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Performance of a cluster of multi-anode photomultipliers equipped with lenses for use in a prototype RICH detector

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Abstract

A cluster of multi-anode photomultiplier tubes (MaPMTs) equipped with focusing lenses in front of the tubes was tested in a prototype ring imaging Cherenkov (RICH) detector in a charged particle beam. The readout electronics were capable of capturing the data at 40 MHz. The effects due to charged particles and magnetic field on the MaPMT performance were also studied. The results are used to evaluate the MaPMT as a possible photodetector for the LHCb RICH detectors. © 2002 Elsevier Science B.V. All rights reserved.

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1. Introduction

This paper reports on the performance of multianode photomultiplier tubes (MaPMTs) for the detection of Cherenkov light in a prototype ring imaging Cherenkov (RICH) detector. The

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MaPMTs are the back-up option³ for the photodetector to be used in the RICH detectors of the LHCb experiment [2] at the future large hadron collider (LHC) at CERN. The performance studies presented here include, for the first time, those where the MaPMT data have been captured at 40 MHz, which is the bunch crossing rate of the LHC. A full description of the desired physics performance of LHCb and the subsequent requirements on the RICH detector can be found elsewhere [3]. A photodetector that meets these requirements must be both sensitive to single photons and spatially precise to a few millimeters. Furthermore, the device and accompanying electronics must have a fast enough response to be read out in 25 ns.

A 3×3 array of MaPMTs has been tested using a RICH prototype in a beam at the CERN SPS facility. In order to reduce the losses of photons in the insensitive areas at the edges of the MaPMT, which corresponds to about 50% of the total area, the MaPMTs have been equipped with lenses. Pipelined readout electronics, compatible with the LHC 25 ns bunch crossing interval, have been tested for the first time on a RICH prototype. Also the effects of two potential hazards in a real detector environment have been investigated: the effect of charged particles traversing the MaPMT and the lenses, and the impact of different strength magnetic fields on the performance of the MaPMTs. For the magnetic field tests the possibility of shielding the MaPMTs against such fields was also studied.

The main aim of the tests was to demonstrate that the MaPMT is a viable photodetector for the LHCb RICH system. These tests aim to determine:

- the performance of the MaPMTs in an array, with and without lenses
- the MaPMT's operation with pipelined readout electronics; and
- the functionality of the MaPMTs in a real detector environment.

Each of the above topics is reported below. In addition, laboratory tests of aspects of the MaPMT performance are presented.

The light collection system of the HERA-B RICH detector [4,5] has many similarities with the LHCb prototype system reported in this paper. The HERA-B RICH detector uses the 4 and 16 anode versions of the MaPMT with a lens system [6] to reduce photon loss to the insensitive areas. Furthermore, the readout electronics operate at 10 MHz. This system has operated successfully since 1998 [7].

The organisation of this paper is as follows. Section 2 contains a description of the hardware used in both the test beam and in the LED scanning facilities. The lenses and the pipelined electronic readout system are described in detail. The results of laboratory tests of the MaPMTs are reported in Section 3. In Section 4 the test beam results with respect to Cherenkov photon counting, with and without lenses, are presented. In addition, the effect of varying the angle of incidence between the incoming Cherenkov photons and the detector plane is investigated. The results are compared to a simulation of the RICH prototype. Sections 5 and 6 give the results of the charged particle and magnetic field studies, respectively. Finally, conclusions are given in Section 7

2. Hardware description

2.1. MaPMTs

The MaPMT consists of an array of square anodes, each with its own metal dynode chain, incorporated into a single vacuum tube to amplify the photoelectrons emitted by the cathode. The densest pixelisation available, 8×8 pixels, provides the spatial resolution required for the LHCb RICH detector. Fig. 1 shows a schematic of the MaPMT. The dynode structure is divided into 64 channels of $2.0 \times 2.0 \text{ mm}^2$ area, separated by 0.3 mm gaps.

The 64-pixel MaPMTs are commercially available and have been tested by LHCb in 1998 [1]. Since then the manufacturer, Hamamatsu, has

³The baseline solution is the pixel hybrid photodiode detector (HPD), studies of which are reported elsewhere [1].



Fig. 1. Sketch of the top and side view of an MaPMT.

provided some modifications which better match the LHCb RICH specifications. The MaPMT R7600-03-M64⁴ described in this paper has a 0.8 mm thick UV-glass window with a semitransparent bialkali photocathode (PC) deposited on the inside. The threshold for the light transmission through the UV-glass window is at a wavelength of 200 nm. The quantum efficiency of the PC is plotted versus the wavelength of the photons in Fig. 2. The quantum efficiency has a maximum of 22% at 380 nm. For each pixel the photoelectrons are focused onto a 12-stage dynode chain (see Table 1) and multiplied through secondary emission. The mean gain of the MaPMT is about 3×10^5 when operated at a voltage of 800 V.



Fig. 2. The quantum efficiency of the MaPMT R7600-03-M64 as a function of wavelength. The measurement was made by Hamamatsu.

Nine MaPMTs were purchased and preselected such that the average gain of the tubes varied by not more than a factor of two. A study of the variation of gain for the 64 pixels within one tube is presented in Section 3.

The geometrical coverage of the MaPMT, defined as the ratio of the sensitive PC area to the total tube area including the outer casing, is only 48%. This fraction can be increased by placing a single lens with one refracting and one flat surface in front of each MaPMT [8]. A single refracting surface with radius of curvature, *R*, has a focal length

$$f = \frac{R}{1 - 1/n}$$

where *n* is the refractive index of the lens material. Fig. 3 shows a schematic view of such a lens system in front of the close-packed photomultipliers. If the distance *d* from the refracting surface to the PC is chosen to be equal to *R*, the demagnification factor is $(f - d)/f \approx 2/3$ for a quartz lens with n = 1.5. Over the full aperture of the lens, light at normal incidence with respect to the photodetector plane is focused onto the PC,

 $^{^{4}}$ With respect to its predecessor, the R5900-00-M64, the borosilicate window is replaced by a UV-glass window which increases the integrated quantum efficiency by 50%. In addition, a flange of 1 mm size around the MaPMT is removed, thereby improving the packing fraction by 14%.

Table 1Resistance chain used to provide the voltages at the PC and the dynodesDvnodePC12345678910





Fig. 3. Schematic of a side view of the lens system, in front of the close-packed MaPMTs. The focal length, f, is 75 mm. The thickness of the lenses, t, is 24 mm. The focusing of normally incident light is illustrated. The full aperture of the lens is focussed onto the sensitive area of the MaPMT.

thus restoring full geometrical acceptance. The demagnification resulting from this lens configuration is illustrated in Fig. 4. This demonstrates that the 'pin cushion' distortion is small compared to the pixel size. The focusing is also quite independent of the angle of incidence of light. For nonnormal incidence the image is placed on the sensitive area of the MaPMT by appropriately translating the lens relative to the PC; this is discussed further in Section 4.5. Nine fused silica lenses, one for each MaPMT have been purchased.⁵ The flat surface, which faces the PC is $26 \times 26 \text{ mm}^2$, the radius of the spherical surface is 25 mm and the maximum height is 24 mm.



Fig. 4. Impact points of a bundle of light rays incident on the entrance window of the MaPMT: (a) with no lens, (b–d) with a lens; (b) is for normally incident light, (c) and (d) are for an angle of incidence of 200 and 400 mrad in the horizontal plane, respectively. In (c) and (d) a translation of the lens relative to the PC has been made to contain the image within the sensitive area of the MaPMT. The solid (dashed) line indicates the total (sensitive) area of the tube.

2.2. Experimental set-up for beam tests

The charged particle beam tests were carried out in the X7b beam at the CERN SPS. The beam was tuned to provide negative particles (95% pions) with momenta $120 \pm 1 \text{ GeV}/c$. The experimental set-up included scintillation counters and a silicon pixel telescope to define and measure the direction of the charged particles, a vessel which contained CF₄ gas radiator, a spherical mirror to focus the Cherenkov light and the MaPMT photodetector cluster. A schematic diagram of the Cherenkov

⁵The lenses were machined and polished by Optical Works, Newquay, Cornwall, UK.



Fig. 5. A schematic of the Cherenkov vessel.

vessel is shown in Fig. 5. The components are briefly described below and more complete description can be found in Ref. [9].

The beam telescope was composed of three planes of silicon detectors, each segmented into a 22×22 matrix of 1.3 mm^2 pixels. The pixels were read out using the Viking VA2 ASIC [10]. This is a 128-channel amplifier–shaper–multiplexer chip, four of which are mounted on each telescope plane.

The Cherenkov vessel is a prototype geometry for the LHCb RICH 1 detector. Charged particles entered the radiator volume along a tube of 90 mm internal diameter and intersected the centre of a spherical aluminised-glass mirror which was tilted by 18° to the beam axis. The plane of the MaPMT array was 1143 mm from the mirror centre. The mirror has a diameter of 112 mm and a focal length of 1117 mm. Its reflectivity has been measured [1] to be 90% at 600 nm, falling to 70% at 200 nm. The mirror was mounted on micrometer screws, fixed to the back plate of the vessel. These allowed fine adjustments to precisely align the Cherenkov photons onto the photodetector array.

The Cherenkov radiator was a CF_4 gas⁶ contained within a volume of length 1000 mm

between the beam entrance window and the mirror. The gas was supplied at high pressure, via a recirculation system [1] to the vessel. The absolute pressure in the vessel could be set and stabilised by the system over a wide pressure range from 100 to 1200 mbar. Throughout data collection, gas pressure and temperature, water vapour and oxygen concentrations were monitored. These were used for correcting the CF_4 refractive index, which has been parameterised as a function of wavelength at STP [11]. Data were collected with CF_4 at a pressure of 700 mbar.

Between the mirror and the photodetectors the radiator vessel was sealed using a 25 mm thick fused silica plate. Initial tests, using a single MaPMT, verified that the loss of Cherenkov light resulting from transmission through this plate was 8%, consistent with that expected due to reflection.

The fused silica lenses described in Section 2.1 were close-packed and mounted close to (<0.5 mm), but not in optical contact with, the PC windows of the 3×3 array of MaPMTs. A micrometer screw allowed the position of the lens array to be displaced sideways by up to 10 mm with respect to the PCs. The overall photodetector assembly could be rotated with respect to the incident Cherenkov light. Unless otherwise specified data were collected at normal incidence.

2.3. Readout electronics

The tests involving individual MaPMTs were performed using a readout chain of CAMAC amplifiers and ADCs [1]. For the beam tests of the 3×3 array of MaPMTs a new pipelined electronic readout system was used, which is shown schematically in Fig. 6. An overview of the system follows, in which several of the components (italicised) will be described in more detail.

Nine MaPMTs were mounted in a 3×3 array on a *bleeder board* unit, which supplied high voltage (HV) to the MaPMTs and positioned them in the vessel. The output signal channels in the back plane of the bleeder board were coupled to the *front-end boards* via *kapton cables*. Each frontend board multiplexed the analogue signals from one or two MaPMTs and was the carrier for the

⁶CF₄ is the LHCb RICH 2 radiator.



Fig. 6. A schematic of the electronic readout and data acquisition systems. The components within the dashed box were those on the detector in the experimental area.

front-end application-specific integrated circuit (ASIC), the *analogue pipeline voltage (APVm)* [12–14]. The APVm shaped, amplified, buffered and multiplexed the input signals. The front-end boards were then coupled to a single *interface board*, which fanned out the power, the trigger signals, the clock and the Philips I²C control signals [15] for the APVm. Fig. 7 shows a photograph of the front-end electronics. The analogue pipeline signals from the APVm and a synchronous signal accompanying it were routed directly to the front-end digitiser (FED) and the rest of the data acquisition system, which is described in Section 2.4.

The bleeder board provided the mechanical support and dynode chain resistor network for up to 16 MaPMTs in a 4×4 array. The board also adapted the MaPMT anode feed-through pitch of



Fig. 7. A photograph of the MaPMT array, bleeder board, front-end electronics board with APVm ASIC and AC-coupler network along with the mechanical support used in the test beam. The components described in Section 2.3 are indicated.

the 16×64 data channels to the pin grid array (PGA) pitch of the kapton cable. The kapton cables were used to couple the 8×8 output PGA for each tube, in the backplane of the bleeder board, to the front-end board. The kapton cables can be seen in Fig. 7. The kapton cable from one MaPMT was coupled to two 40-way SAMTEC⁷ connectors (64 data channels and 16 ground lines) on the front-end board.

The layout of the front-end board is given in Fig. 8. The main components on the board are the AC-coupler network, which also acts as a fan-in, and the APVm ASIC. The APVm ASICs were designed for use with silicon strip detectors or micro-strip gas chambers (MSGCs) which produce signals approximately 10 times smaller than those from an MaPMT. Therefore, the MaPMT signals have to be attenuated within the dynamic range of the APVm. This was achieved with an AC-coupler. The coupler was made from a gold plated ceramic base on which tracks were etched.

The APVm [14] is one of the APV series [12,13] of radiation-hard front-end ASICs which have been designed for the readout of the CMS inner detector [16]. The APVm has been fabricated using the Harris AVLSIRA bulk CMOS process [17].

⁷Cable-to-board SFMC series.



Fig. 8. A schematic of the front-end board which carries the APVm ASIC.

These ASICs have been previously used in a beam environment for the readout of silicon-strip detectors [12].

In the test beam readout system the APVm ASIC, running at 40 MHz, sampled the 128 input analogue signals every 25 ns. The signals were stored in a pipeline structure of 160 cells in depth, which allowed a maximum first-level trigger latency of $3.2 \,\mu s$.

On arrival of a trigger to the APVm the data were tagged for readout. The analogue output was cycled out of the ASIC at half the data-sampling rate (20 MHz). The whole analogue data frame was $7 \,\mu$ s in length. Further details of the pipeline control logic can be found in Ref. [14] and the references therein.

Synchronous to the data output there was a second output which changed level when a data frame was being read out, which is illustrated in the fifth line of the timing diagram given in Fig. 9. This was used to trigger the data acquisition system as described in Section 2.4.

The APVm ASICs are not designed to meet the requirements of the LHCb trigger and readout architecture. In particular, the 1:128 multiplexing of the analogue signals at 20 MHz precluded operation at the first-level trigger rate of 1 MHz

[18] and a signal return-to-zero within 25 ns was only possible in the de-convolution mode of APVm operation [12]. This requires three consecutive samples for the algorithm, and therefore prevents triggering on consecutive events. Nevertheless these tests provided an important indication that the use of MaPMTs will be compatible with the operation of the LHCb RICH when equipped with appropriate front-end ASICs [19,20], which are currently under development, the design of which addresses both of these issues.

The interface board fanned out the low-voltage differential signalling (LVDS) trigger and clock signals, which were generated by the SEQSI [21] VME module, to the front-end boards. Furthermore, it distributed and filtered the ± 2 and ± 5 V power supplies required to operate the APVm and the buffers on the front-end board, respectively. The control of the bias voltages, shaping currents, latency, operation and calibration modes of the APVm, was done using the Philips I²C protocol signals, which were routed via the interface board. The control signals were generated on a PC using a LABView interface⁸ to drive an I²C PCI-card.

⁸National Instruments.



Fig. 9. The timing diagram for the pipelined electronic readout and data acquisition system. The data frame begins a variable time up to $3.2 \,\mu s$ after the beam trigger. The data frames is $7 \,\mu s$ long.

2.4. The data acquisition system

The main components of the VME-based data acquisition system are shown in Fig. 6. Data were generated from three sources: the nine MaPMTs, the silicon beam telescope and the trigger scintillators. The event size of 1.5 kbyte is dominated by the MaPMT data, which was not zero-suppressed. The acquisition system was capable of sustaining a trigger rate in excess of 1 kHz for the 1.7 s duration of the SPS spill.

The beam trigger was formed from the coincidence between the four scintillators in the beam line. A beam trigger signal initiated the readout sequence to be generated in the SEQSI, which is shown in the third line of the timing diagram. The SEQSI produced a 25 ns wide LVDS pulse to trigger the front-end ASIC, which marked the event in the pipeline to be read out.

Each of the the six APVm ASICs produced an analogue data output which were digitised using the FED [22,23]. The FED is a PCI Mezzanine Card (PMC) which was affixed to a VME-based motherboard and processor unit.⁹ The FED PMC was a prototype module from the readout of the CMS inner tracker. The front panel of the FED PMC has eight analogue input data channels, a trigger and a clock input. The data from the frontend boards were both level shifted and amplified, to fall within the dynamic range of the Flash ADCs (FADCs) on the FED PMC, by a separate level changing board. The 40 MHz clock input was taken from the interface board; this was done to preserve the correct phase relationship between the clock and trigger input signals to which the FED PMC was sensitive. The trigger was required to be an LVDS signal of width <25 ns. This was created from the signal synchronous to the data by AC-coupling its front-edge and then converting this pulse signal to LVDS on the FED level changing board.

Event data were accumulated in the readout processor's local memory during the SPS spill and were transferred via 100 Mbit/s Ethernet connection to a mass storage device during the inter-spill gap.

2.5. Monte Carlo simulation

A detailed simulation program of the set-up was developed, which is described in detail in Ref. [1]. The refractive index of the CF_4 radiator as a function of the photon wavelength was obtained from the parameterisation used in Ref. [11]. The values of the refractive index and the measured mirror reflectivity were identical to those given in Ref. [1].

The program also simulated the MaPMTs as described in Section 2.1, including the effects of lens focusing (Fig. 3), the geometry of the detector surface, (Fig. 1) and the quantum efficiency of the MaPMTs (Fig. 2). A detailed electronics response (including the dynode chain) was not simulated. Instead the signal loss at the first dynode and below the threshold cut was estimated from the data. The average signal loss was subtracted MaPMT-by-MaPMT from the simulated photon counts.

⁹CES RIO, model No. 8061.



Fig. 10. A schematic of one of the LED scanning facilities equipped with CAMAC readout electronics. Gradient index (GRIN) lenses are used to focus the LED at the entrance and exit (dashed inset) to the optical fibre.

2.6. LED scanning facilities

Further tests of tubes and the electronic readout were performed using LED scanning facilities. Two such facilities were used. The general features of both facilities are described below and are shown schematically in Fig. 10.

The MaPMTs were protected from extraneous light by a light-tight box. All cabling was brought into the box via feed-through connectors, which were isolated from the frame of the box to reduce ground loops. The tube was supported and clamped in a silicon resin-bonded fibre block. This provided insulation of the MaPMT casing, which was held at the cathode potential, to prevent current leakage across the window.

The light source used was a blue 470 nm LED with a maximum luminosity of 1000 mcd and a view angle of 15°. The pulsing of the LED was performed using a FET circuit which provided a switching rate of 10 kHz with a pulse duration of approximately 10 ns. The LED was mounted externally and fed through the dark box using a mono-mode optical fibre. This was done for two reasons: to restrict the light pulse to a narrow wavelength band with a Gaussian distribution and to minimise the spot size from the end of the fibre by reducing aberrations. To reduce the LED spot size at the MaPMT window a sequence of lenses was used at the entry and the exit to the optical fibre. The width of the light spot from the fibre at the MaPMT window was 50 or 100 µm depending on the focusing system. These values were measured using a CCD camera.

The MaPMT and the fibre tip were both mounted on motorised stages. The stages could be positioned with a resolution better than $5 \mu m$ which allowed precise scans over the MaPMT's acceptance. A stepper motor driver, interfaced to a PC, was used to control the stages.

3. LED scan results

The response of the MaPMTs to single photons has been measured with the scanning facility described in Section 2.6. The PC of the MaPMT was operated at a voltage of -900 V. The LED intensity was set such that for $\sim 25\%$ of the events at least one photoelectron was produced at the PC, within the 200 ns interval during which the signal was sampled. The events were recorded at a rate of ~1000 Hz. In Fig. 11 a measured pulse-height spectrum is shown. The broad signal containing mostly one photoelectron and the narrow pedestal peak are clearly visible. The mean pulse-height, s, is approximately 90 ADC counts above pedestals. The spectrum has been fitted by a function which allows a Gaussian shape for each photoelectron signal and for the pedestal peak; the number of photoelectrons in a pixel per event, n_{pe} , has to follow a Poisson distribution with a mean, λ_{pe} . The sigma of the Gaussian signal shapes is constrained to be proportional to $\sqrt{n_{\rm pe}}$. The fit is



Fig. 11. The photon spectra of an MaPMT pixel with a fit superimposed.

superimposed on the data points. The sigma of the single photon signal, σ_s , is about 50 ADC counts. The agreement between fit and data is good for large pulse-heights which allows for reliable determination of *s*, σ_s and λ_{pe} . The signal shape is non-Gaussian at small pulse-heights and as a consequence the fit fails to describe the data just above and below the pedestal peak; this would lead to an unreliable measurement of the signal loss using this method. Furthermore, this region contains a contribution from the photoelectric effect at the first dynode induced by photons transmitted through the PC window [24]. This effect has not been considered in the fit presented here.

The value of s/σ_s gives an estimate of $\sqrt{g_1}$ to first order, where g_1 is the gain at the first dynode. The gain is underestimated in this method as the additional broadening of the signal from the rest of the dynode chain is neglected. For the pixels studied a lower limit of 3.7 for g_1 was found from s/σ_s . The probability that no multiplication occurs at the first dynode, P_1 , is equal to e^{-g_1} . Therefore, the gain measured corresponds to a value of P_1 of 2.5% or less. The signal-to-pedestal-width ratio is 40:1.

The dependence of the gain of the MaPMT on different parameters has also been studied. The



Fig. 12. The measurements of (a) *s*, the mean pulse-height, and (b) s/σ_s as a function of HV. Measurements for pixels in the centre and at the border of the MaPMT are given.

gain becomes larger with increasing negative HV applied to the PC. Fig. 12 shows the measurements of s and s/σ_s as a function of the HV applied at the PC. The gain varies for the 64 different dynode chains within a tube. In Fig. 13 the s of all 64 channels of one tube is given. The gain varies by up to a factor of three with an RMS spread of about 30% above the mean value. Channels at the edge of the array in the y-direction and at the edge of the array at large x have lower gain.

The edge pixels were investigated in more detail by scanning across the tubes in steps of 0.1 mm. The measured gain as a function of the position of the light source across the tube is shown in the top of Fig. 14. The scan was made in the *x*-direction as defined in Fig. 13. For the edge pixel the gain was not constant and dropped before the geometrical edge of the pixel. This was also reflected in the measurement of the average number of observed photons, λ_{pe} , as shown in the bottom of Fig. 14. The collection efficiency, which is proportional to λ_{pe} , deteriorated towards the edge of the pixel. This reduced the overall efficiency of the MaPMT by a few percent. The pixel size is defined by the 50% efficiency points of a pixel and was found to



Fig. 13. The measured value of *s* for all pixels of an MaPMT. The coordinate system is such that the additional focusing wires of the MaPMT run parallel to the *y*-axis at the centre of each pixel column.



Fig. 14. Scan across 3 MaPMT pixels in the *x*-direction as defined in Fig. 13. The measurements of (a) *s* and (b) λ_{pe} as a function of scanned position.

be 2.1 mm, which is a little larger than the 2.0 mm opening of the dynodes reported by the manufacturer.

4. Cherenkov light detection

Results obtained from measurements of Cherenkov rings using the MaPMT cluster equipped with lenses are presented in this section. The experimental set-up and beam conditions are described in Section 2.2. The algorithms for correcting raw ADC counts for common-mode fluctuations and identifying crosstalk within the pipelined electronics are described in Sections 4.1 and 4.2. In Sections 4.3–4.5, the measurement of the number of photoelectrons produced per charged particle is presented and the results are compared to the simulation. Results are compared with and without lenses, and for different angles of incidence of Cherenkov radiation on the photodetector



Fig. 15. The physical positions, as seen by the incident Cherenkov photons, and the labels of the MaPMTs and the corresponding front-end boards.

plane. All data used in the analysis were taken with a voltage of -1000 V applied to the PC.

The numbering scheme used throughout this article for the MaPMTs and front-end boards is shown in Fig. 15.

4.1. Common mode correction

In the first stage of analysis the data were connected for common-mode fluctuations. These fluctuations were observed as time-dependent shifts in the pedestals of each channel, correlated throughout an MaPMT.

Common-mode fluctuations were corrected tube-by-tube. In a first iteration, the pedestal mean, μ , and width, σ , were determined for each pixel. The width after this stage overestimated the noise in the channel due to the common-mode contribution. The data were then reprocessed and pixels with a pulse-height above $\mu + 3\sigma$ were classified as a hit and were excluded. For the 64 or less pixels remaining without a hit in an individual event, the differences between the ADC values and the pedestal means, calculated in the first iteration, were averaged across a single tube. This gave the common-mode correction of that MaPMT for that event. This correction was subsequently subtracted from all pulse-heights for all pixels in an MaPMT.

Table 2 shows the common-mode correction for each tube. It is evident that the common-mode behaviour was very similar for tubes on the same front-end board. Laboratory tests where 0, 1 or 2 tubes were connected to a front-end board confirmed that the common-mode fluctuations were associated with the front-end board and not to the tubes themselves.

4.2. Crosstalk identification and correction

Crosstalk was identified using an LED to illuminate the MaPMT array uniformly with single photons.

Fig. 16(a) shows the correlation coefficient, $\rho(ADC_x, ADC_y)$, between the pulse-heights of pixels x, y within the same tube. The significant off-diagonal correlations indicate a large crosstalk between pixels. Fig. 16(b) shows $\rho(ADC_x, ADC_y)$ when reading out the MaPMT with CAMAC electronics. The absence of crosstalk in this latter case indicates that the source of the crosstalk is located in the pipelined readout electronics chain and not within the tube. The 95% confidence limit on the level of cross-talk in the tube is 0.3%; this

Table 2 Widths of the pedestal peaks before and after common-mode correction for all tubes

Tube	Board	Common mode correction (ADC counts)	Pedestal widths (ADC counts)	
			Before	After
1	1	1.4	1.8	1.0
4	1	1.3	1.7	1.0
2	2	1.0	1.4	1.0
5	2	1.0	1.4	1.0
3	3	0.9	1.2	0.8
6	3	0.8	1.1	0.8
7	4	0.9	1.2	0.9
8	5	0.8	1.2	0.8
9	6	0.9	1.5	1.1



Fig. 16. Correlation coefficients between the pulse-heights of pixels within one tube for the (a) pipelined and (b) CAMAC readout. For clarity the scale has been truncated to a maximum of 0.5. The diagonal has a correlation coefficient of 1.

compares well with measurements of the 16 anode MaPMT [25].

To determine the nature of the crosstalk, the probability that a signal in pixel x was induced by a hit in pixel y was determined. Firstly a hit pixel was identified as having an ADC-value greater than 5σ above the pedestal mean. In the case of a hit in both pixels x and y, the pixel with the greater ADC-value was defined as the true photon hit; the other pixel hit was assumed to have been induced by crosstalk. The crosstalk probability is then defined as the ratio of the total number of pixel y-induced hits in pixel x to the total number of hits in pixel x. Genuine multi-photon events mean that this probability has a small offset from zero everywhere.

Fig. 17 shows the crosstalk probabilities for one front-end board. It can be seen that the crosstalk extends across the board, hence is not contained within a single MaPMT. The crosstalk has a symmetric component, where pixel y induces a signal in pixel x and vice versa, and also an asymmetric component. Three sources of crosstalk with differing strength were identified as originating from the readout electronics; these are listed in Table 3. The values for the asymmetric crosstalk varied widely between different ASICs used. Given the identified sources of crosstalk, a set of crosstalk partners which could induce a hit was associated to each pixel.

In subsequent photon-counting analyses using the pipelined electronics, the first step was the



Fig. 17. Crosstalk probabilities for board 2. The entries correspond to the probabilities that a signal in pixel x (on the x-axis) was induced by a hit in pixel y (on the y-axis).

removal of crosstalk hits. For each hit pixel the crosstalk partners were also searched for a hit. The pixel under consideration was then discarded if any of its associated crosstalk partners had a hit with a greater pulse-height.

This method leads to a loss in efficiency due to the rejection of genuine hits in the crosstalk partners. Correction factors were applied pixel by pixel to the data to correct for this effect. The corrections factors were dependent on the Cherenkov ring position on the MaPMT array. Integrated over the whole array, the total correction factor was 9%.

Table 3

The sources of crosstalk and ratio of signal to crosstalk pulse heights, r

Source	r
Symmetric crosstalk	
AC-coupler	0.15
Kapton cables and PGA	0.01
Asymmetric crosstalk	
APVm ASIC	0.01-0.33

An alternative crosstalk correction algorithm was also implemented for each pixel. This method involves the subtraction of a constant fraction of the pulse-height in pixel y from the pulse-height measured in the crosstalk partner, pixel x. The fractions were determined from the LED data. This method was used to correct the ADC spectra and to evaluate the systematic error due to the crosstalk correction.

Although significant crosstalk is observed in parts of the front-end readout system, in any future hardware iteration the crosstalk from the AC-coupler can be reduced by introducing a ground plane. Furthermore, in future iterations of the pipelined readout, it is anticipated that the ASIC preamplifier gain will be better matched to the input signals. Therefore, an AC-coupler will no longer be necessary.

4.3. Photon counting method

Photon counting was performed for each pixel. Firstly, the mean (μ) and width (σ) of the common-mode corrected ADC pedestal were found by fitting a Gaussian distribution. A threshold cut for each pixel was defined at $\mu + 5\sigma$; any ADC count above this threshold was considered as a hit. Crosstalk hits were removed as described previously.

The ratio of events, $f_{\rm hit}$, with a hit in a given pixel to the total number of triggered events was calculated. $f_{\rm hit}$ is related by Poisson statistics to the mean number of observed photons which give a hit per event, $\lambda_{\rm hit}$, by

$$\lambda_{\rm hit} = -\ln(1 - f_{\rm hit}). \tag{1}$$

This relationship assumes no signal loss. In reality there is loss arising from two sources. Firstly, the flow of electrons can terminate at a stage in the dynode chain, due to no secondary emission. This is dominated by the probability that a single photoelectron arriving at the first dynode does not produce any secondaries, $P_1 = e^{-g_1}$, where g_1 is the gain at the first dynode. The second source of signal loss is due to the pulseheight being below the threshold cut.

In making the comparison between data and simulation, a correction is made to the simulation for the relative fractions of signal loss, described in Section 4.4.

4.4. Results from the MaPMT array

The major correction to the photon counting is that associated to crosstalk; $\sim 45\%$ of the pixel hits are from this source. An example of the crosstalk correction is given in Fig. 18 which



Fig. 18. Spectra (a) before and (b) after correction. The plot of the spectra after correction has the fit superimposed (solid line). The single photoelectron part of the spectra is also shown (dashed line). The vertical line indicates the 5σ cut above the pedestal which defined a photon hit.

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shows a typical pulse-height spectrum from Cherenkov light, before and after the crosstalk correction.

The corrected spectra were used to establish the signal loss in each pixel. The spectra were fitted with a function to describe the output of a photomultiplier tube. The fitting function describes the amplification of the dynode chain analytically as a series of Poissonian processes [26]. The five parameters returned by the fit are μ and σ of the pedestal, the mean number of photoelectrons per pixel per event, $\lambda_{\rm pe}$, g_1 and the conversion factor between the number of electrons at the end of the dynode chain and the ADC value. An example of a fit is shown in Fig. 18(b). From the shape of the single photoelectron part of the function and the gain at the first dynode, both types of signal loss can be estimated. The value of g_1 is 2.2 for this pixel; the value obtained using the fit method described in Section 3 is 2.1. The excellent fit to the corrected data demonstrates that the crosstalk component has been successfully removed.

Table 4 shows the signal loss averaged over each MaPMT. The average total signal loss is 13%, and the average values of the loss below threshold and P_1 are 10% and 3%, respectively. The values in the table were used in the full simulation of the MaPMT array, described in Section 2.5.

LED runs were used to identify deal channels. Laboratory scans showed that the dead channels were associated with the readout electronics and not the MaPMTs. Also, noisy channels which

Table 4
Measurements of photon signal losses, averaged over pixels for
each MaPMT

Tube	Loss below cut (%)	Gain at 1st dynode	Total loss (%)
1	8 ± 4	3.2 ± 0.5	13 ± 7
2	12 ± 5	3.9 ± 0.4	14 ± 6
3	14 ± 2	3.2 ± 0.4	18 ± 4
4	5 ± 2	4.0 ± 0.4	7 ± 2
6	7 ± 3	3.8 ± 0.8	10 ± 7
7	14 ± 4	3.2 ± 0.4	17 ± 6
8	11 ± 3	3.4 ± 0.5	15 ± 5
9	11 ± 3	3.7 ± 0.7	14 ± 5

contained a very large number of hits after the crosstalk correction were identified. Dead and noisy channels were masked in the photon counting analysis for both experimental and simulation data. Altogether 36 channels (6% of the array) were removed; however, the number of masked channels on the Cherenkov ring with and without lenses was only 4 and 6, respectively.

The integrated signals for a run of 6000 events measured with the 3×3 array of MaPMTs with and without quartz lenses are shown in Fig. 19.



Fig. 19. Cherenkov ring from a 1 m CF_4 radiator at a pressure of 700 mbar integrated over 6k events, measured with the 3×3 array of MaPMTs (a) with, and (b) without quartz lenses mounted in front of the tubes. In (a) the insensitive areas between tubes are not shown and the active areas of adjacent tubes are plotted next to each other. In (b) the insensitive areas are shown along with the array dimensions.

The Cherenkov rings are clearly visible, as is the effect of the lenses.

Finally, background hits were removed. Background arises from electronic and detector noise, and scattered Cherenkov light, assumed to be uniform over the array. The background was estimated by averaging the hits, MaPMT-by-MaPMT, over all pixels that were not lying on the Cherenkov ring.

In Table 5 the results on photon counting for the 3×3 array of MaPMTs are shown, with and without lenses. The mean numbers of hits per pixel per event, λ_{hits} , were summed over the whole array to give the total hits per event. The background contribution, integrated over the whole array, was subtracted to give the total number of photons per event, N_{pe} . The gain in N_{pe} by employing the lenses is 55%. The photon yield for the individual tubes is shown in Table 6; the results agree well with the simulation. From this it can be estimated that the relative quantum efficiency of the tubes varies by less than $\pm 10\%$.

The large number of events (6000 per run) result in the statistical errors being 0.5%. Systematic errors from several sources have been estimated. The major source of error is the crosstalk correction. This error was estimated to be 4.5% by comparing the results obtained with the alternative method of crosstalk removal, described in Section 4.2. An error of 1.2% was associated with the stability over the data-taking period. This was estimated by comparing the value of N_{pe} over different runs. The total error on $N_{\rm pe}$ is 4.7%. There is an uncertainty on the simulation value of $N_{\rm pe}$ of 2.6% due to the errors on the signal loss measurements. Within these errors the data on photon counting results are in reasonable agreement with simulation.

From the observed yield of photoelectrons, the figure of merit for a RICH detector, $N_0 = N_{\rm pe}/(\sin^2(\theta_{\rm C})L)$, where L is the length of the radiator (100 cm) and $\theta_{\rm C}$ is the Cherenkov angle, can be calculated. The value of N_0 is determined to be $110 \pm 7 \,{\rm cm}^{-1}$. The measured value of $\theta_{\rm C}$ was 25.5 mrad, compared to the expectation of 24.9 mrad. The average of these two numbers was used in the calculation of N_0 , with the full difference taken as the error.

Table 5

Total photon yields per event for the 3×3 array of MaPMTs. For the case with lenses the yield before and after crosstalk correction is given

	With lenses		Without lenses corrected
	No correction	Corrected	
Data	13.61	7.25	4.69
Background	—	0.29	0.21
Signal $(N_{\rm pe})$	_	6.96 ± 0.33	4.49 ± 0.21
Simulated (N_{pe})		6.49 ± 0.17	4.03 ± 0.10

Table 6

Photon yields per event, N_{pe} , for the individual MaPMTs with lenses, after the cross talk correction has been applied. The results are ordered as in the layout of Fig. 15

	N _{pe} per tube		
Signal	0.62	1.11	0.65
-	1.20	0.00	1.16
	0.66	0.90	0.66
Simulation	0.56	1.10	0.68
	0.93	0.00	1.06
	0.58	0.91	0.67

A measurement of the resolution is not presented here because it is dominated by the pixelisation of the MaPMT, which is not the case for the LHCb RICH design [3]. The geometry and gas had been chosen such that the Cherenkov radiation from 120 GeV/c pions was contained within the 3×3 array of MaPMTs for tests of the lenses, tubes and electronics, and not for the measurement of $\theta_{\rm C}$ resolution in an LHCb RICH prototype. Measurements of Cherenkov angle resolution with MaPMTs in an LHCb RICH 2 prototype are reported elsewhere [1].

4.5. Varying the angle of incidence

The final LHCb RICH design may have a geometry where the Cherenkov light is not incident normal to the photodetector plane. Therefore, the performance of the array with



Fig. 20. Recovering photons in a titled MaPMT array by shifting the lenses relative to the MaPMTs.

lenses was tested for the case where the photons arrive at a varying angle α relative to the normal of the detector plane. LED runs were used for these tests.

Non-normal photon incidence leads to losses due to several sources. These include increased reflection at the surface of the lens, a reduction in effective area seen by photons from the mirror, which is proportional to $\cos \alpha$, and a shift in the image on the MaPMT PC. Provided the image is fully contained within the back surface of the lens, which is in front of the MaPMT's PC, the loss due to the shift can be completely recovered by displacing the lens array relative to the MaPMTs. An ideal displacement is such that the photon image is fully contained within the sensitive area, as illustrated in Fig. 20.

Columns of 8 pixels in each MaPMT were defined as shown in Fig. 20. The hits per pixel per event averaged over a column is shown in Figs. 21(a)–(d), for different angles of incidence and lens displacements. It can be seen that ideal displacements of 4.5 and 5.8 mm were achieved for α of 20° and 30°, respectively. A number of the lenses had blackened sides, while others had diffuse sides separated with white paper. The effect of reflection from the diffuse sides leads to a small increase for column 1, which can be seen in Figs. 21(c) and (d).

Table 7 summarises the results at different angles α , where an ideal displacement in the lenses had been introduced; measurements are shown separately for lenses with blackened sides and lenses with diffuse sides. Results are compared



Fig. 21. Average number of hits per pixel as a function of column number. Light was incident from the right (column 8) at angle α . Four different configurations of incident light and lens displacement are shown: (a) $\alpha = 0^{\circ}$, (b) $\alpha = 20^{\circ}$ and displacement = 2.5 mm, (c) $\alpha = 20^{\circ}$ and displacement = 4.5 m, and (d) $\alpha = 30^{\circ}$ and displacement = 5.8 mm.

with the expectation from the 0° case, considering all the contributions to the loss of photons mentioned above.

For the 20° case, the loss is dominated by the reduction in effective area, while for the 30° case, a significant fraction of the lens image is outside the back surface of the lens. The disagreement between expected and measured values of 30° with diffuse sides is possibly due to some light being

Table 7

Efficiency at different angles relative to normal incidence. The expectations for 20° and 30° are normalised to the observed value at 0°

Angle of incidence (°)	Blackened		Diffuse	
	Observed (%)	Expected (%)	Observed (%)	Expected (%)
20	88	91	94	91
30	74	72	82	73

reflected back onto the PC from the lens sides, a contribution not included in the calculation of the expected value.

5. Charged particle studies

To study the effect of charged particles incident upon an MaPMT a single tube was placed, with its axis horizontal,¹⁰ on a horizontal rotating platform in the beam line. Data were taken with $120 \,\text{GeV}/c$ pions traversing the MaPMT, with and without a quartz lens. Angles were scanned in the horizontal plane ranging from 0° , corresponding to charged particles incident on the MaPMT lens (or window), to 180°, corresponding to charged particles incident on the back of the MaPMT. The particle's impact point and trajectory was determined using the silicon telescope. For this analysis, only events with a single hit in each plane of the telescope were considered. The set-up and definition of the geometry are indicated in Fig. 22.

The configuration was modelled in a dedicated simulation which included a full description of the optical properties of the MaPMT lens, window and the gap between the two. The properties of the PC, other than the net quantum efficiency, were assumed to be the same as those measured in Ref. [27].



Fig. 22. A schematic of the set-up for the charged particle studies, showing the silicon telescope, the angle definition and the centre of rotation (the centre of the lens).

Fig. 23 shows the mean number of MaPMT hit pixels per charged particle as a function of the horizontal position of the particle in the silicon telescope, for different angles of beam incidence. In the vertical coordinate, the charged particle trajectory was limited to a band of $\pm 5.2 \text{ mm}$ (4 silicon pixels) around the centre of the lens. Superimposed are the results from simulation, with the grey shading indicating the changes observed when the parameters in the optical modelling are varied within reasonable limits. The agreement between data and simulation is satisfactory.

The quartz lens provides a significant radiator length. However, there is no optical coupling made

¹⁰The photodetector axis is defined as the normal direction to the photocathode, through its centre.



Fig. 23. The mean number of hit pixels seen for incident charged particles for an MaPMT with lens. The results are plotted against the horizontal coordinate in the silicon telescope, and at different incident angles. Data are represented by the points and simulation by the solid line. The grey shading indicates the variations observed when the parameters of the optical modelling are varied within reasonable limits.

between the lens and the window, and consequently many of the Cherenkov photons produced in the lens undergo internal reflection at this boundary. For small incoming particle angles fewer than 10 pixels are hit. At angles around 45° many more of the photons produced in the lens are transmitted and penetrate the window, resulting in up to 30 hit pixels. At 90° a sharp spike is seen for those particles which transverse the window parallel to the PC. At larger angles an average of less than 10 pixels is hit.

The MaPMT ADC spectra were fitted to establish how many photoelectrons contributed to each hit pixel. Significant variation was found, but certain pixels were observed to receive more than five photoelectrons. These results were consistent with the simulation.

With the flux of charged particles on the photodetectors expected in the LHCb experiment, such effects will not significantly degrade the performance of the RICH detectors [3].

A similar analysis was performed on data taken with a single MaPMT without a lens. Here about 5 hits per event were observed, with little dependence on the incident angle. In the special case where the particle traverses parallel to the PC, similar behaviour is seen to the data taken with a lens. These results are all well described by the simulation.

6. Magnetic field studies

The MaPMTs must operate in the fringe fields of the LHCb dipole magnet. The strength of these fringe fields is expected to be as high as 30 G in the vicinity of the RICH photodetectors [2].

The sensitivity of the MaPMT to a magnetic field has been studied by placing a single tube within a Helmholtz coil providing an axial magnetic fields of up to 30 G. Using an LED light source, the relative efficiency of a tube has been measured for magnetic fields transverse (B_x and B_{ν}) and longitudinal (B_z) to the photodetector axis. Fig. 24(a) shows the relative efficiency as a function of the magnetic field strength for the three field orientations. This demonstrates that the MaPMT has little sensitivity to transverse magnetic fields up to 30 G. For longitudinal fields of $B_z \ge 10 \,\mathrm{G}$ the efficiency of the MaPMT deteriorates. The loss contains a small component resulting from a decrease in gain. However, the loss occurs mostly in the two edge rows, parallel to the x-axis where the focusing of the photoelectrons onto the first dynode is most sensitive to magnetic fields; such a loss cannot be recovered. At $B_z = 30 \,\mathrm{G}$ the collection efficiency of the edge rows is reduced to 50% with respect to that at $B_z = 0 \,\mathrm{G}.$

The effect of shielding the MaPMT with a mumetal tube of square cross-section with a width 30 mm, length 60 mm and wall thickness 0.9 mm was measured. The shield enclosed the tube and extended beyond the MaPMT window face by a distance, d. Fig. 24(b) shows the relative efficiency as a function of B_z without and with the shield, for two values of d (13 and 32 mm). The mu-metal tube is effective in reducing the efficiency loss; with



Fig. 24. The efficiency relative to 0 G as a function of the magnetic field strength for (a) transverse $(B_x \text{ and } B_y)$ and longitudinal (B_z) fields. In (b) the effect shielding the MaPMT with a mu-metal tube at different *d* (see text) is shown.

an extension of 32 mm or more there is no significant loss is efficiency due to the 30 G field.

7. Summary and conclusions

The performance of an MaPMT array equipped with lenses has been shown to agree well with expectations. The use of lenses to reduce the loss due to insensitive regions of the MaPMT has led to the expected improvement in the number of photoelectrons detected. The MaPMTs have been equipped with pipelined electronics to capture the data at 40 MHz which has performed well and Cherenkov rings have been clearly identified.

The effect of charged particles at different angles of incidence on an MaPMT equipped with a lens was found to agree well with expectations. Individual MaPMTs have been successfully operated in stray magnetic fields up to 30 G with appropriate mu-metal shielding.

Given the results reported in this paper, combined with the successful operation of a similar system by HERA-B [7], the conclusion is that the MaPMT meets the photodetector requirements of the LHCb RICH counters.

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References

- E. Albrecht, et al., Nucl. Instr. and Meth. A 456 (2001) 233.
- [2] The LHCb Collaboration, LHCb technical proposal, CERN/LHCC/98-4.
- [3] The LHCb Collaboration, LHCb RICH technical design report, CERN/LHCC/2000-37.
- [4] J. Rosen, Nucl. Instr. and Meth. A 408 (1998) 191.
- [5] J. Pyrlik, Nucl. Instr. and Meth. A 446 (2000) 299.
- [6] D.R. Broemmelsiek, Nucl. Instr. and Meth. A 433 (1999) 136.
- [7] I. Arino, et al., Nucl. Instr. and Meth. A 453 (2000) 289.
- [8] R. Forty, Use of lenses to increase the RICH photodetector coverage, LHCb/98/038.
- [9] E. Albrecht, et al., Nucl. Instr. and Meth. A 411 (1998) 249.
- [10] O. Toker, et al., Nucl. Instr. and Meth. A 340 (1994) 572.
- [11] R. Abjean, et al., Nucl. Instr. and Meth. A 292 (1990) 593.
- [12] MDM de Fez-Lazo, et al., Nucl. Instr. and Meth. A 382 (1996) 533.
- [13] M. Raymond, et al., London 1997, Electronics for LHC Experiments, CERN/LHCC/97-60 (1997) 158.
- [14] L.L. Jones, et al., Rome 1998, Electronics for LHC Experiments, CERN/LHCC/98-36 (1998) 185.
- [15] Philips Semiconductors, The I²C-bus specification, Version 2.1, January 2000.
- [16] The CMS Collaboration, The tracker system project technical design report, CERN/LHCC/98-6.

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- [17] M. Raymond, et al., Nucl. Instr. and Meth. A 351 (1994) 449.
- [18] J. Christiansen, Requirements to the L0 front-end electronics, LHCb/99/029.
- [19] N. van Bakel, et al., Snowmass 1999, Electronics for LHC Experiments, CERN/LHCC/98-33 (1999) 167.
- [20] F. Anghinolfi, et al., IEEE Trans. Nucl. Sci. NS-44 (1997) 298.
- [21] M. Morrisey, SEQSI Manual, Rutherford Appelton Laboratory, unpublished.
- [22] S.A. Baird, et al., Snowmass 1999, Electronics for LHC Experiments, CERN/LHCC/98-33 (1999) 357.
- [23] J. Coughlan, CMS Front-End Driver PMC USER Manual, Rutherford Appleton Laboratory, unpublished.
- [24] I. Chikorov-Zorin, et al., Nucl. Instr. and Meth. A 456 (2001) 310.
- [25] P. Križan, et al., Nucl. Instr. and Meth. A 394 (1997) 27.
- [26] J. Rademacker, Nucl. Instr. and Meth. A 484 (2002) 432.
- [27] M.E. Moorhead, N.W. Tanner, Nucl. Instr. and Meth. A 378 (1996) 162.