

# WW scattering studies at a Future Linear Collider

A presentation given at the University of Edinburgh - High Energy Physics Group.

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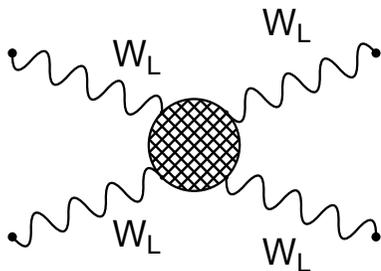


# Outline

- Motivations
  - Physics (why  $WW$  scattering?)
  - Why a FLC?
- Plans for a Future Linear Collider
- $WW$  Scattering Analysis
- Z and W reconstruction
- Results
- Sensitivities
- Conclusions

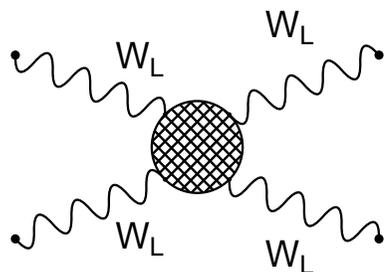
# Motivations

- The mechanism describing how Nature gives mass to particles remains one of the open questions in particle physics today.
- The Higgs Mechanism is the answer in the Standard Model
- If there is no a Higgs, new physics is needed at the TeV scale to restore unitarity
- It is in this context, that the strong scattering of  $W_L W_L$  bosons provides a window to look for information about the underlying symmetry.



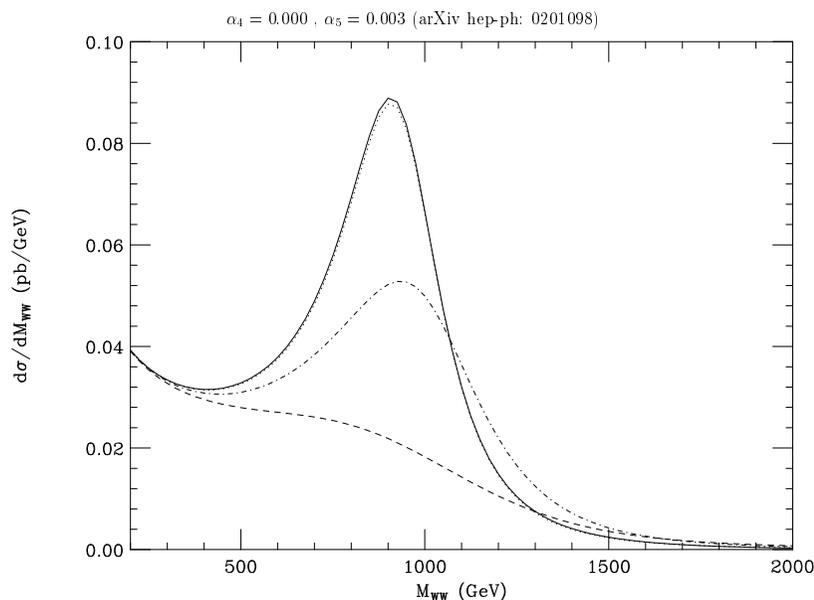
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- It is in this context, that the strong scattering of  $W_L W_L$  bosons provides a window to look for information about the underlying symmetry.
- The EW can be described by the EW Chiral Lagrangian.
- This is an effective theory which:
  - has operators of higher dimensions
  - introduces anomalous couplings
- In particular there are two 4D operators:
$$L_4 = \frac{\alpha_4}{16\pi^2} \text{tr}(V_\mu V_\nu) \text{tr}(V^\mu V^\nu)$$
$$L_5 = \frac{\alpha_5}{16\pi^2} \text{tr}(V_\mu V^\mu) \text{tr}(V_\nu V^\nu)$$
- The coefficients  $\alpha_4$  and  $\alpha_5$  are related to the scale of the new physics ( in the SM these parameters are 0)



# Motivations

- From WW scattering studies at LHC  
(Butterworth, et al - Phys.Rev.D65:096014):
  - EW Chiral Lagrangian
  - Unitarisation protocols
- ▷ Prediction of resonances depending on the values of the  $\alpha_4$  and  $\alpha_5$  parameters
- As an example:



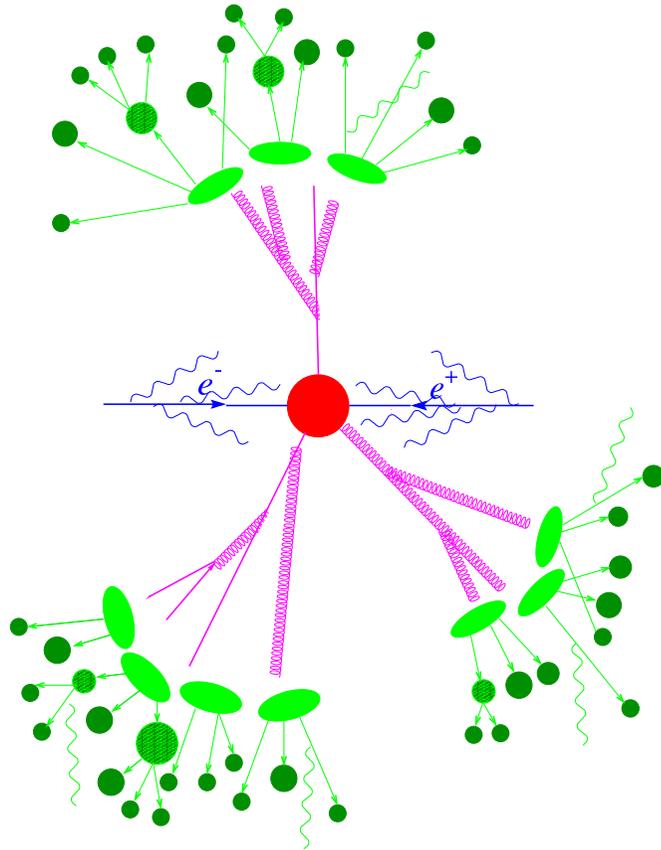
To sum up:

- What's the sensitivity to the  $\alpha_4$  and  $\alpha_5$  that can be reached at a Future Linear Collider?  
Can I improve previous analysis on the subject?  
(Ref: Chierici, et al - LC-PHSM-2001-038)
- Given that these parameters can be measured, what can we learn about new physics at higher energies?  
( LHC - LC complementarity )



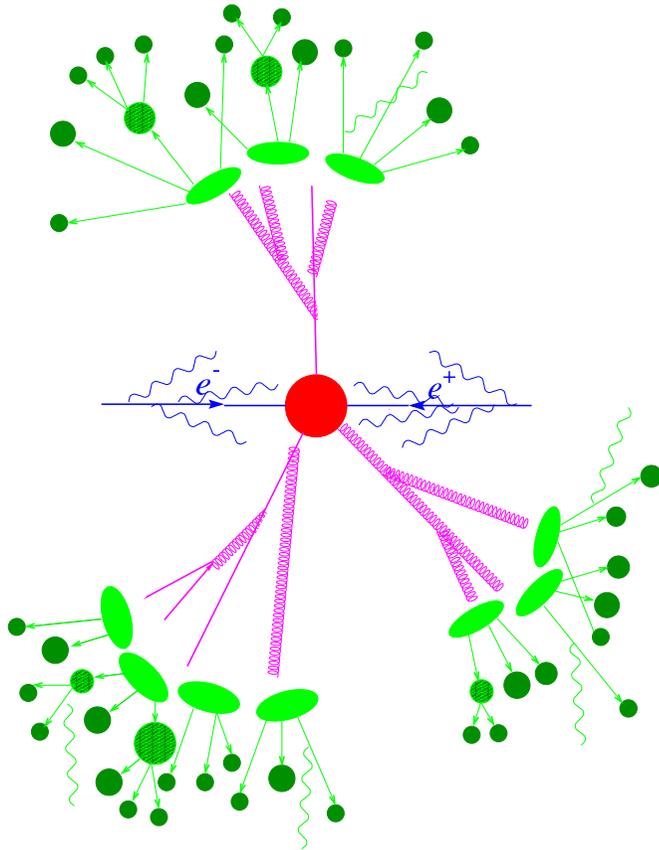
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The LC scenario

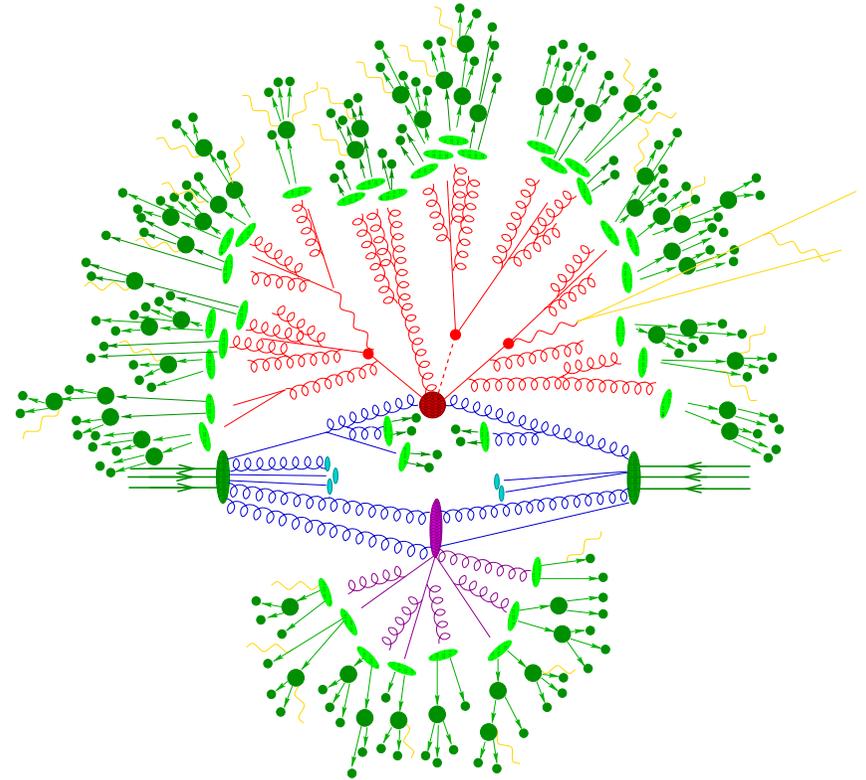


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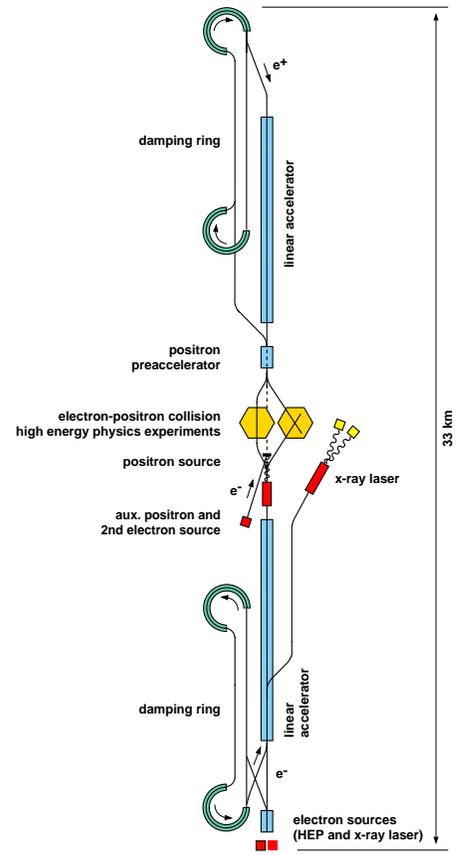
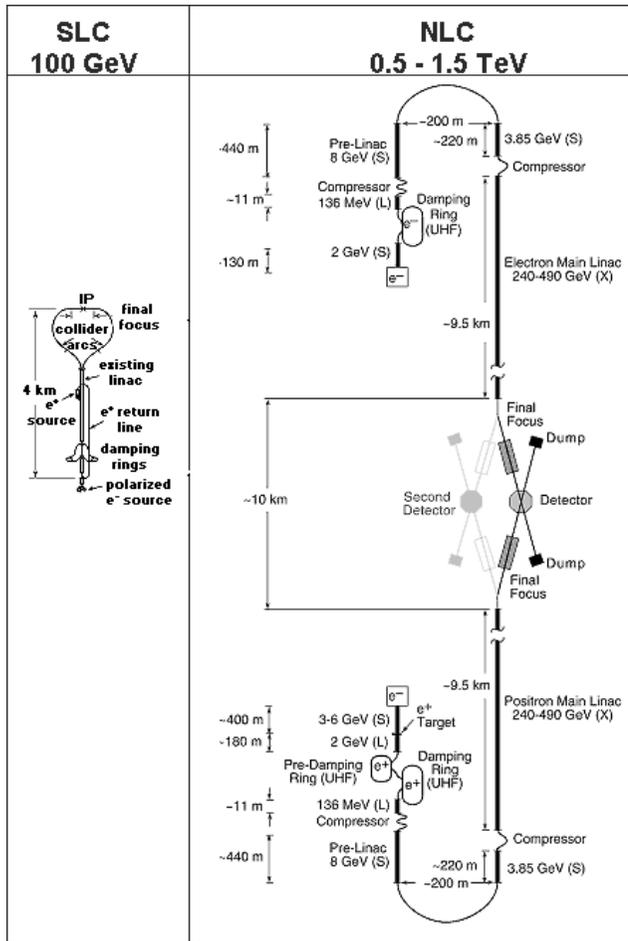


The LHC scenario



# A Future Linear Collider

A global collaboration and project (ILC home page <http://www.linearcollider.org>)



H. Maier 3/2000

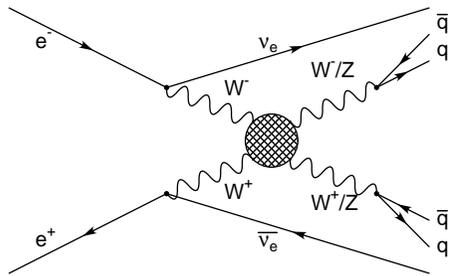


# WW Scattering Analysis

Signal consists of the following processes:

$$e^+e^- \rightarrow \nu\bar{\nu}W^+W^- \rightarrow \nu\bar{\nu}q\bar{q}q\bar{q}$$

$$e^+e^- \rightarrow \nu\bar{\nu}ZZ \rightarrow \nu\bar{\nu}q\bar{q}q\bar{q}$$



● Scenario:  $\alpha_4 = \alpha_5 = 0.0$  (SM) Higgs  $\rightarrow \infty$

● Backgrounds:

$$e^+e^- \rightarrow \nu\bar{\nu}q\bar{q}q\bar{q} \text{ (non-res.)}$$

$$e^+e^- \rightarrow e^+e^-W^+W^-$$

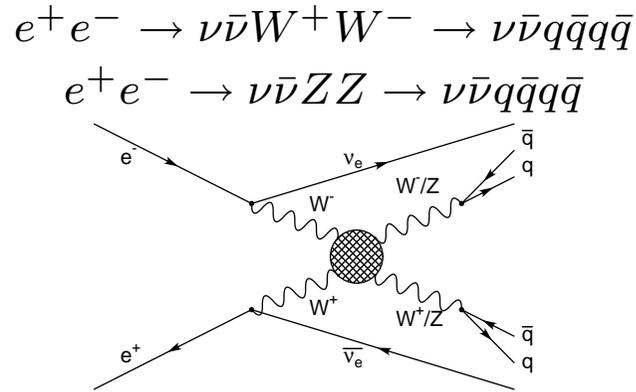
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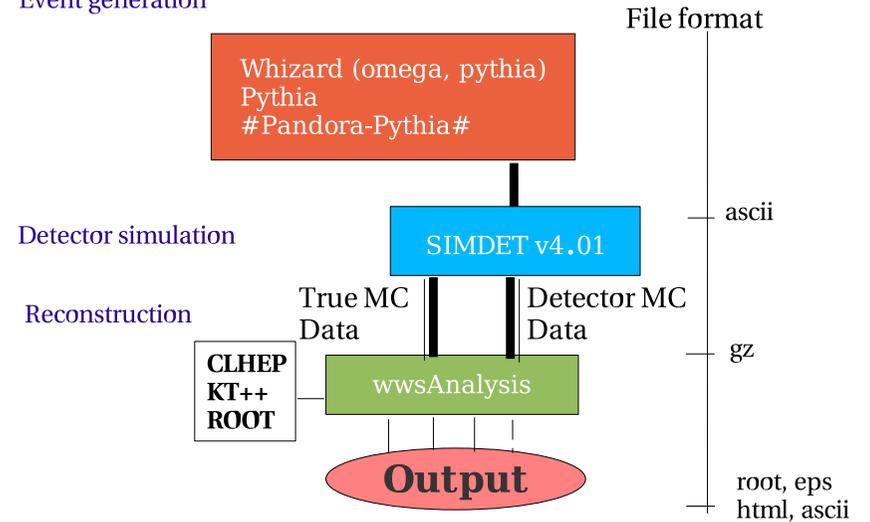
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Framework:  
Event generation



WHiZard 1.29 is the main event generator:

- 6 fermions final states
- all possible quark final states were generated
- need to apply **cuts** to separate signals from other processes
- the anomalous  $\alpha_4$  and  $\alpha_5$  quartic couplings are included
- beam polarisation

# WW Scattering Analysis

- We followed TESLA project specifications:  
(TeV Energy Super-conducting Linear Collider Accelerator)
  - C.M.E.:  $\sqrt{s} = 800 \text{ GeV}$
  - Polarised beams:  
0.80  $e^-$ , 0.40  $e^+$  (PoWER Group)
  - Luminosity:  $\mathcal{L} = 1000 \text{ fb}^{-1}$   
>  $L(10^{34} \text{ cm}^{-2}\text{s}^{-1})=5.8$
- Both ISR and FSR are turned On
- Summary of the cross sections obtained from our study:

Type	Generated process: $e^+e^- \rightarrow$	Cross Sect. [fb]	Generator
6 fermions	$W^+W^-\nu\bar{\nu} \rightarrow q\bar{q}q\bar{q}\nu\bar{\nu}$	9.21	Whizard
	$ZZ\nu\bar{\nu} \rightarrow q\bar{q}q\bar{q}\nu\bar{\nu}$	4.05	Whizard
	$q\bar{q}q\bar{q}\nu\bar{\nu}$ (backgrounds)	6.55	Whizard
	$WZ\nu\bar{\nu} \rightarrow q\bar{q}q\bar{q}\nu\bar{\nu}$	38.50	Whizard
	$e^+e^-W^+W^- \rightarrow e^+e^-q\bar{q}q\bar{q}$	234.80	Pythia*
4 fermions	$W^+W^- \rightarrow q\bar{q}q\bar{q}$	1948.10	Pythia*
	$ZZ \rightarrow q\bar{q}q\bar{q}$	142.90	Pythia*
	$e^+e^-t\bar{t}$	1.30	Pythia*
2 fermions	$t\bar{t} \rightarrow X$	136.90	Pythia *
	$q\bar{q}$	4464.60	Pythia*

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- We used the fast Detector Simulation SIMDET (v.4.01):
  - Tracking system: CCD vertex detector (1.5cm) + Forward Tracker
  - Magnetic field: 4 T
- Calorimetry:
  - ECal resolution:  $\Delta E/E = 0.2/\sqrt{E}$
  - HCal resolution:  $\Delta E/E = 0.5/\sqrt{E}$
- 3D cells - good granularity -> Energy Flow concept.

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# Z and W reconstruction

Main problem is to reconstruct Z and W **pairs**

- Objects from the detector simulation are forced into 4 jets using the  $K_T$  jet algorithm  
- exclusive mode, E recomb. scheme
- If succeed, we then have 3 possible combinations

- Use a 1C Kinematic Fit to find the best pair option

$$Q(\vec{x}, \vec{\lambda}) = (\vec{x} - \vec{x}_0)V^{-1}(\vec{x} - \vec{x}_0) + 2\vec{\lambda}\vec{f}(\vec{x})$$

- Where:  $\vec{f}(\vec{x})$  : constraints

$\vec{x}$  : jet parameters ( $P_{tot}, \theta, \phi$ )

$\vec{\lambda}$  : Lagrange multipliers

$\vec{V}$  : error matrix

Error matrix: resolution functions

$$\sigma_{P_{tot}}(p_q), \sigma_{\theta}(p_q), \sigma_{\phi}(p_q, \theta_q)$$

- 1c :  $M_{jet_1jet_2} = M_{jet_3jet_4}$



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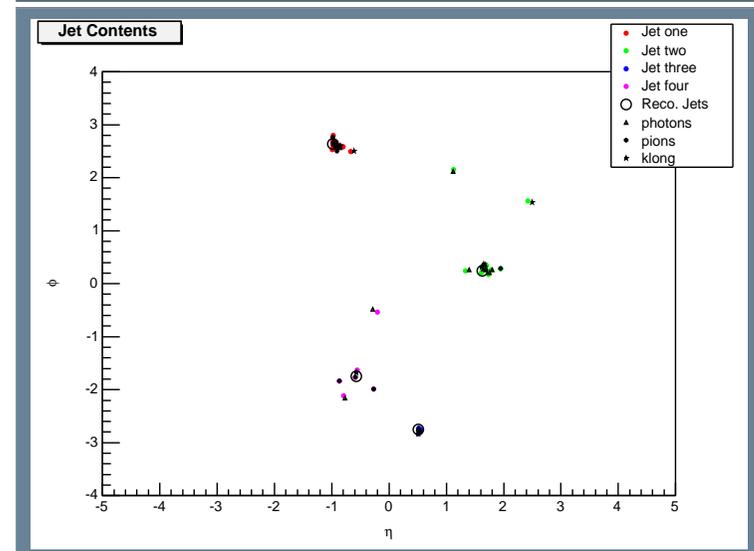
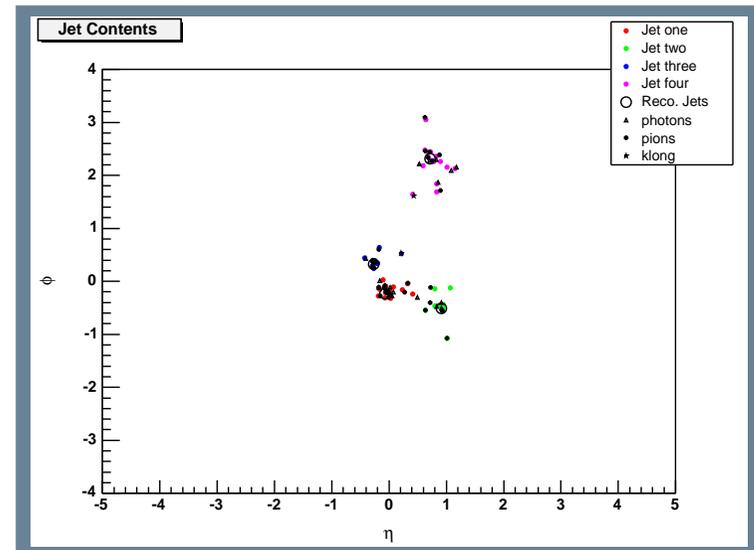
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• Jet configurations



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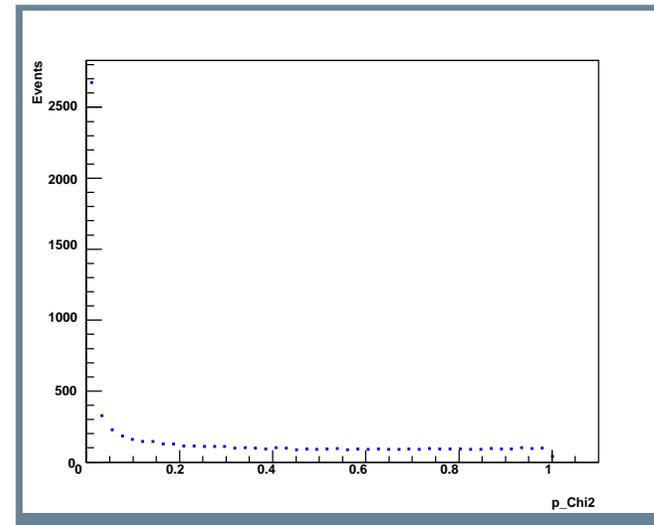
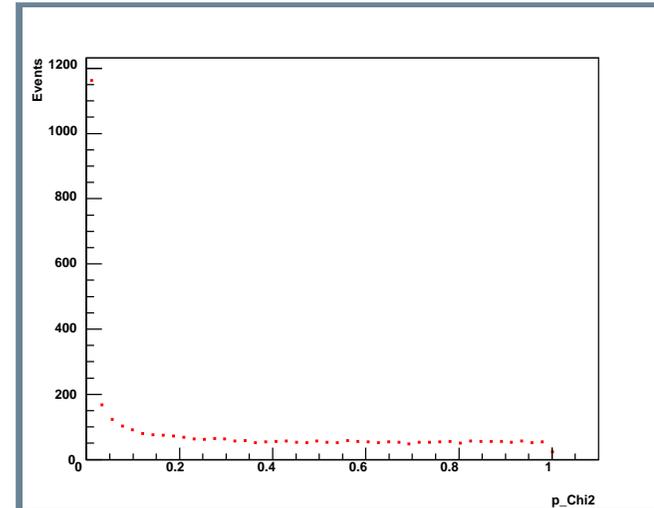
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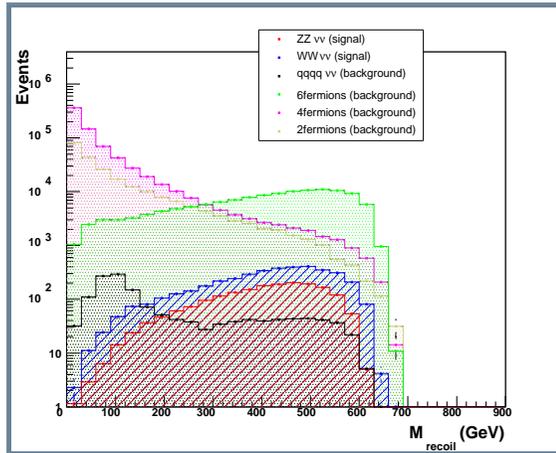
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## • Kinematic Fit results

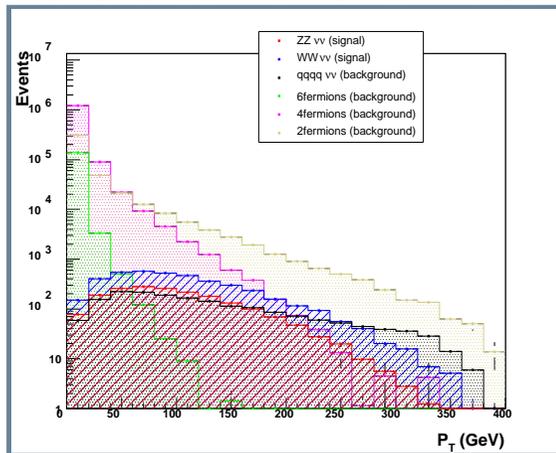


# Z and W reconstruction

## Recoil Mass distribution



## Transverse momentum distribution



## General selection cuts

- Recoil mass:  $M_{recoil} \geq 200$  GeV

- $P_T \geq 20$  GeV

- $E_{trans} \geq 150$  GeV

- Scaled ycut parameter

$$4.0 \leq \ln \sqrt{ycut_{1,2} * s} \leq 7.2$$

- Total missing

$$\text{momentum} | \cos \theta_{P_{miss}} | < 0.99$$

- Most energetic track  $| \cos \theta_{P_{Emax}} | < 0.99$

- Charged tracks in each jet  $nTracks \geq 2$

- Probability ( $\chi^2$ )  $> 0.005$

- Ask for energy around highest track  $\geq 2$  GeV 5 deg cone

## ZZ selection

$$85 < M_{1C} < 100 \text{ GeV}$$

## WW selection

$$75 < M_{1C} < 85 \text{ GeV}$$

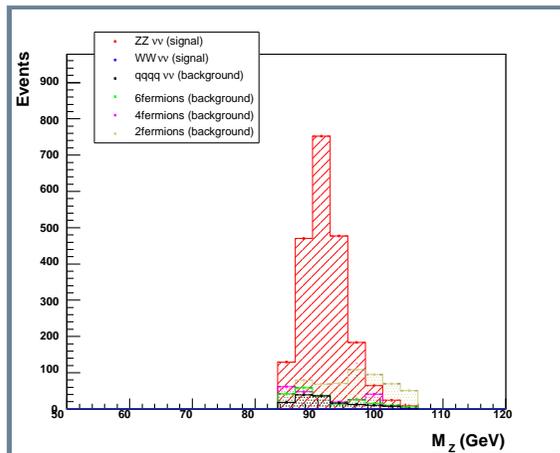
more...



## ● Cut flow summary

Cut flow	Signals		Backgrounds		
	$\nu\bar{\nu}WW$	$\nu\bar{\nu}ZZ$	$q\bar{q}q\bar{q}$	$WZ\nu e$	Other
none	9210	4050	6550	38500	6928600
$M_{recoil}$	7128	3825	1935	49	32815
$P_T$	6863	3664	1860	49	3450
$E_T$	6347	3562	1688	42	2439
$y_{cut}$	6141	3497	1601	42	1890
$\cos\theta_{P_{e_{max}}}$	6133	3493	1595	42	1886
$\cos\theta_{P_{miss}}$	6086	3470	1580	42	1778
Charged tracks	6086	3028	1490	21	1505
$E_{cone}$	5971	2981	1468	9	1244
$P(\chi^2)$	<b>5971</b>	<b>2295</b>	<b>1139</b>	negl.	<b>1047</b>

## ● $\nu\bar{\nu}ZZ$ selection

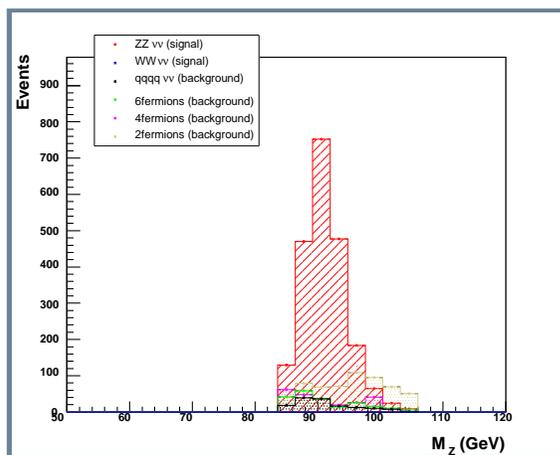


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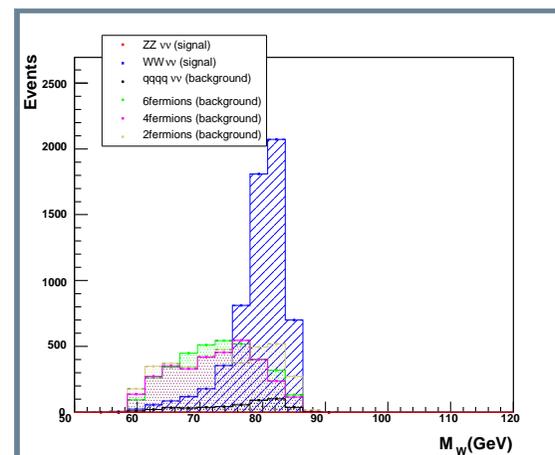
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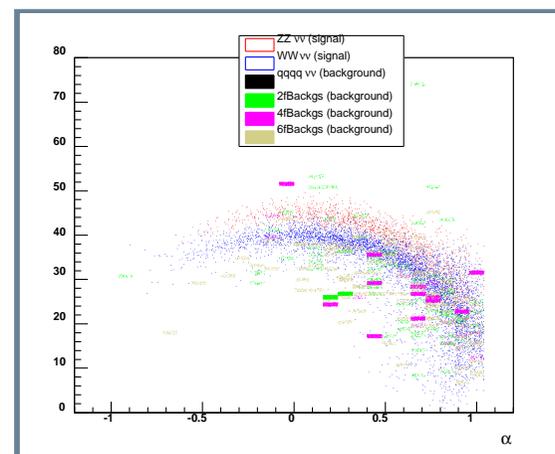
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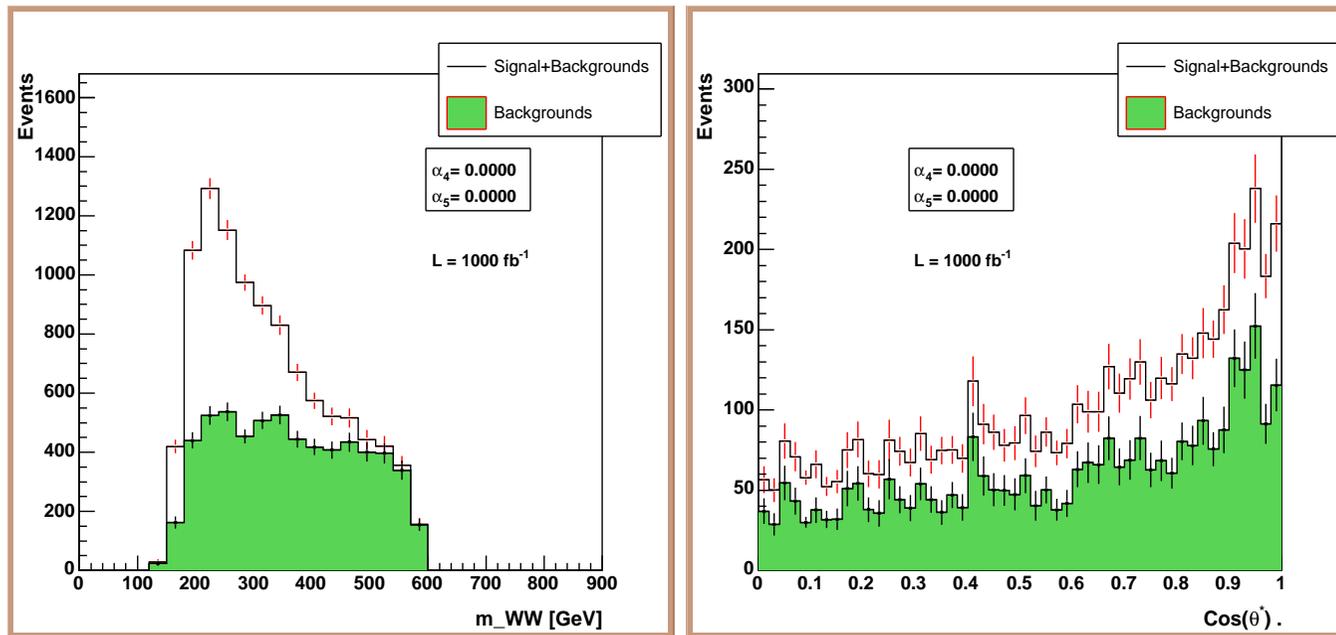
## ● Armentero-Podolanski plot



# Sensitivity study

Now I have Z and W candidates and a working analysis system.  
I combined the pairs of Z and W and make some distributions:

- $M_{WW}$  and  $|\cos \theta^*|$  distribution for  $\alpha_4 = \alpha_5 = 0.0$



What happens when  $\alpha_4$  and  $\alpha_5$  are different from zero?

Expected rate change in the end results and therefore deviations from SM predictions



# Sensitivity study

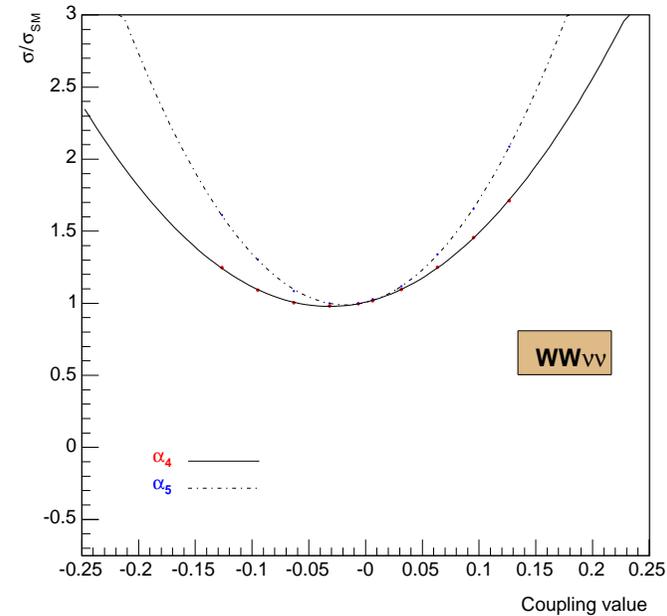
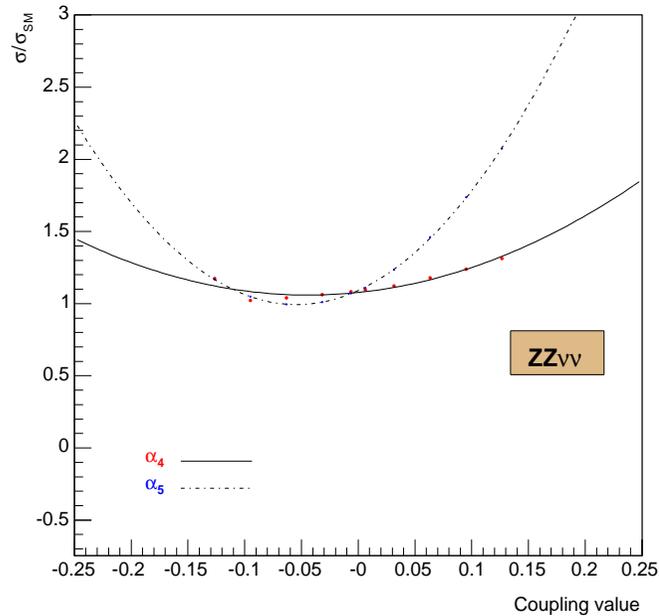
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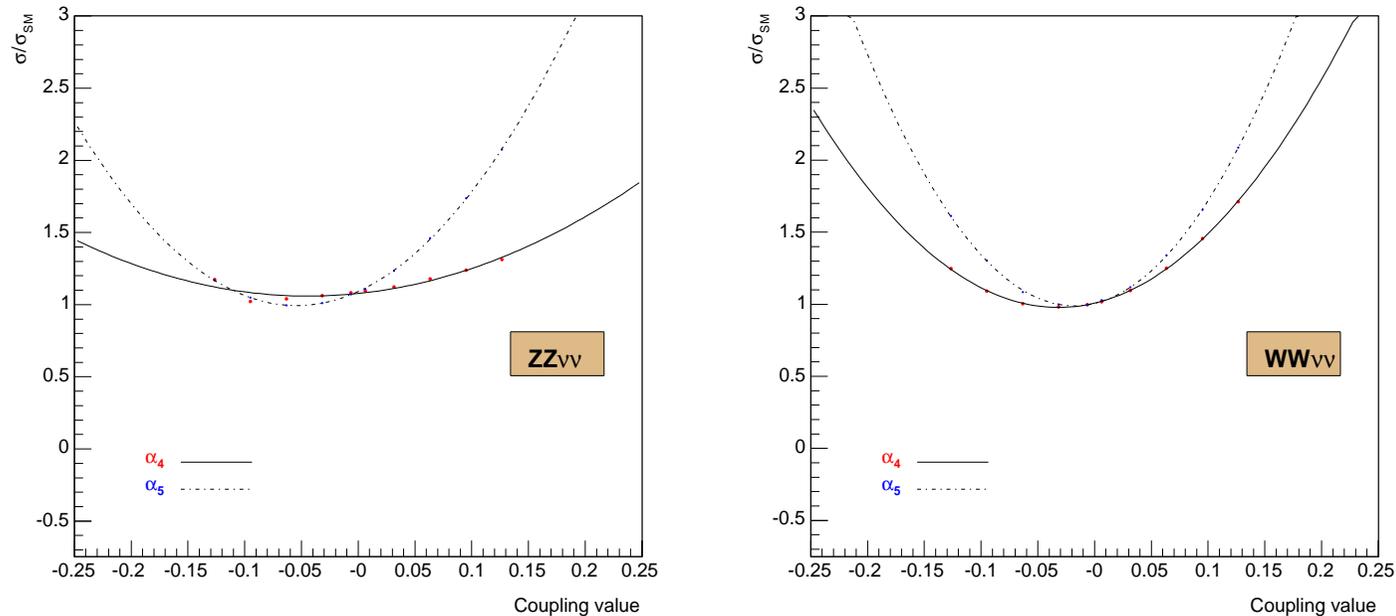
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- We expect better sensitivity to  $\alpha_5$  than  $\alpha_4$  in particular when looking at the  $\nu\bar{\nu}WW$  channel

# Sensitivity study

- Generated 12 extra scenarios with both  $\alpha_5$  and  $\alpha_4$  diff. from zero (each scenario had 400,000 events, enough statistics)

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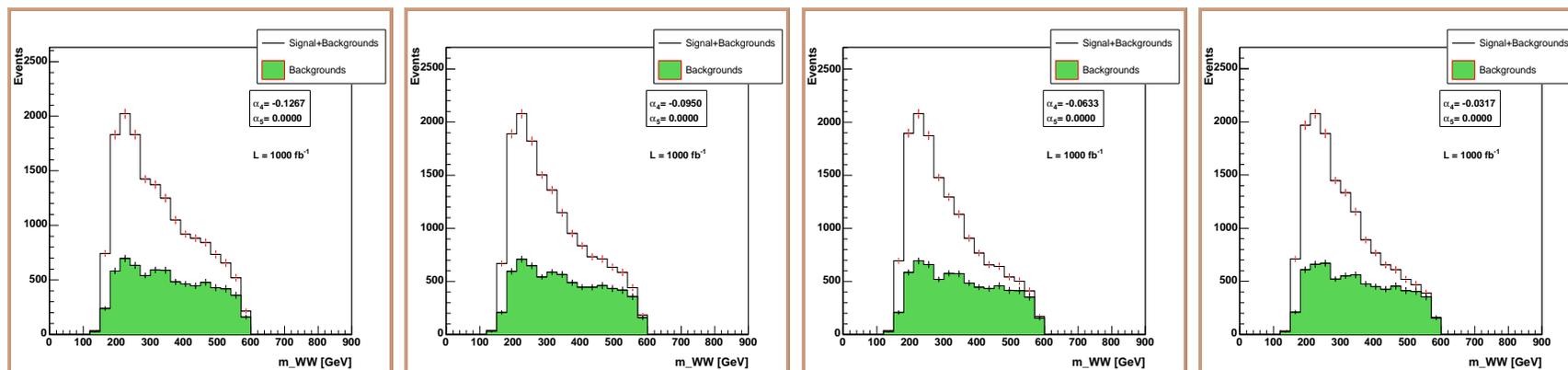
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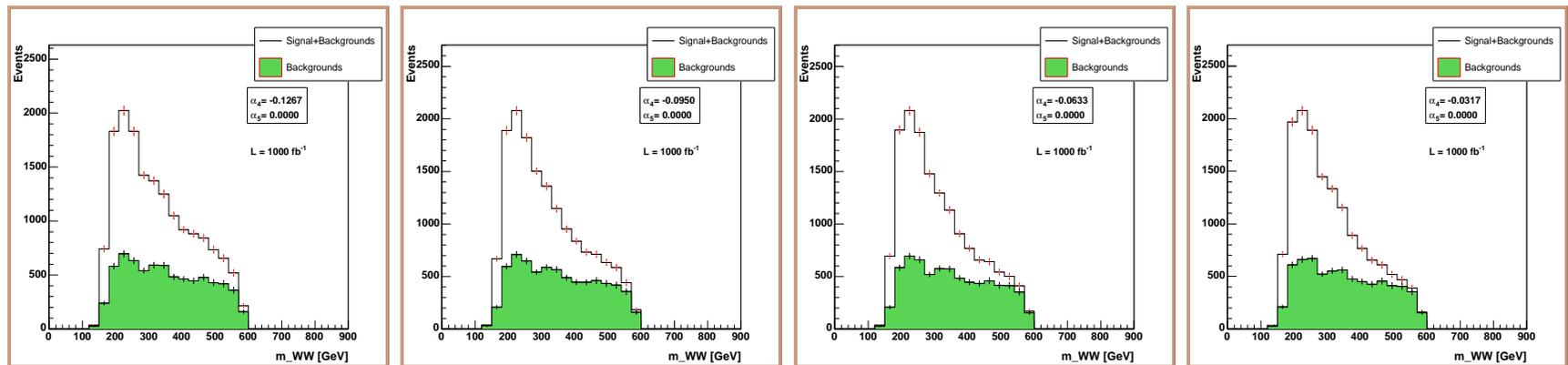
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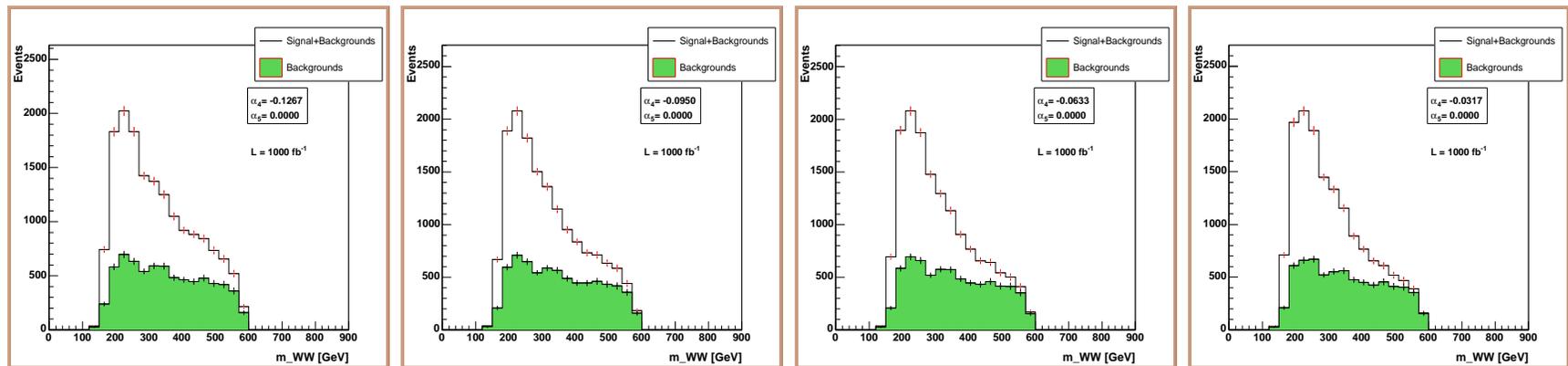
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- BLLH takes as input: SM predicted signal, "observed" events, expected BKG and uncertainties in selection efficiencies, backgrounds and luminosity (not really needed ; = 0.001)

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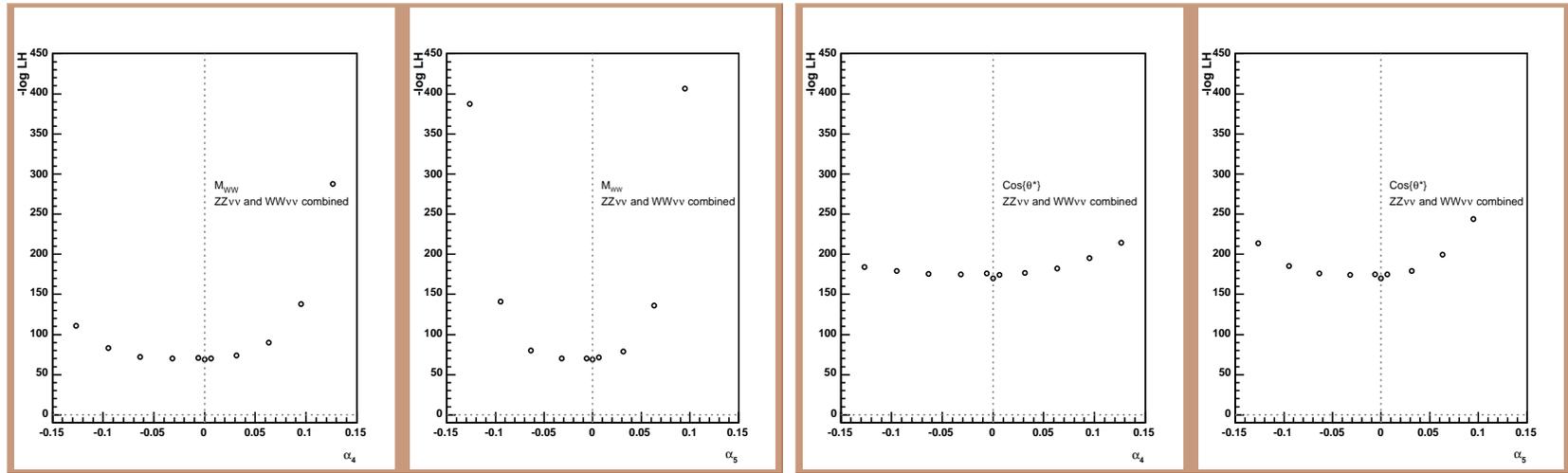
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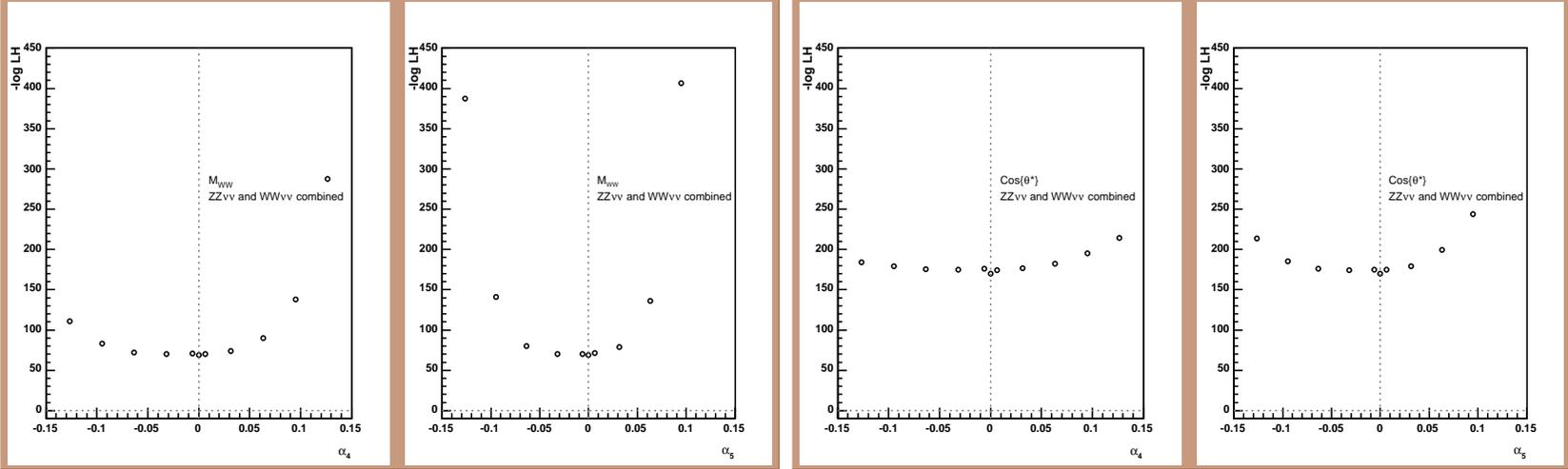
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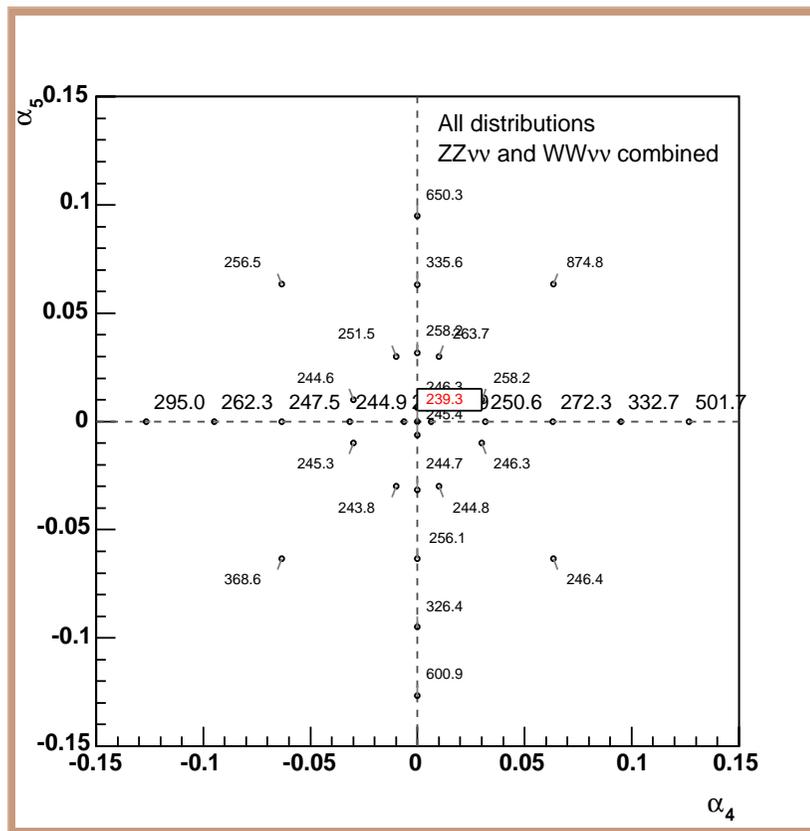


- Observation: no symmetric behaviour of those LLH points with respect to the minimum (SM scenario)



# Sensitivity study

- The combined results for those two distributions are



# Sensitivity study

- Under construction!
- The fit of those LLH values has been more complicated than expected
- At the moment, I'm using S-plines to get a nice fit to those points and extract the limits that I want (and desperately need :) )
- What are the estimated **values**?

# Conclusions

- The hadronic decays of processes

$$e^+e^- \rightarrow \nu\bar{\nu}W^+W^-$$

$$e^+e^- \rightarrow \nu\bar{\nu}ZZ$$

can be exploited to find new physics provided LHC does not find a Higgs boson

- If our ignorance about new physics is parametrised in term of the  $\alpha_4$  and  $\alpha_5$  anomalous couplings, they could be measure at the ILC
- I achieved to write an analysis framework to study hadronic and leptonic decays
  - ▷ It is OO and it would be interesting to see what can do with semi-leptonic decays
- I applied very useful analysis techniques (jet reconstruction, kinematic fit, binned log likelihoods)
- There is progress done on extracting the sensitivity to those anomalous couplings and therefore provide 68/90 percent Confidence Levels

# Conclusions

*If you can look into the seeds of time,  
And say which grain will grow and which will not  
Speak to me.*

*Macbeth, William Shakespeare*

# Extra slide 1

Signal preparation using the following cuts in phase space:

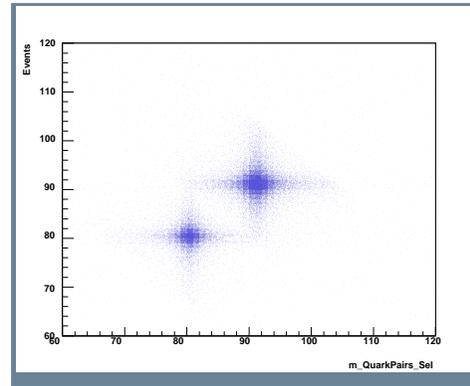
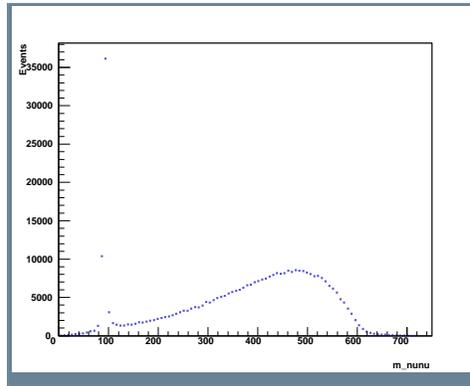
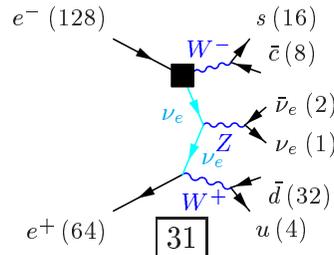
$$147.0 \text{ GeV} \leq m_{q\bar{q}}^1 + m_{q\bar{q}}^2 \leq 171.0 \text{ GeV} : W$$

$$171.0 \text{ GeV} \leq m_{q\bar{q}}^1 + m_{q\bar{q}}^2 \leq 195.0 \text{ GeV} : Z$$

$$|m_{q\bar{q}}^1 - m_{q\bar{q}}^2| \leq 20.0 \text{ GeV}$$

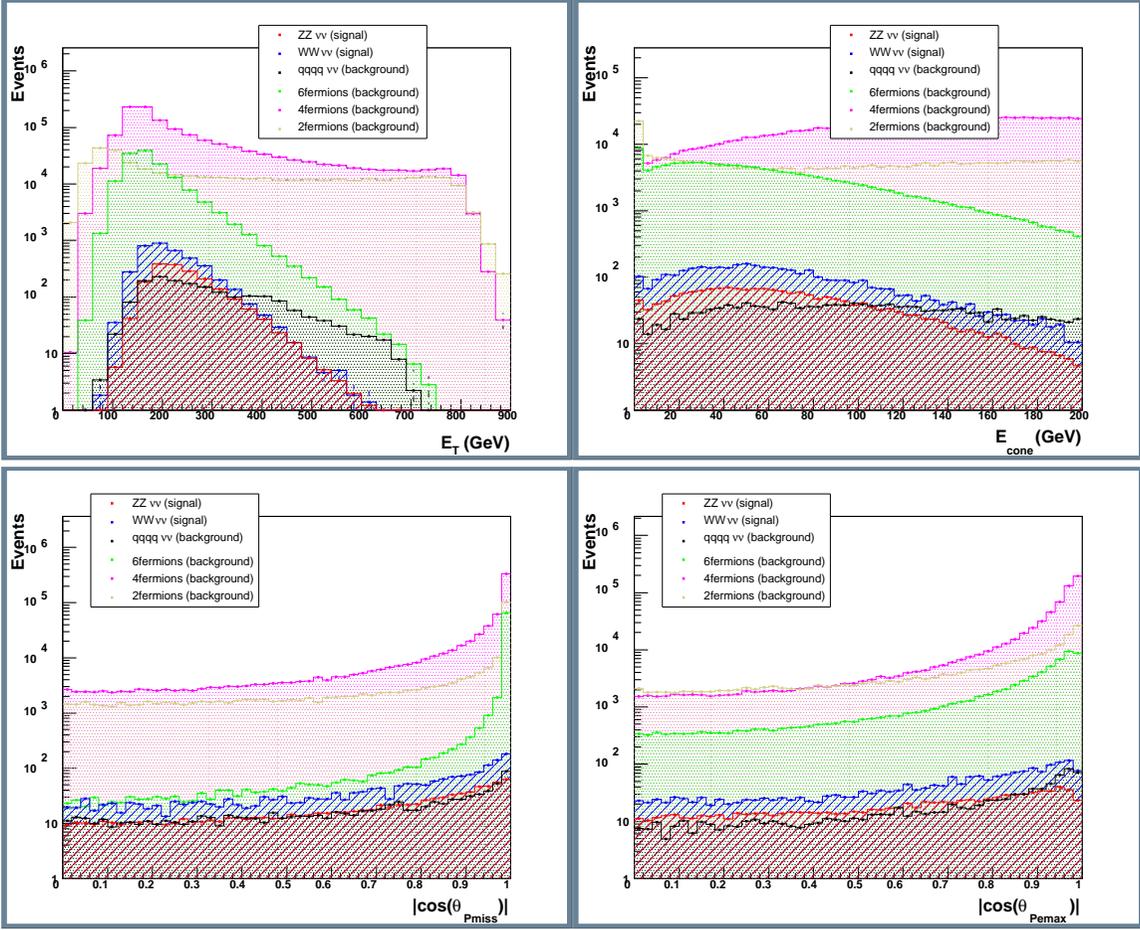
$$m_{\nu\bar{\nu}} \geq 100.0 \text{ GeV}$$

Multiplicity: 3  
 Resonances: 3  
 Log-enhanced: 2  
 t-channel: 2



# Extra slide 2

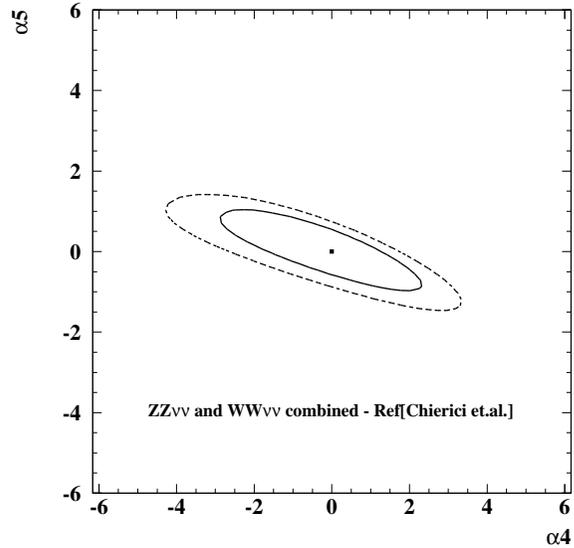
More distributions:



# Chierici et al results

Previous results:

- Confidence Levels contours



- Sensitivities (1 dimensional limits)

1 DIM analysis	68% C.L. (TESLA 1000 fb <sup>-1</sup> 800 GeV and polarisation)	
$\alpha_4$	$\sigma_- = -1.1$	$\sigma_+ = 0.8$
$\alpha_5$	$\sigma_- = -0.4$	$\sigma_+ = 0.3$

- My preliminary results
  - ▷ using a polynomial fit

- Sensitivities (2 dimensional limits)

2 DIM analysis	68% C.L. (TESLA 1000 fb <sup>-1</sup> 800 GeV and polarisation)	
$\alpha_4$	$\sigma_- = -1.18$	$\sigma_+ = 1.24$
$\alpha_5$	$\sigma_- = -0.95$	$\sigma_+ = 0.96$

