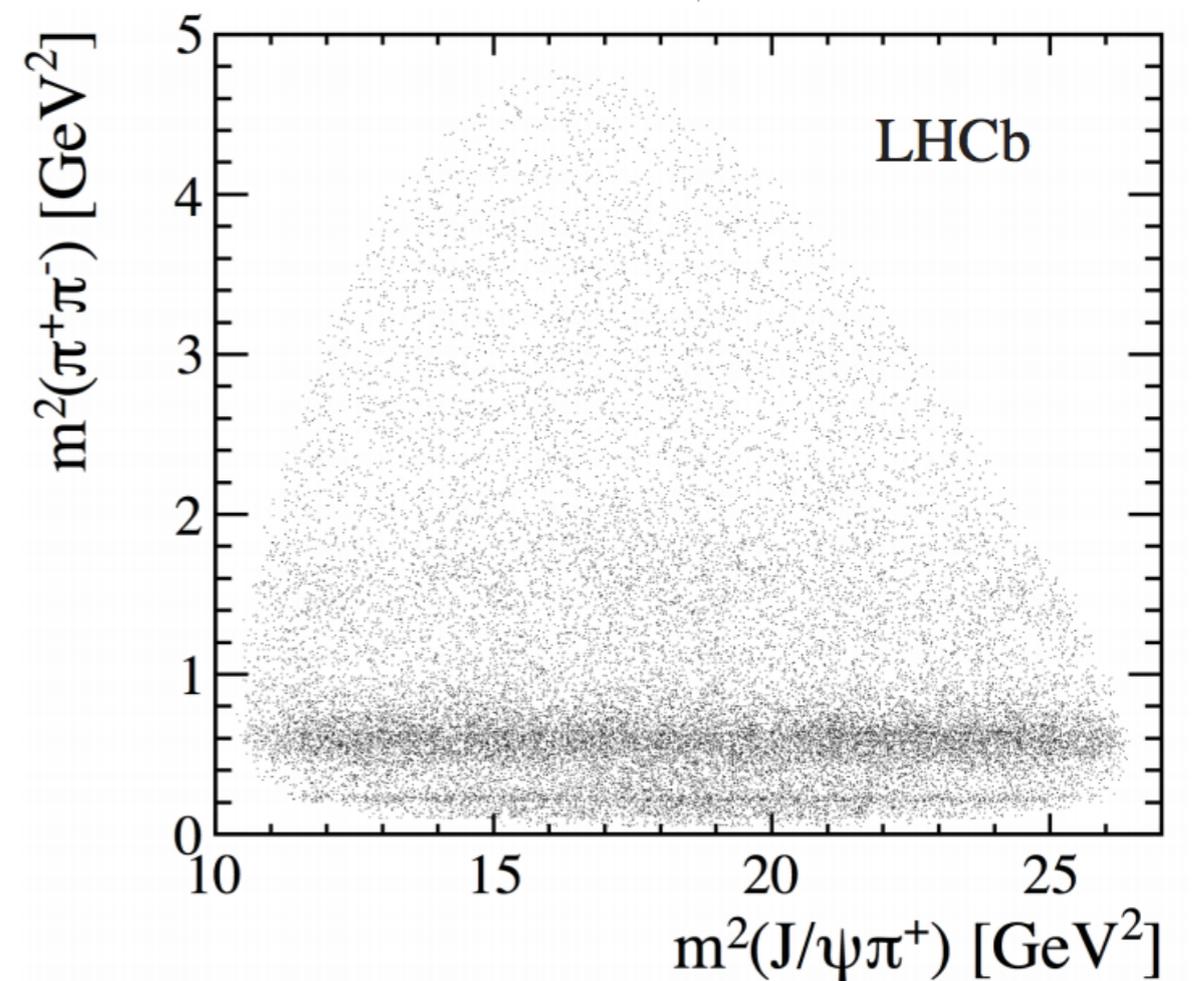
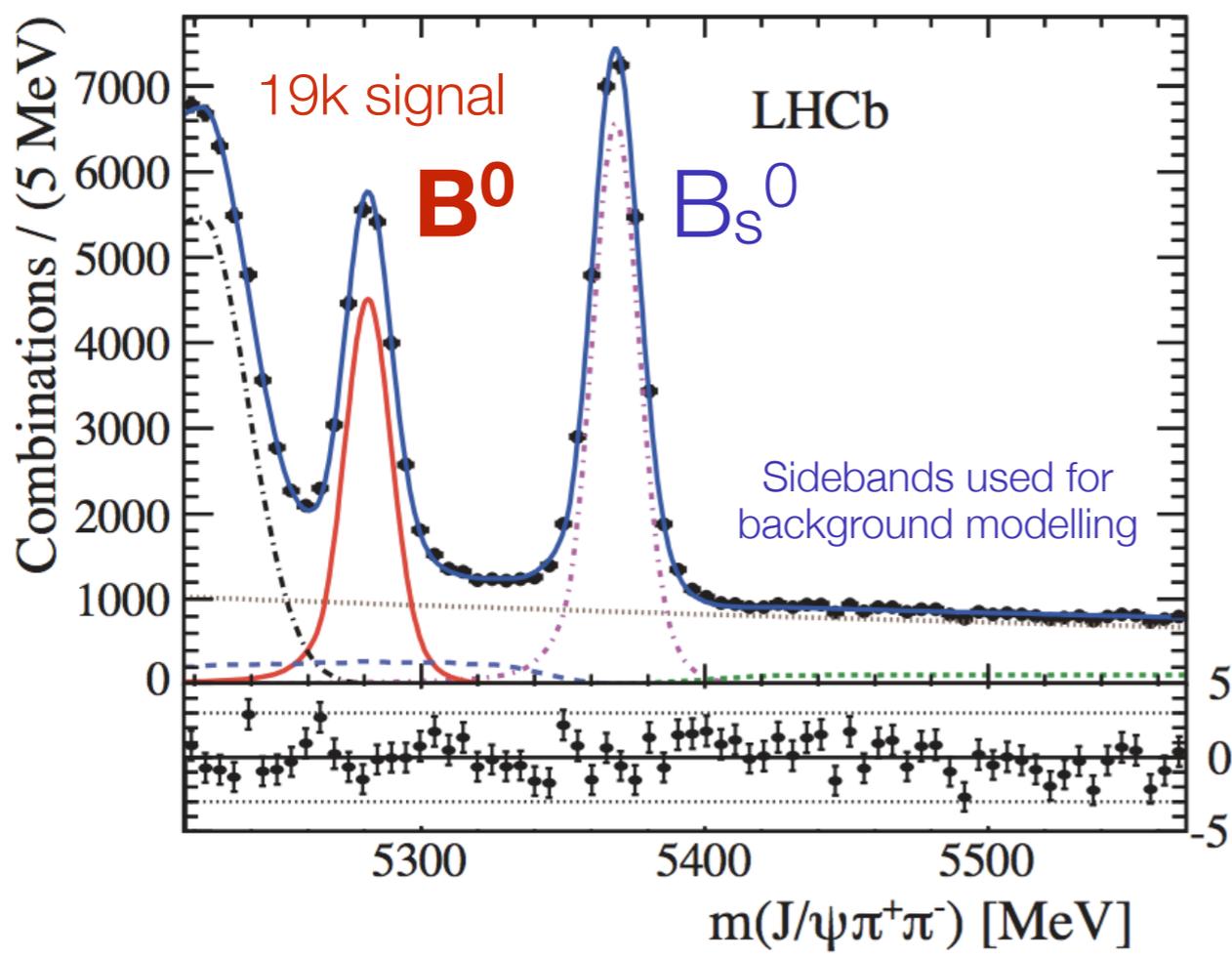
$$\tan^2 \varphi_m \equiv r_\sigma^f = \frac{\mathcal{B}(\bar{B}^0 \rightarrow J/\psi f_0(980)) \Phi(500)}{\mathcal{B}(\bar{B}^0 \rightarrow J/\psi f_0(500)) \Phi(980)}, \quad = 1/2$$

↑
phase space

Amplitude analysis of $B^0 \rightarrow J/\psi \pi^+ \pi^-$



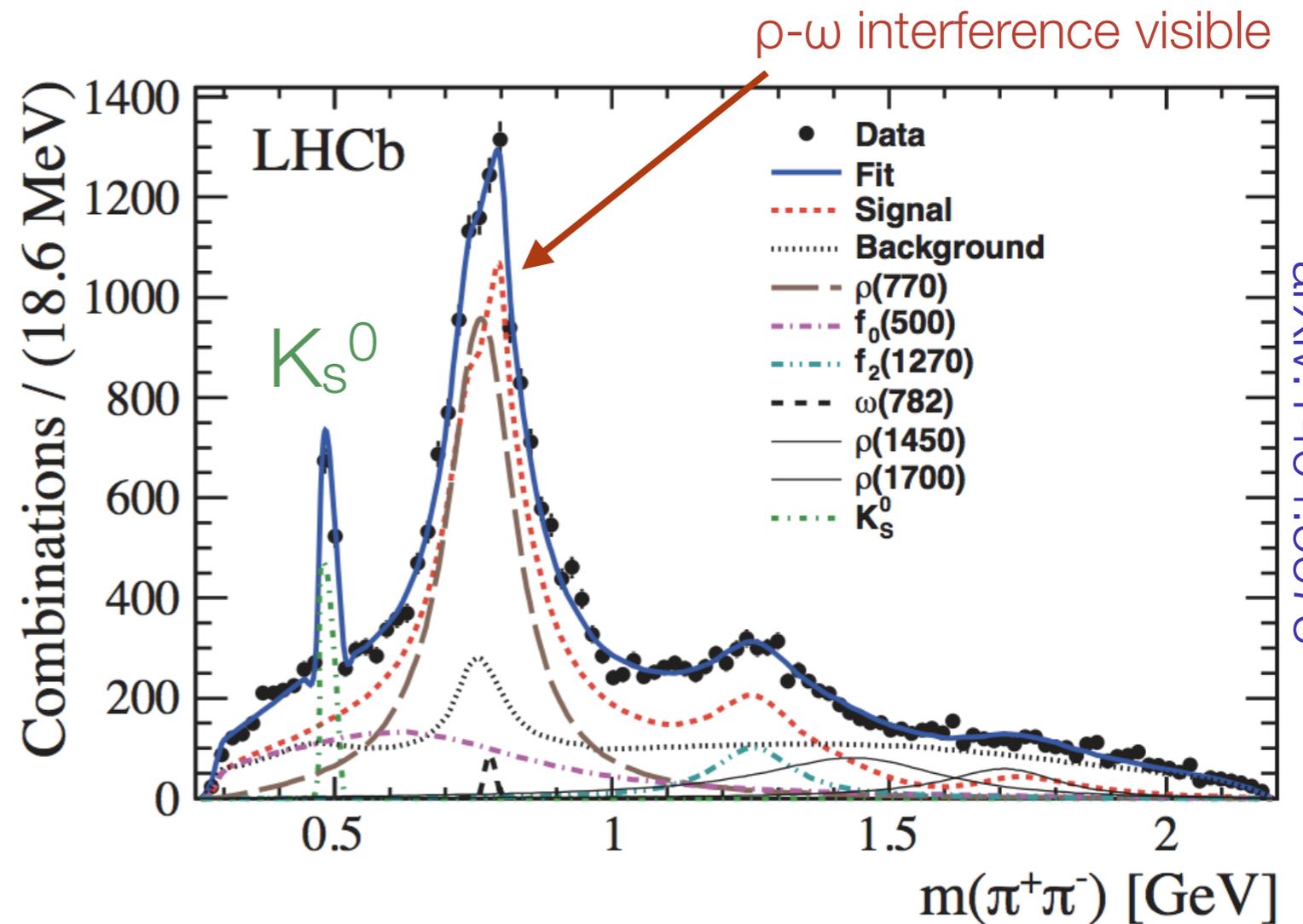
- Similar analysis to Z(4430)
 - Build 4D matrix element from overlapping $\pi^+ \pi^-$ resonances.
 - Correct for efficiency.
- No sign of exotic $J/\psi \pi^+$ resonances...



arXiv:1404.5673

Amplitude analysis of $B^0 \rightarrow J/\Psi \pi^+ \pi^-$

Component	Fit fraction (%)
$\rho(770)$	$63.1 \pm 2.2^{+3.4}_{-2.2}$
$f_0(500)$	$22.2 \pm 1.2^{+2.6}_{-3.5}$
$f_2(1270)$	$7.5 \pm 0.6^{+0.4}_{-0.6}$
$\omega(782)$	$0.68^{+0.20+0.17}_{-0.14-0.13}$
$\rho(1450)$	$11.6 \pm 2.8 \pm 4.7$
$\rho(1700)$	$5.1 \pm 1.2 \pm 3.0$



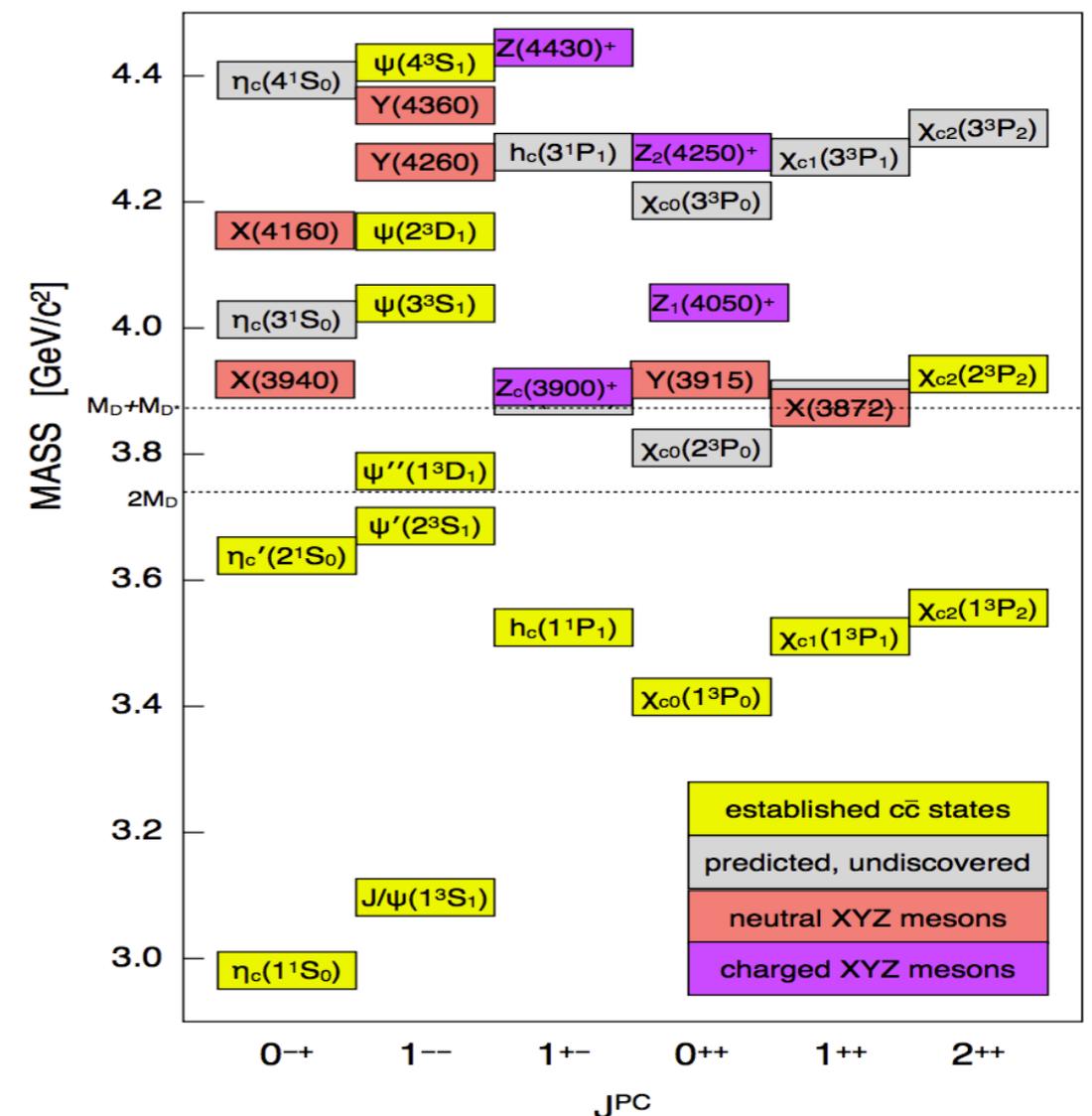
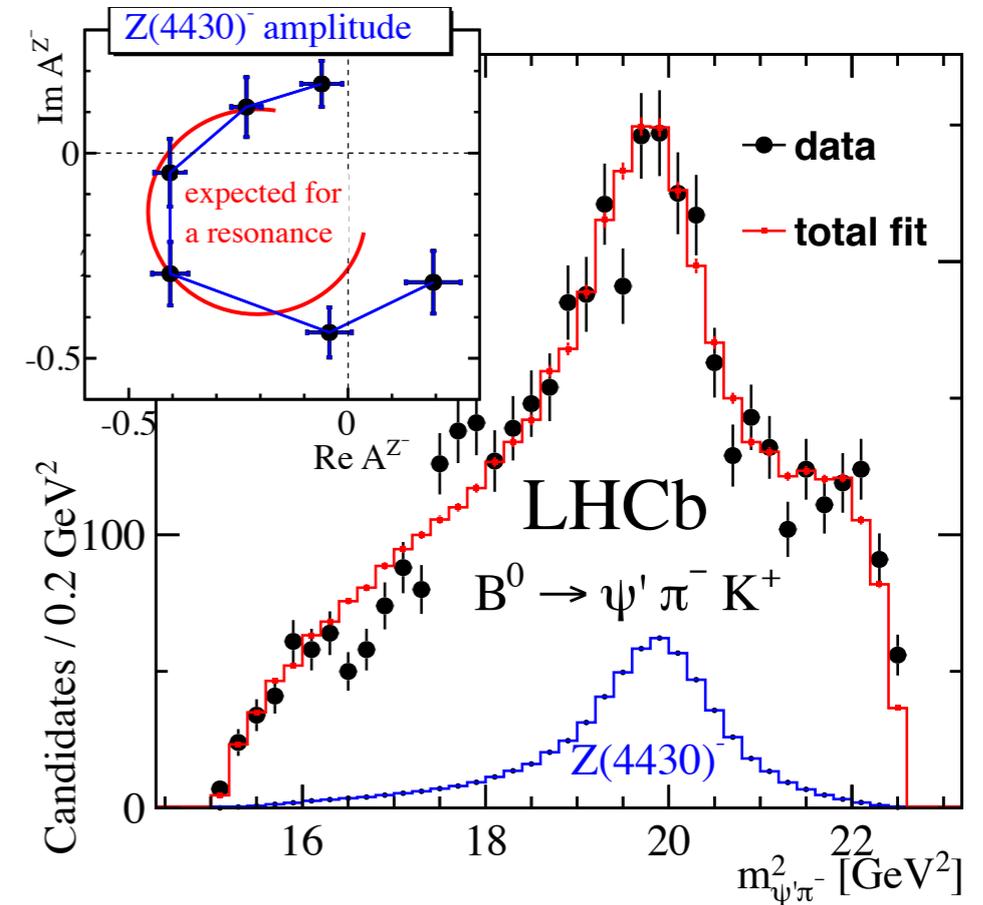
- Best fit model shows does not require $f_0(980)$ component.
- Gives upper limit on the mixing angle between $f_0(500)$ and $f_0(980)$.

$$\tan^2 \varphi_m \equiv r_\sigma^f = (1.1^{+1.2+6.0}_{-0.7-0.7}) \times 10^{-2} < 0.098 \quad \text{at 90\% C.L}$$

Different from tetraquark prediction (1/2) by 8σ

Summary

- LHCb has confirmed this existence and shown the **resonant** behaviour of the $Z(4430)^-$.
- Minimal quark content of $c\bar{c}u\bar{d}$.
- No clear picture of the complex system of charmonium-like exotic resonances.
- $Z(4430)^-$ should help to improve understanding.
- Further constraints could come from observing this in other decay modes.
- Next steps...
 - LHCb has large datasets of B decays containing J/ψ , $\Psi(2S)$, $\chi_{c\dots}$ where other exotics could live.
 - Data taking starts again in 2015, looking forward to collecting even higher statistics!



BACKUP

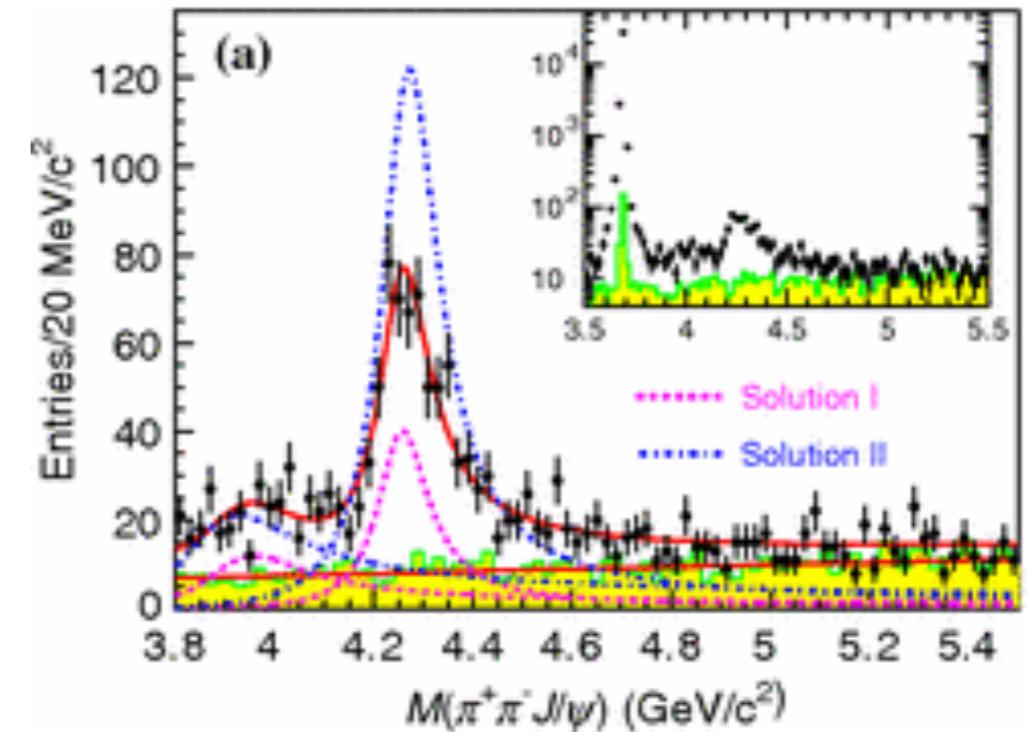
$Z_c(3900)$ in $e^+e^- \rightarrow \pi^+\pi^-J/\psi$

- Other exotic **charged** state observed by BESIII and Belle

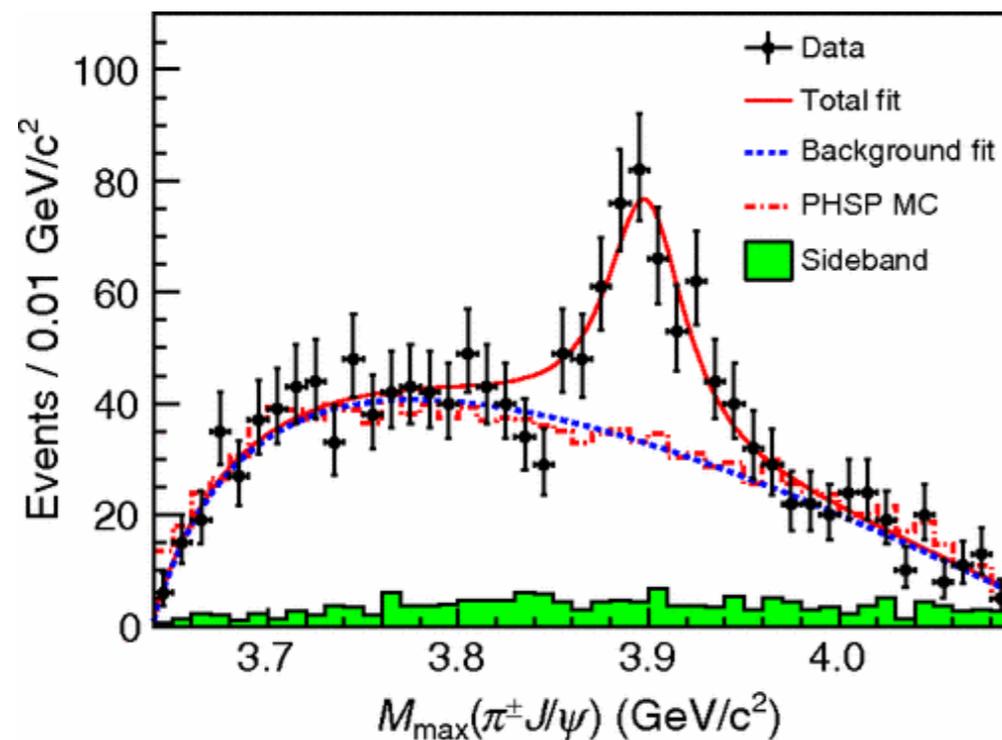
$$M = (3894.5 \pm 6.6 \pm 4.5) \text{ MeV}/c^2$$

$$\Gamma = (63 \pm 24 \pm 26) \text{ MeV}/c^2$$

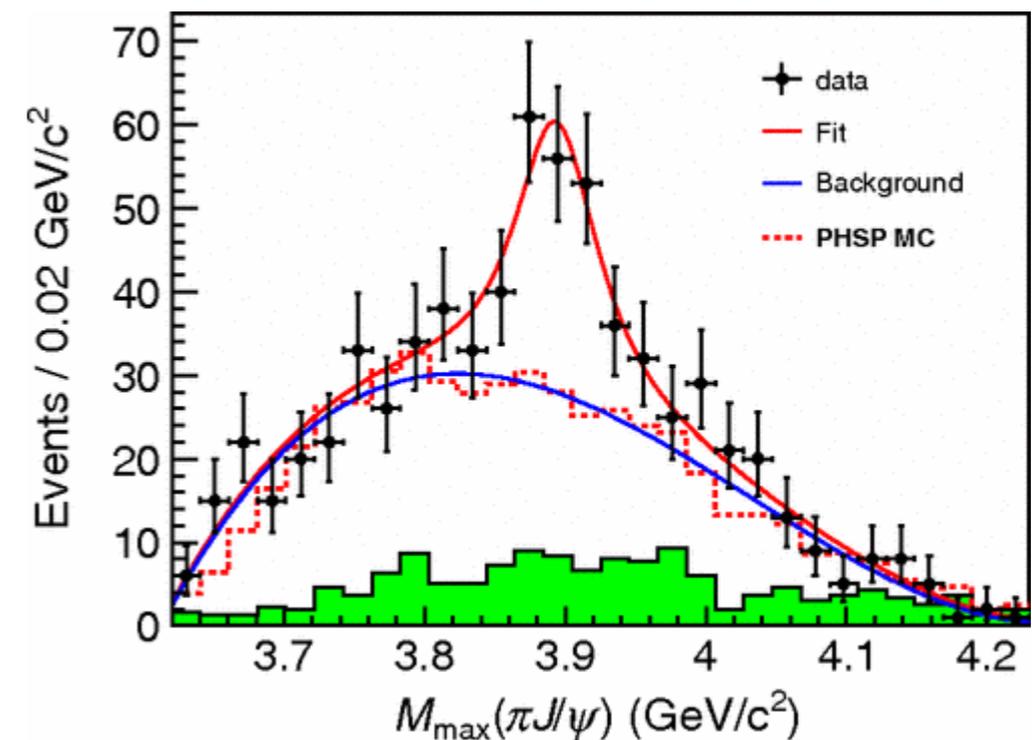
Y(4260)



Phys. Rev. Lett. 110, 252002



Phys. Rev. Lett. 110, 252001

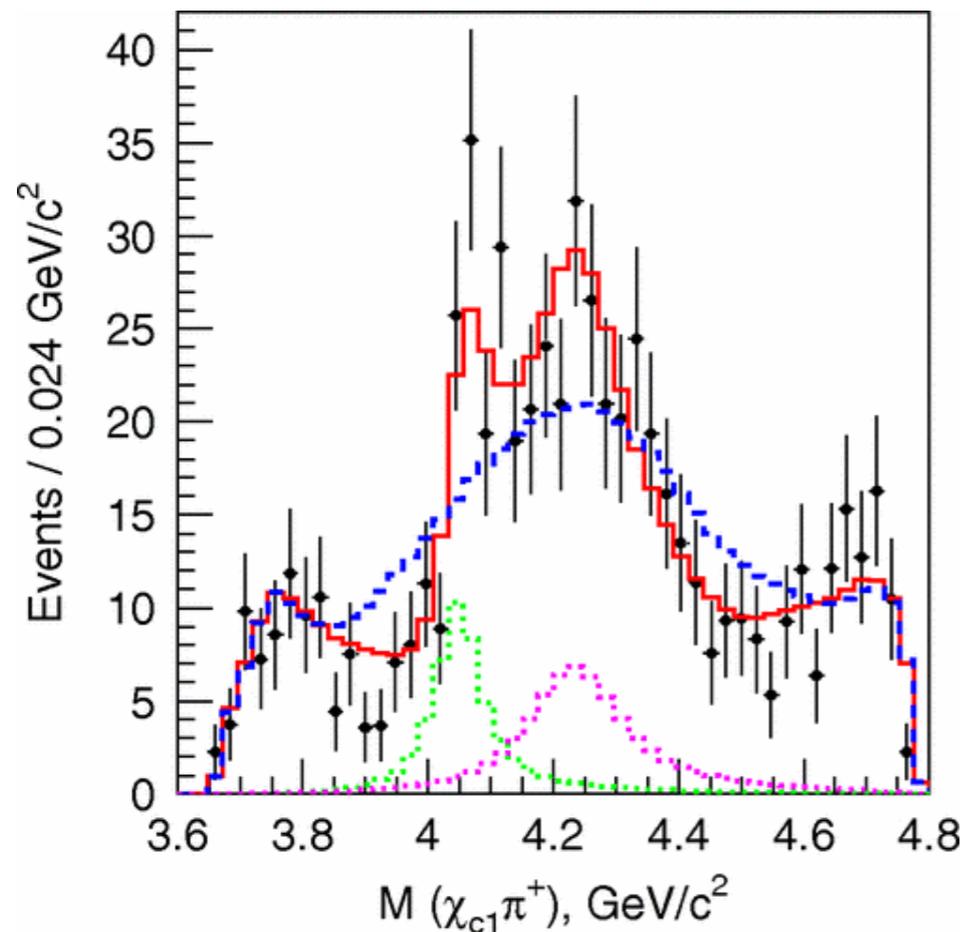


Phys. Rev. Lett. 110, 252002

Other exotic states in quarkonium spectra

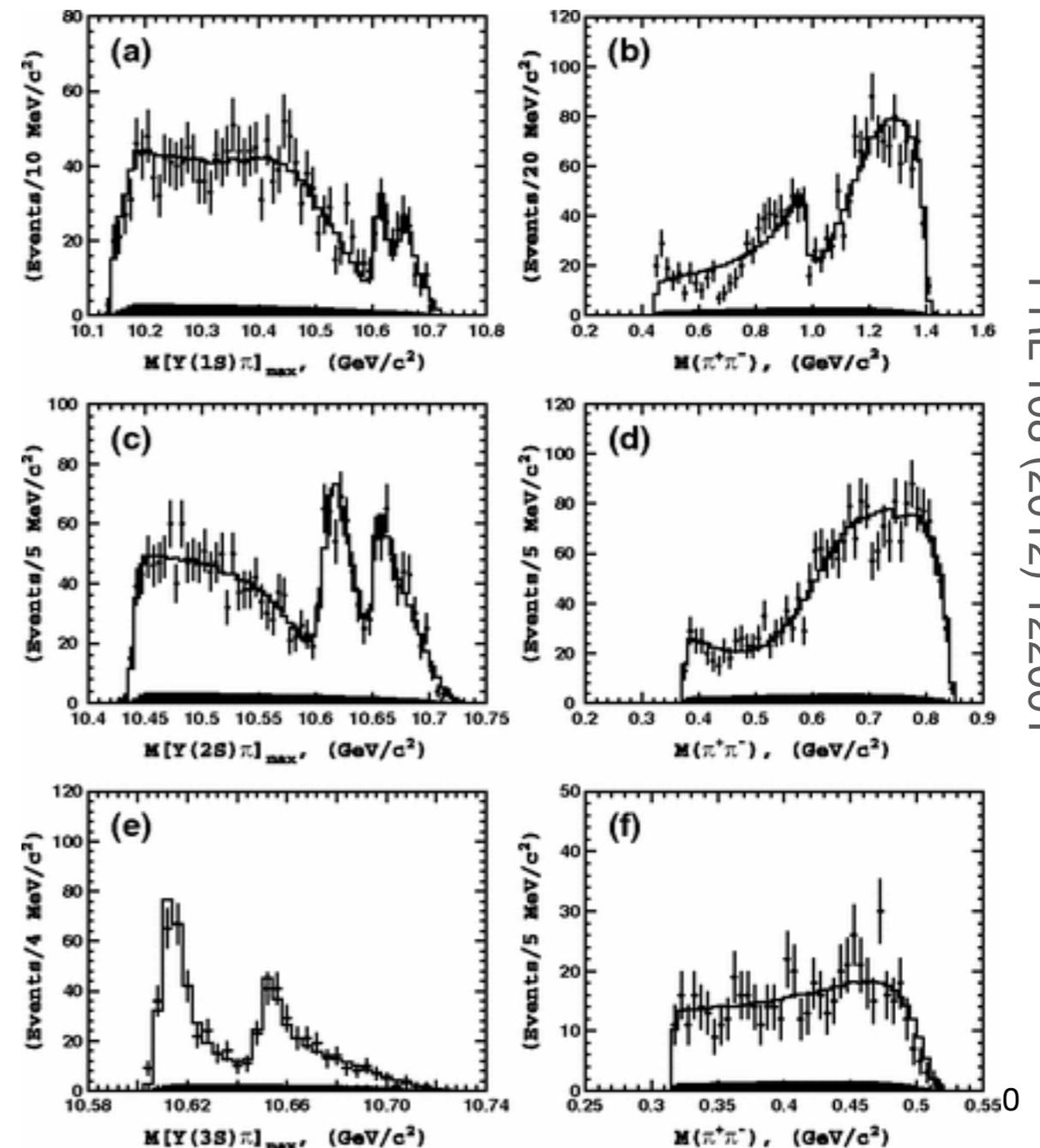
- Belle have evidence for $Z_1(4050)^-$ and $Z_2(4250)^-$ states in $B^0 \rightarrow Z^- K^+$, $Z^- \rightarrow \chi_{c1} \pi^-$.
- BaBar have not confirmed... Phys. Rev. D 85, 052003

- Also Belle has claimed evidence for Z_b resonances when looking at $b\bar{b}$ spectrum.



PRD 78 (2008) 072004

LHCb should be able to do something here in future



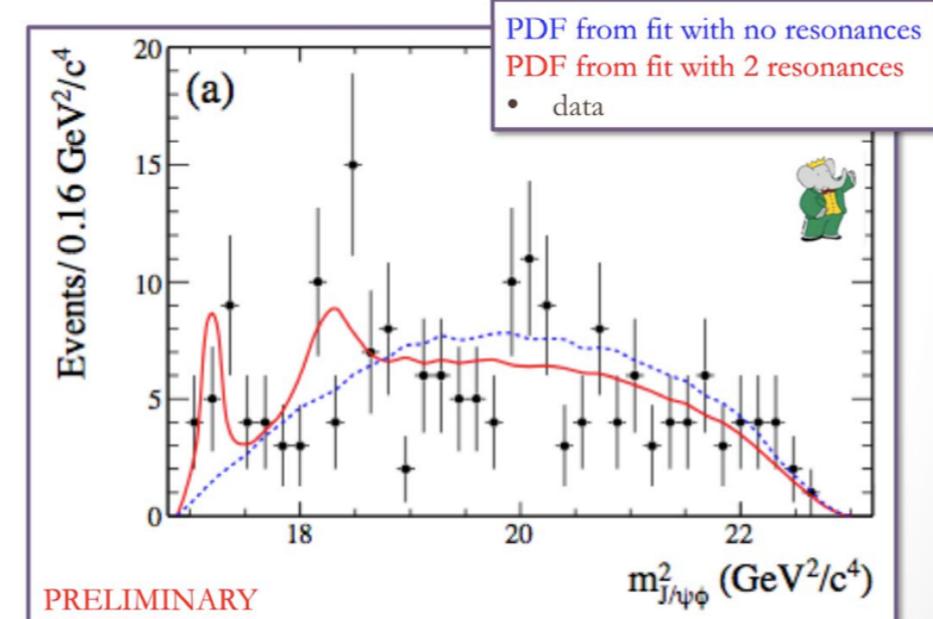
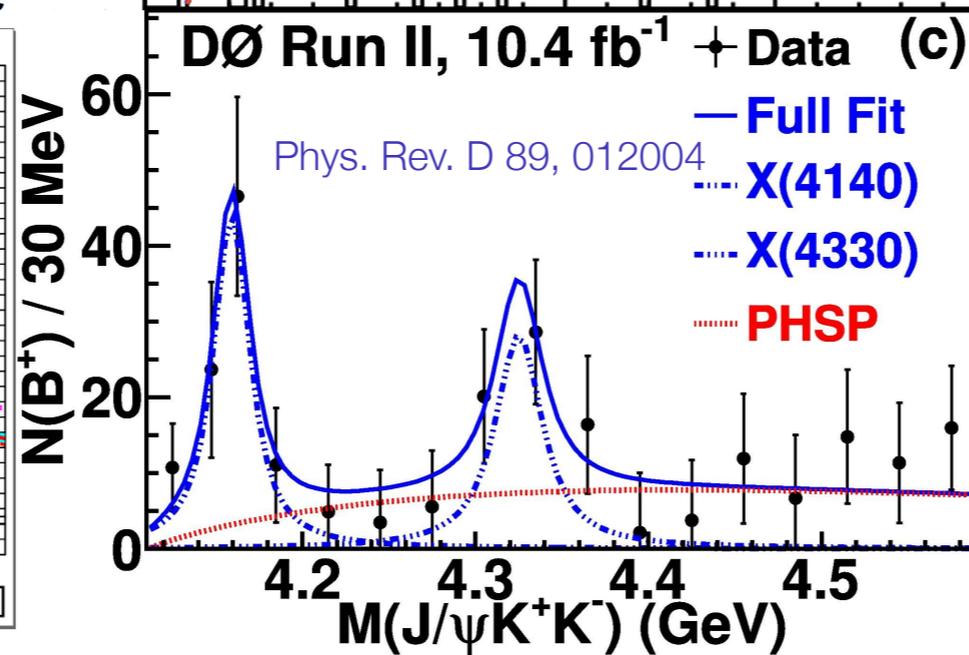
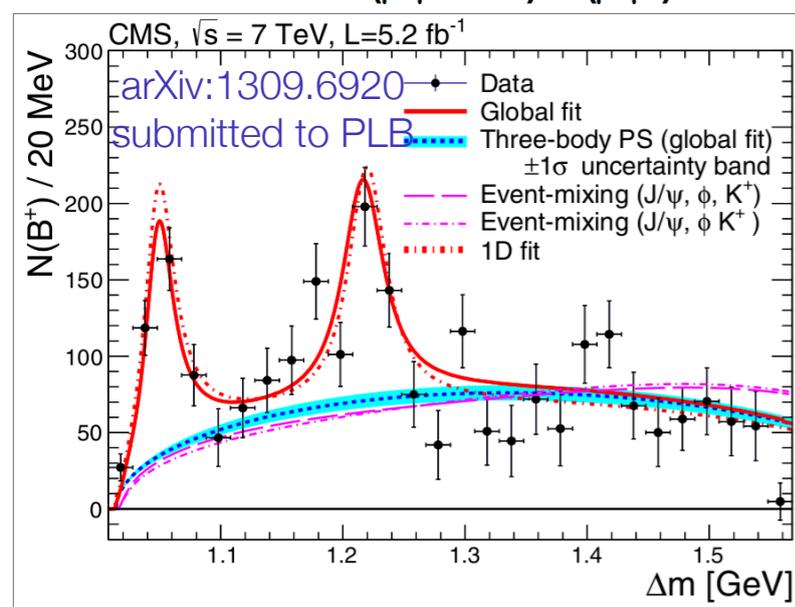
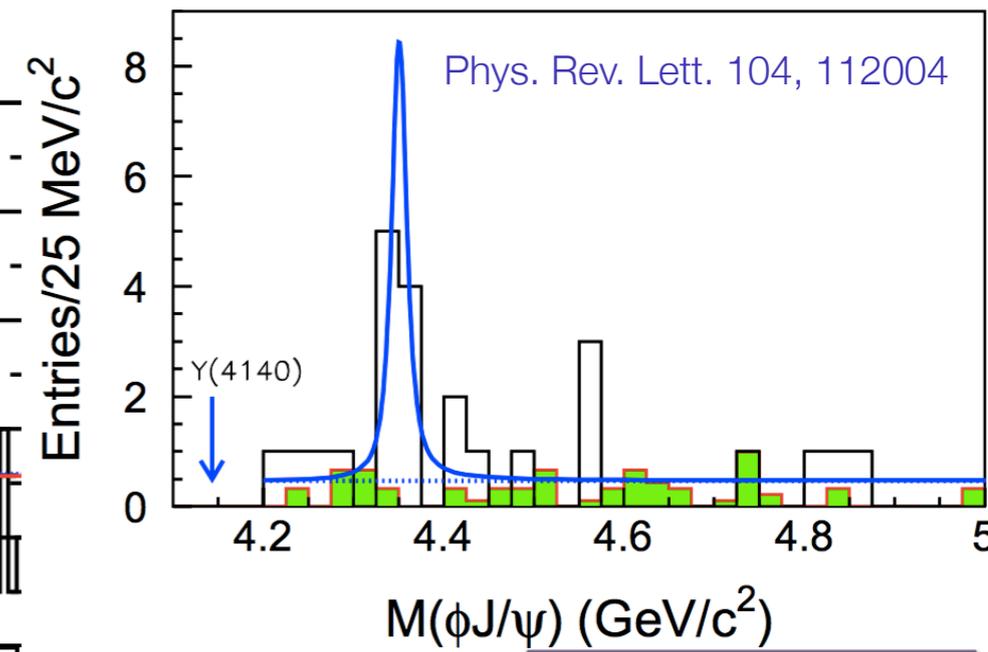
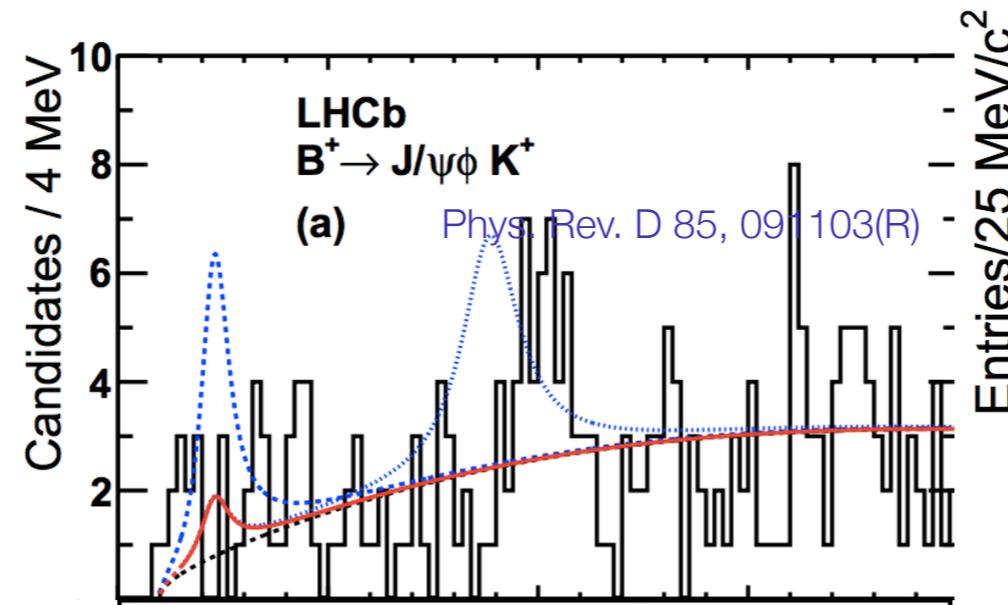
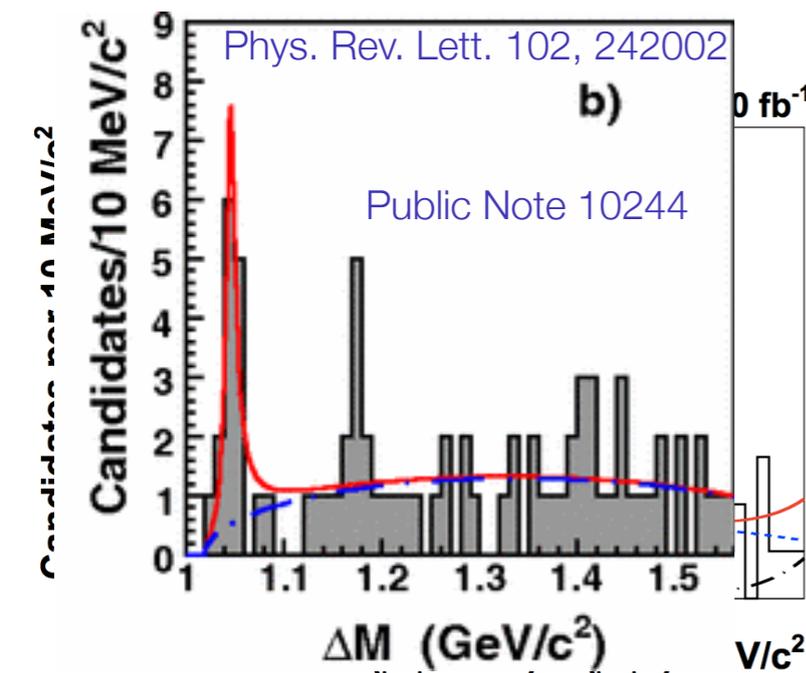
PRL 108 (2012) 122001

An enigma... the X(4140)

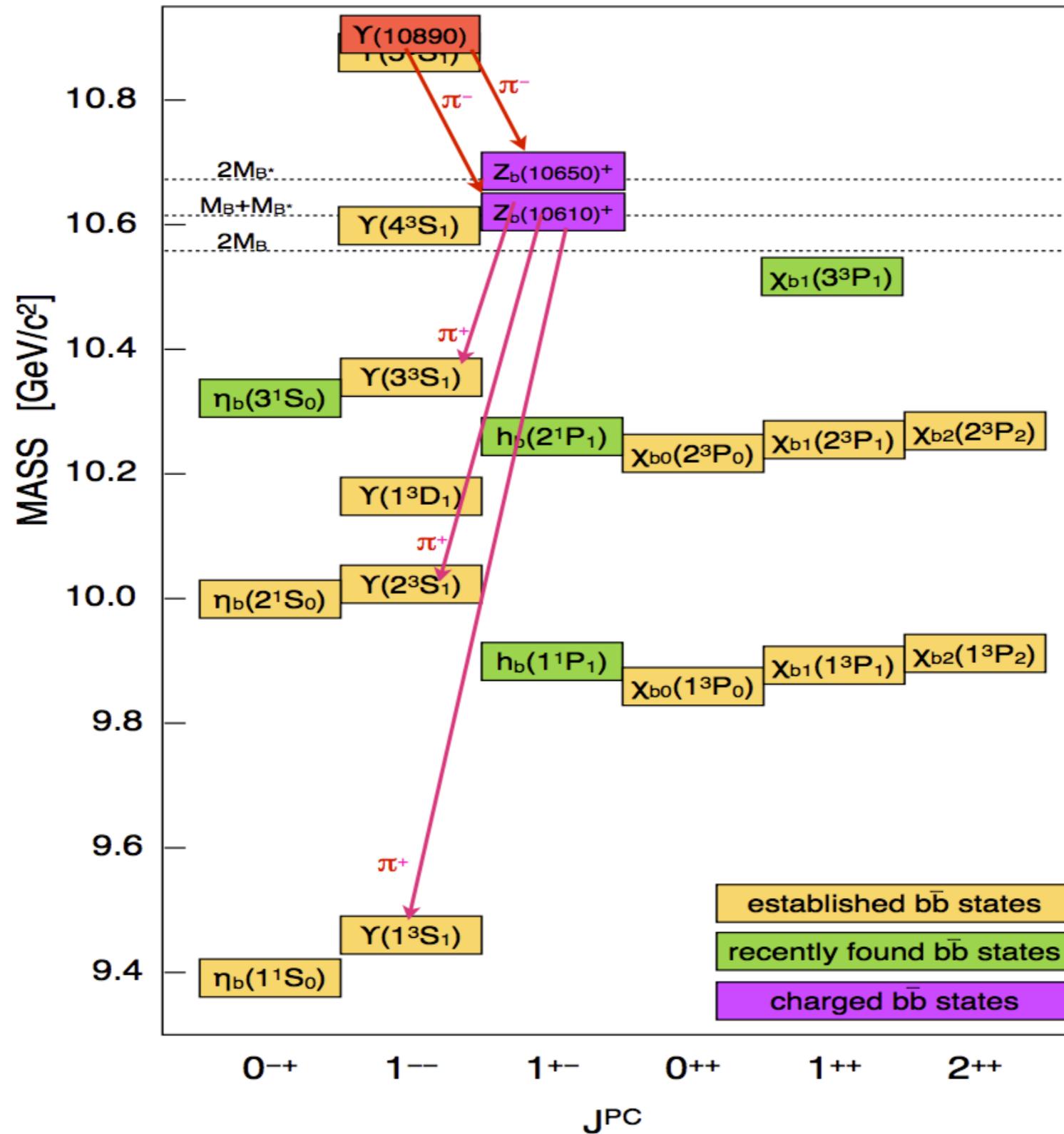
$$B^{\pm/0} \rightarrow XK^{\pm/0}$$

$$X \rightarrow J/\psi\phi$$

- X(4140) seen by some experiments, not by others in $m(J/\psi\Phi)$.
- Could be some hybrid state: $c\bar{c}s\bar{s}$



Bottomonium spectrum



Olsen arXiv:1403.1254

Helicity formalism

- Helicity (λ) is projection of $\bar{\mathbf{J}}$ onto $\bar{\mathbf{p}}$ ($\lambda = -|J| \dots + |J|$)
- $a \rightarrow bc$

$$|\mathcal{M}|^2 \propto \left| A_{\lambda_b, \lambda_c} d_{\lambda_a, \lambda_b - \lambda_c}^{J_a}(\theta) e^{i(\lambda_a - (\lambda_b - \lambda_c))\phi} \right|^2$$

- A is complex helicity coupling
- d are Wigner d -matrices (see tables in PDG)
- θ is helicity angle
- ϕ is azimuthal angle defined by decay plane
 - Dependence drops out unless studying cascade decay like $a \rightarrow bc$, $b \rightarrow de$

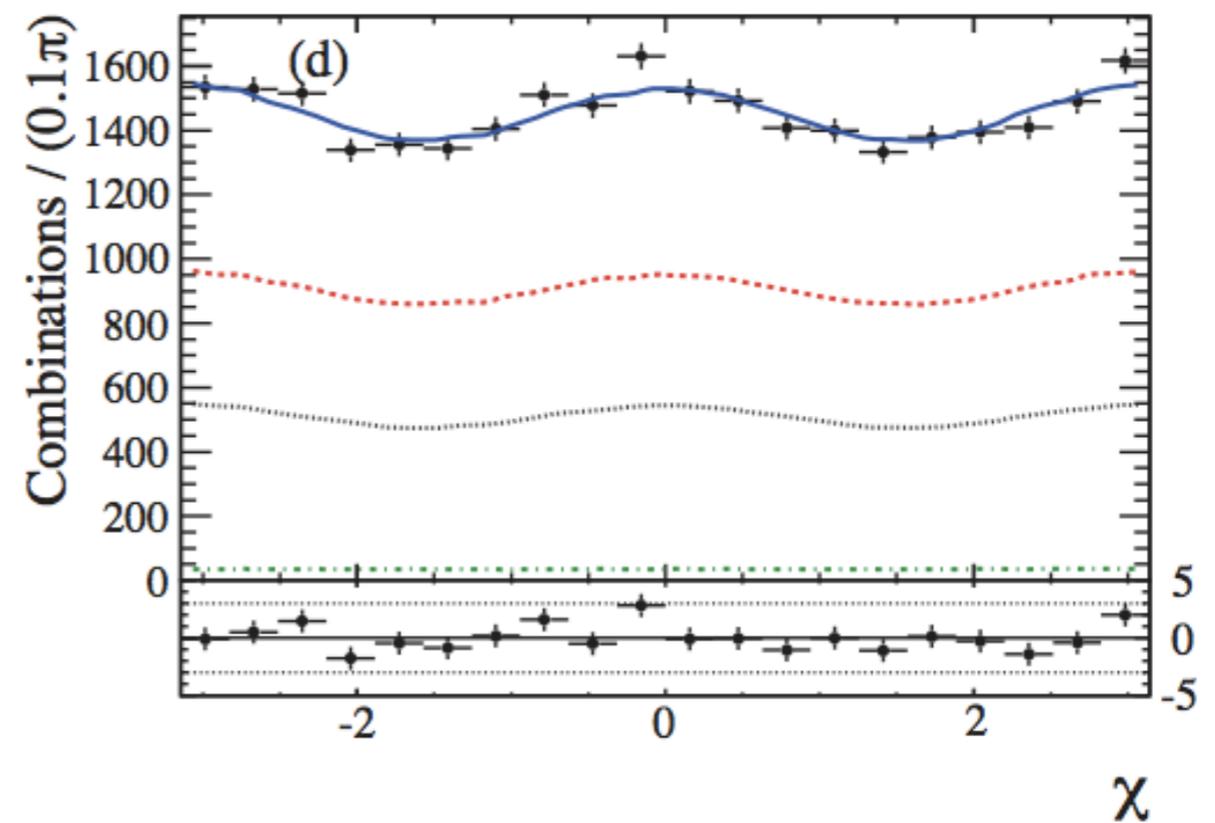
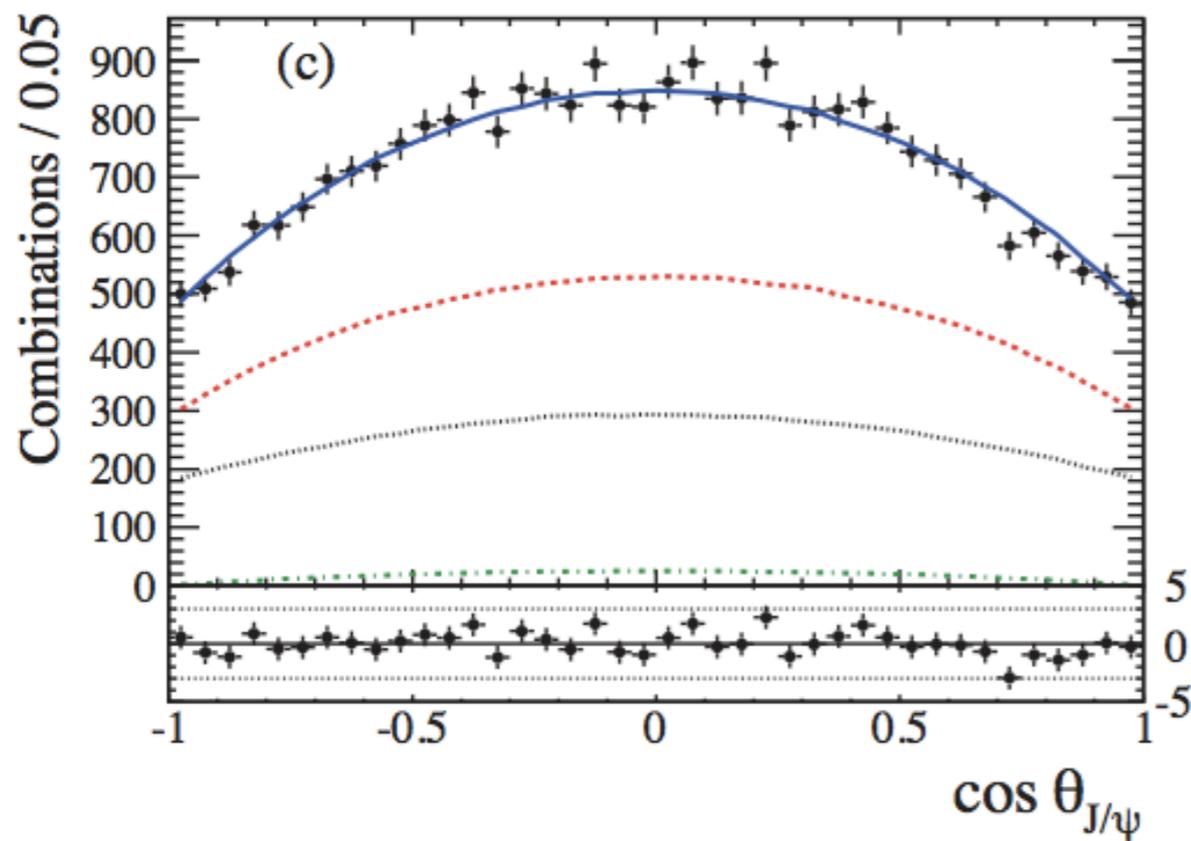
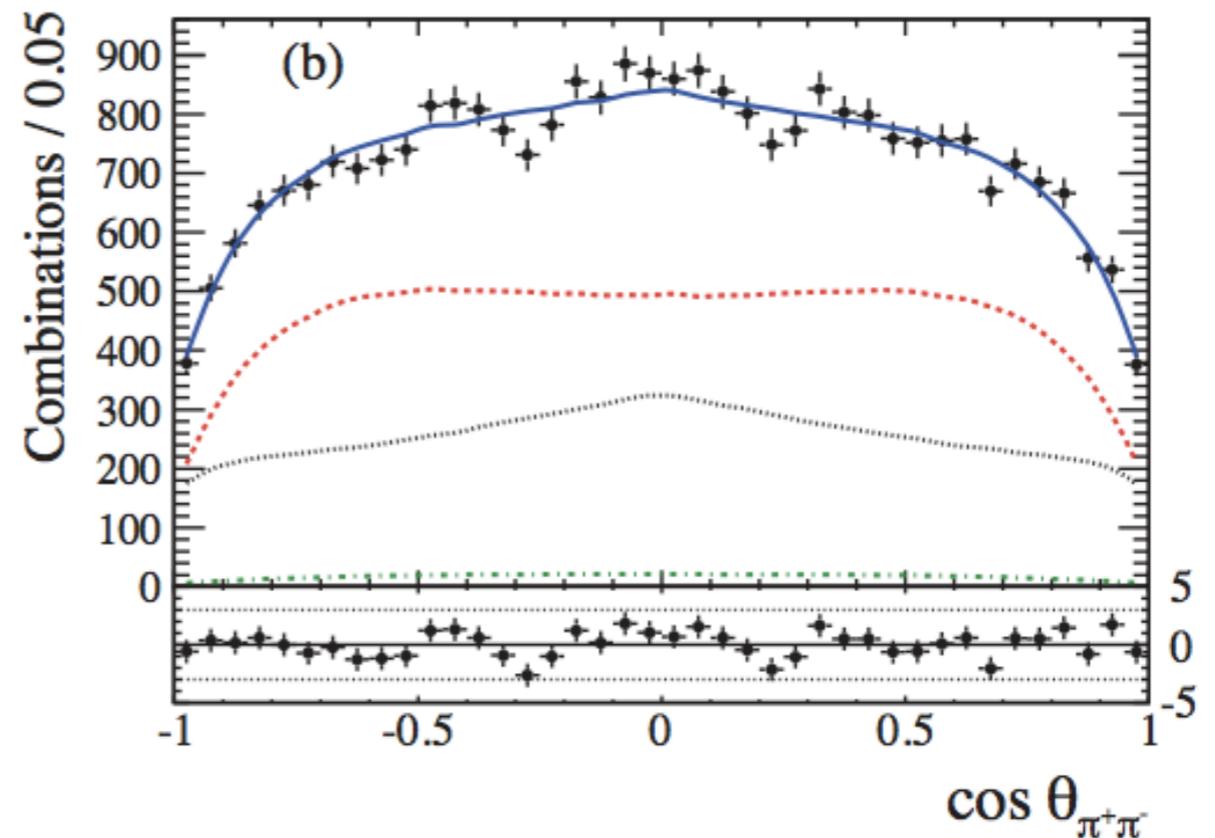
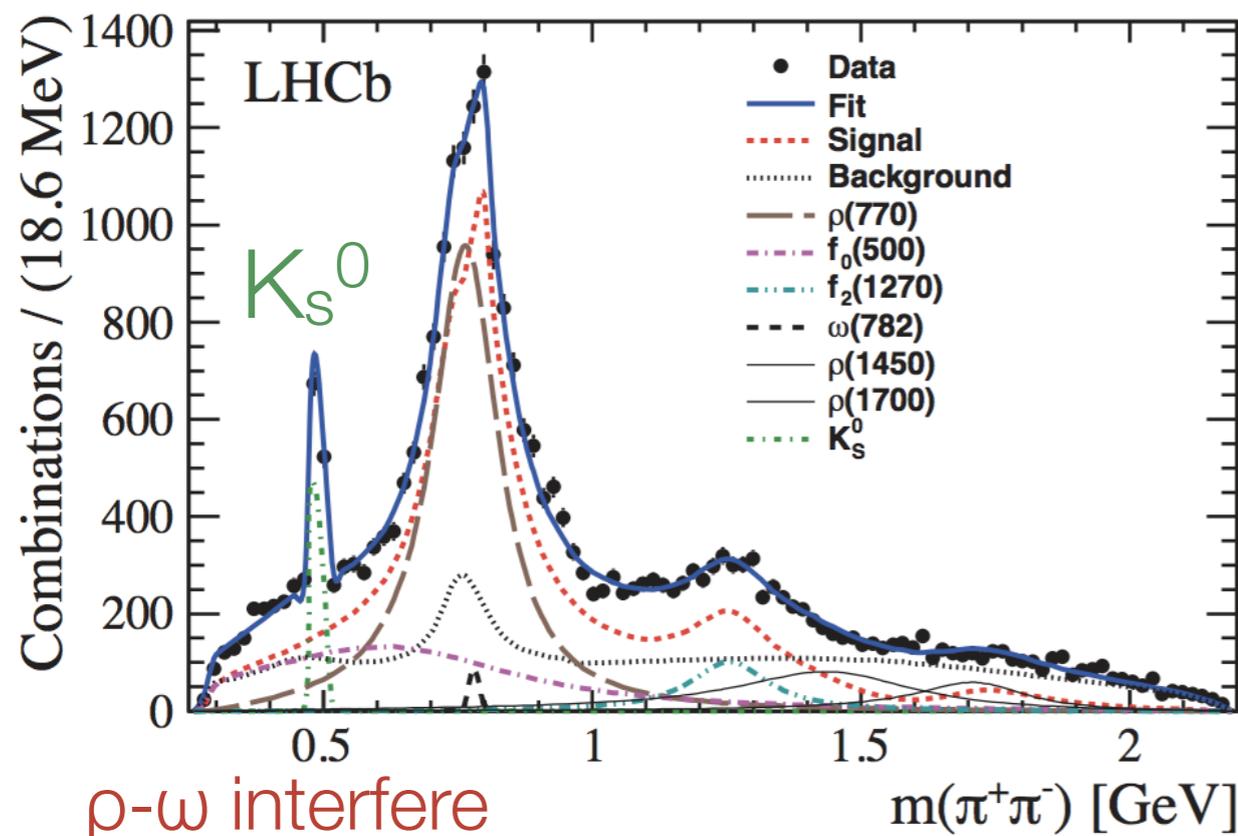
Helicity formalism

- Cascade decays: $a \rightarrow bc$, $b \rightarrow de$
- In this case, need to **coherently sum over helicity of intermediate particle**...
- ...and **sum incoherently over final state particle helicities**.

$$|\mathcal{M}|^2 \propto \sum_{\lambda_c} \sum_{\lambda_d} \sum_{\lambda_e} \left| \sum_{\lambda_b} A_{\lambda_b, \lambda_c}^a A_{\lambda_d, \lambda_e}^b \dots \right|^2$$

- For $B^0 \rightarrow \psi(2S)K^+\pi^-$
 - B^0 is spin-0, $\lambda_B = 0$
 - $\psi(2S) \rightarrow \mu^+\mu^-$ is EM decay, $\Delta\lambda_\mu = \pm 1$

Amplitude analysis of $B^0 \rightarrow J/\psi \pi^+ \pi^-$



References

- PDG review on light scalar mesons
- Amsler et al, Physics reports 389 (2004) 61-117
- Close <http://arxiv.org/pdf/hep-ph/0204205v3.pdf>
- Polosa et al (Z(4430), tetraquark model) <http://arxiv.org/pdf/1405.1551.pdf>
- Gell-Mann (Schematic model of baryons and mesons) Physics Letters volume 8, number 3 (1964).
- <http://pdg.lbl.gov/2011/reviews/rpp2011-rev-clebsch-gordan-coefs.pdf>