Hard Jets and Higgs Bosons

HEJ: All-Order Perturbative Corrections to Hard Multi-Jet Processes

Jeppe R. Andersen

IPPP, Durham University

Edinburgh, Jan 16 2013

Elements of Proton Collisions

Hard scattering, shower, matching to fixed order multiple interactions, underlying event...

Jets to the rescue!

Multi-Jet Predictions

Why we **must** care about HO corrections (in some situations)... A new approach to multiple, wide-angle emissions from the **hard scattering**:

High Energy Jets

Merging with shower. Predictions for dijets, W+jets, H+jets,...

Theory vs. Data

Results of **first data** compared to HEJ Hard, higher order effects beyond NLO

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Hard Jets and Higgs Bosons

A Real pp-Collision



$$Z \to \mu^- \mu^+ + 3$$
 jets

Run Number 158466, Event Number 4174272 Date: 2010-07-02 17:49:13 CEST



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Hard Jets and Higgs Bosons

The Theoretical Description, I*)



*) Drawing by R. Corke

The Theoretical Description, II*)



*) Drawing by R. Corke

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The Theoretical Description, III*)



Drawing by R. Corke

Depending on the question we want to answer, we **may not need** to describe all the **stages of the collision**.

The notion of jets allow us to **compare pure perturbation theory** (few partons) to **experimental observation** (many hadrons)

Transverse Momentum Rapidity: $y = \ln \frac{E+p_z}{E-p_z}$

still need to ensure (relative) insensitivity to underlying event, multiple interactions... ask questions only about relatively hard jets ($p_{\perp} > 30$ GeV?)



Jet (algorithms) to the Rescue!

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still need to ensure (relative) insensitivity to underlying event, multiple interactions... ask questions only about relatively hard jets (p_{\perp} > 30 GeV?)



Obviously need the jet algorithms to be well-defined both experimentally (many discrete hits) and theoretically (probing singularity structure). Use fastjet!

The Perturbative Description



We don't have a choice!

- Many BSM (e.g. SUSY) particles will have *decay chains* involving the production of jets (e.g. 4 jets + p_T). Calculation of signal is easy (one process), SM contribution is very hard (several processes).
- All LHC processes involves QCD-charged particles; sometimes the (n+1)-jet cross section is as large as the n-jet cross section!
- It is a challenge we cannot ignore !

The age old hunt...

Effects beyond NLO DGLAP?

... apart from the obvious soft and collinear regions (shower profile) Do we need more than NLO DGLAP to describe the hard jet events at the LHC?

The News

The data collected in 2010 already show effects beyond **NLO** DGLAP...

- for some observables based on hard jets
- in certain regions of phase space

Scope of this talk

Will not discuss several interesting effects:

- jet broadening (shower profiles)
- impact of underlying event on the jet energy

These are (well?) described by a tunable shower MC.

Will instead focus on the description of the **hard event**, and in particular on observables not well described by **NLO** DGLAP.

Which regions of phase space receive large corrections from hard perturbative corrections (= additional jet activity)

Compare the description of hard jet activity from NLO, NLO+shower, High Energy Jets. Dijets, W+Dijets, H+Dijets; Similarities in Jet Activity

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Multiple (\geq 2) hard jets...

Smaller number of jets solved satisfactory (?) already...(POWHEG, MC@NLO, NNLO,...)

Special radiation pattern from **current-current** scattering Look into **higher order corrections beyond** "inclusive *K*-factor" Concentrate on the **hard, perturbative corrections** relevant for a description of the final state **in terms of jets**.

Goal

Build framework for **all-order summation** (virtual+real emissions). Exact in another limit than the usual soft&collinear. Better suited for describing **radiation relevant for multi-jet** production.

Insight

Can use the insight gained from studying the relevant limit to **guide and improve** analyses: *CP*-properties of the Higgs-boson couplings

- Collinear (jet profile)
- Soft (*p_t*-hierarchies)

 Opening of phase space (semi-hard emissions - not related to a divergence of |M|²). Think (e.g.) multiple jets of fixed p_t, with increasing rapidity span (span=max difference in rapidity of two hard jets=∆y).
 All calculations will agree that number of additional jets increases - but the amount of radiation will differ (wildly) - e.g. due to limitations on the number (NLO) or hardness (shower) of additional radiation allowed by theoretical assumptions.



h+dijets (at least 40GeV). Δy_{ab} : Rapidity difference between most forward and backward hard jet

Compare NLO (green), CKKW matched shower (red), and High Energy Jets (blue).

All models show a clear increase in the number of hard jets as the rapidity span Δy_{ab} increases.

J.R. Andersen, J. Campbell, S. Höche, arXiv:1003.1241

Please recall this plot when I discuss the results of the ATLAS study of $\langle N_{\rm jets} \rangle$

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Goal (inspired by the great Fadin & Lipatov)

Sufficiently **simple** model for hard radiative corrections that the all-order sum can be evaluated explicitly (completely exclusive)

but...

Sufficiently accurate that the description is relevant

Factorisation of QCD Matrix Elements

It is **well known** that QCD matrix elements **factorise** in certain kinematical limits: **Collinear limit** \rightarrow enters many resummation formalisms, parton showers....

Like all good limits, the collinear approximation is applied **outside its** strict region of validity.

Will discuss the **less well-studied factorisation** of scattering amplitudes in a different kinematic limit, better suited for describing perturbative corrections from **hard parton emission**

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The Possibility for Predictions of *n*-jet Rates

The Power of Reggeisation



Maintain (at LL) terms of the form

$$\left(\alpha_s \ln \frac{\hat{\mathbf{s}}_{ij}}{|\hat{\mathbf{t}}_i|} \right)$$

to all orders in α_s .

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also guark-anti-guark pairs produced. Approximation of any-jet rate possible.

Universal behaviour of scattering amplitudes in the HE limit:

$$\forall i \in \{2, \dots, n-1\} : y_{i-1} \gg y_i \gg y_{i+1} \\ \forall i, j : |p_{i\perp}| \approx |p_{j\perp}|$$

$$\begin{split} \left| \overline{\mathcal{M}}_{gg \to g \cdots g}^{MRK} \right|^2 &= \frac{4 \ s^2}{N_C^2 - 1} \ \frac{g^2 \ C_A}{|p_{1\perp}|^2} \left(\prod_{i=2}^{n-1} \frac{4 \ g^2 \ C_A}{|p_{i\perp}|^2} \right) \frac{g^2 \ C_A}{|p_{n\perp}|^2} \\ \left| \overline{\mathcal{M}}_{qg \to qg \cdots g}^{MRK} \right|^2 &= \frac{4 \ s^2}{N_C^2 - 1} \ \frac{g^2 \ C_F}{|p_{1\perp}|^2} \left(\prod_{i=2}^{n-1} \frac{4 \ g^2 \ C_A}{|p_{i\perp}|^2} \right) \frac{g^2 \ C_A}{|p_{n\perp}|^2} , \\ \left| \overline{\mathcal{M}}_{qQ \to qg \cdots Q}^{MRK} \right|^2 &= \frac{4 \ s^2}{N_C^2 - 1} \ \frac{g^2 \ C_F}{|p_{1\perp}|^2} \left(\prod_{i=2}^{n-1} \frac{4 \ g^2 \ C_A}{|p_{i\perp}|^2} \right) \frac{g^2 \ C_F}{|p_{n\perp}|^2} , \end{split}$$

Allow for analytic resummation (BFKL equation). However, how well does this actually approximate the amplitude?

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Study just a slice in phase space:



Study just a slice in phase space:



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Study just a slice in phase space:



Study just a slice in phase space:

40GeV jets in Mercedes star (transverse) configuration. Rapidities at $-\Delta y, 0, \Delta y$.



High Energy Jets (HEJ):

- 1) Inspiration from Fadin&Lipatov: dominance by t-channel
- 2) No kinematic approximations in invariants (denominator)
- 3) Accurate definition of currents (coupling through t-channel exchange)
- 4) Gauge invariance. Not just asymptotically.

Scattering of qQ-Helicity States

Start by describing quark scattering. Simple matrix element for $q(a)Q(b) \rightarrow q(1)Q(2)$:

$$M_{q^- \mathsf{Q}^- o q^- \mathsf{Q}^-} = \langle \mathsf{1} | \mu | \pmb{a}
angle rac{\mathcal{g}^{\mu
u}}{t} \langle \mathsf{2} |
u | \pmb{b}
angle$$

t-channel factorised: Contraction of (local) currents across *t*-channel pole

$$\begin{split} \left| \overline{\mathcal{M}}_{qQ \to qQ}^{t} \right|^{2} &= \frac{1}{4 \left(N_{C}^{2} - 1 \right)} \left\| S_{qQ \to qQ} \right\|^{2} \\ & \cdot \left(g^{2} C_{F} \frac{1}{t_{1}} \right) \\ & \cdot \left(g^{2} C_{F} \frac{1}{t_{2}} \right). \end{split}$$

Extend to $2 \rightarrow n \dots$

J.M.Smillie and JRA: arXiv:0908.2786

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Building Blocks for an Amplitude

Identification of the **dominant contributions** to the **perturbative series** in the limit of well-separated particles

 $p_g \cdot V = 0$ can easily be checked (**exact** gauge **invariance**) The approximation for $qQ \rightarrow qgQ$ is given by

$$\begin{split} \left| \overline{\mathcal{M}}_{qQ \rightarrow qgQ}^t \right|^2 &= \frac{1}{4 \left(N_C^2 - 1 \right)} \, \left\| S_{qQ \rightarrow qQ} \right\|^2 \\ & \cdot \left(g^2 \, C_{\!\!F} \, \frac{1}{t_1} \right) \cdot \, \left(g^2 \, C_{\!\!F} \, \frac{1}{t_2} \right) \\ & \cdot \left(\frac{-g^2 C_A}{t_1 t_2} \, V^\mu(q_1, q_2) V_\mu(q_1, q_2) \right). \end{split}$$

Quark-Gluon Scattering

"What happens in $2 \rightarrow 2$ -processes with gluons? Surely the *t*-channel factorisation is spoiled!"



Complete t-channel factorisation!

J.M.Smillie and JRA

The *t*-channel current generated by a gluon in qg scattering is that genersated by a quark, but with a colour factor

$$\frac{1}{2}\left(C_{A}-\frac{1}{C_{A}}\right)\left(\frac{p_{b}^{-}}{p_{2}^{-}}+\frac{p_{2}^{-}}{p_{b}^{-}}\right)+\frac{1}{C_{A}}$$

instead of C_F . Tends to C_A in MRK limit.

Similar results for e.g. $g^+g^- \rightarrow g^+g^-$. Exact, complete *t*-channel factorisation.

By using the formalism of **current-current scattering**, we get a better description of the *t*-channel pole than by using just the BFKL kinematic limit.

- Have prescription for $2 \rightarrow n$ matrix element, including virtual corrections: Lipatov Ansatz $1/t \rightarrow 1/t \exp(-\omega(t)\Delta y_{ij})$
- Organisation of cancellation of IR (soft) divergences is easy
- Can calculate the sum over the *n*-particle phase space explicitly $(n \sim 30)$ to get the all-order corrections (just as if one had provided all the $N^{30}LO$ matrix elements and a regularisation procedure)
- **Match** to *n*-jet tree-level (by merging *m*-parton momenta to *n* hard jet-momenta) where this can be evaluated in reasonable time
- Resummation of HEJ recently merged with a parton shower (Ariadne)

Two drivers for multi-jet production:

- large ratio of transverse scales (shower resummation)
- Colour exchange over a range in rapidity

The LHC has the energy to explore the second mechanism. Several interesting studies already with the first (2010) year of data!

ATLAS: Study of Further Jet Activity in Dijet Events



This Atlas analysis did not cleanly separate the two "drivers" of jet production. (cut on \bar{p}_t induces large p_t -hierarchy on forward/backward jet, besides the hierarchy between large \bar{p}_t and Q_0 , the general jet scale)

HEJ slightly undershoots the jet activity when large ratios of transverse scales are imposed (shower region).

Very good agreement in the most important regions of phase space Obviously *beyond* NLO (more than one extra jet on average at $\Delta y \ge 3!$)

CERN-PH-EP-2011-100

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CMS: Simultaneous prod. of central and forward jet



Jets: anti-kt, R=.5, $p_t > 35$ GeV

central : $|\eta| < 2.8$ forward : 3.2 < $|\eta| < 4.7$

(not particularly large rapidity spans, typically 1 unit). Measure the p_t -spectrum of the central and the forward jet. Any difference is obviously due to additional radiation.

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Hard Jets and Higgs Bosons

Comparison to Theory, I



Comparison to Theory, II



Predictions for ratio of Inclusive Jet Rates vs. H_{T2}

S. Alioli, E. Re, J.M. Smillie, C. Oleari, JRA; arXiv:1202.1475



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Ratio of Inclusive Jet Rates vs. Rapidity

S. Alioli, E. Re, J.M. Smillie, C. Oleari, JRA; arXiv:1202.1475



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Simple set of cuts, combined with a exclusive dijet-analyses can discriminate clearly between the mechanisms of perturbative corrections implemented in NLO, POWHEG (NLO+Shower) and High Energy Jets.

T. Hapola, J.M. Smillie, JRA (JHEP 1209 (2012) 047)



D0: W+Jets



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CP Properties of Higgs-Boson Couplings from Hjj through Gluon Fusion Stabilising the Extraction against Higher Order Corrections

Why study Higgs Boson production in Association with Dijets?

The distribution in the **azimuthal angle** between the **two** jets in *Hjj* allows for a **clean extraction** of CP properties

The Problem

... in a region of phase space where the **perturbative corrections** are large.

How do we deal with events with three or more jets?

The Solution

By constructing an azimuthal observable, which takes into account the **information from all the jets** of the event!

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Considerations for Weak Boson Fusion



... and gluon fusion (Higgs coupling to gluons through top loop)



$$\mathcal{M} \propto rac{j_1^{\mu} \ C_{\mu
u}^{H} \ j_2^{
u}}{t_1 \ t_2}, \qquad j_1^{\mu} = \overline{\psi}_1 \gamma^{\mu} \psi_a$$
 $C_H^{\mu
u} = a_2 \left(q_1 q_2 g^{\mu
u} \ - \ q_1^{
u} q_2^{\mu}
ight)$
 $+ a_3 \ \varepsilon^{\mu
u
ho\sigma} \ q_{1
ho} \ q_{2\sigma}.$



Take e.g. the term $\varepsilon^{\mu\nu\rho\sigma} q_{1\rho} q_{2\sigma}$: for $|p_{1,z}| \gg |p_{1,x,y}|$ and for small energy loss (i.e. $p_{a,e} \sim p_{1,e}$):

$$\left[j_1^0 \, j_2^3 - j_1^3 \, j_2^0\right] \left(\mathbf{q}_{1\perp} \times \mathbf{q}_{2\perp}\right).$$

In this limit, the azimuthal dependence of the propagators is also suppressed: $|\mathcal{M}|^2 : \sin^2(\phi)$ (CP-odd), $\cos^2(\phi)$ (CP-even).

Azimuthal distribution



JRA, K. Arnold, D. Zeppenfeld (JHEP 1006 (2010) 091)

$$\begin{array}{l} \textit{CP-even, } p_{j\perp} > 40 \; \text{GeV}, \quad \textit{y}_{ja} < \textit{y}_h < \textit{y}_{jb}, \\ |\textit{y}_{ja,j_b}| < 4.5, \min \left(|\textit{y}_h - \textit{y}_{ja}|, |\textit{y}_h - \textit{y}_{j_b}| \right) > \textit{y}_{\text{sep}}. \end{array}$$

Signature and Cross Section



Rapidity separation between the jets and the Higgs Boson **enhance the azimuthal correlation**.

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Hard Jets and Higgs Bosons



All models show a clear increase in the number of hard jets as the rapidity span increases.

How to extract the *CP*structure of the Higgs boson coupling from events with **three or more** jets?

2 hardest jets?

J.R. Andersen, J. Campbell, S. Höche, arXiv:1003.1241



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2 hard jets furthest apart in rapidity?

J.R. Andersen, J. Campbell, S. Höche, arXiv:1003.1241

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Hard Jets and Higgs Bosons

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Significant washing out of the azimuthal correlation observed at tree-level *hjj*

J.R. Andersen, J. Campbell, S. Höche, arXiv:1003.1241



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Cuts and histograms for comparison study

Simulation & cuts:

- ▶ 8 TeV pp collisions, Higgs production by gluon fusion
- Jet-finding with anti- k_t , R = 0.4
- At least two jets with $|\eta_j| <$ 5, $p_{tj} >$ 25 GeV
- ▶ VBF cuts: $\Delta y_{jj} > 2.8$, $m_{jj} > 400$ GeV, tagging jets defined as two highest p_t jets; 3rd jet considered if $p_{tj} > 20$ GeV.

Histograms:

1.	p_{tj1} : 25200 GeV, 25 GeV steps	6.	m_{jj} : 0800 GeV, 40 GeV steps
2.	p_{tj2} : 25150 GeV 25 GeV steps	7.	$\Delta \phi_{jj}$: 0 π , 10 bins
3.	y_{j1} : $-5 \dots 5$ in steps of 1	8.	p_{tj3} : 20100, 10 GeV steps
4.	y_{j2} : $-5 \dots 5$ in steps of 1	9.	y_{j3} : $-5 \dots 5$, steps of 1
5.	$ \Delta y_{jj} $: 08, in steps of 1	[10.	$\Delta \phi_{ij,\gamma\gamma}$]

Comparison plots: Sherpa (20 GeV matching); MC@NLO (30 GeV matching); MINLO: Hjj sample; all at parton level, without MPI (UE)

Gavin Salam (CERN)	Jets in Higgs Searches	Higgs XS WG 2012-12-06 22 / 30	
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Excess or not?



MINLO, Sherpa & HEJ all agree at central jet rapidities; aMC@NLO 25-30% lower

Excess or not?

Distributions of ggF+2j AFTER VBF aMC@NLO topological cuts HEJ



factor 2 difference between aMC@NLO and Sherpa/MINLO, smaller differences between MINLO, Sherpa

recall Sherpa is H+2@LO, aMC@NLO & MINLO are H+2@NLO

MINLO

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Hard Jets and Higgs Bosons

Develop Insight Into the Perturbative Corrections



$$C^{H}(\mathbf{q}_{a\perp},\mathbf{q}_{b\perp}) = -i \frac{\alpha_{s}}{3\pi v} \mathbf{q}_{a\perp} \cdot \mathbf{q}_{b\perp}, \quad y_{0} < \cdots < y_{j} < y_{H} < y_{j+1} < y_{n}$$

The **High Energy Limit** tells us to investigate the **azimuthal angle** between the **sum of the jet vectors** either side in rapidity of the Higgs Boson!

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And It Even Works!



JRA, K. Arnold, D. Zeppenfeld, arXiv:1001.3822

Three subsamples of tree-level three-jet events: two jets on same side of the Higgs boson parallel (S1), perpendicular (S2) or anti-parallel (S3). Azimuthal correlation almost unchanged from hjj.

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Two hardest jets on one side, and the softest on the other (all above 40GeV - 1/3 of inclusive 3-jet cross section). Using **just the two hardest** jets gives **unsatisfactory** result.

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Hard Jets and Higgs Bosons

 The LHC probes hard (=jets) perturbative corrections beyond pure NLO

... already at 7TeV!

- High Energy Jets provides a new approach to the perturbative description of LHC physics
 - ... and compares favourably to data in several analyses

... already in its present, first iteration (several improvements foreseen in the theoretical description)